Intro to the Cosmic Microwave Background

Chris Sheehy BNL June 20, 2017

Cosmological paradigm

Cosmological paradigm

The standard cosmological paradigm is an expanding Universe containing dark energy (A) and cold dark matter.

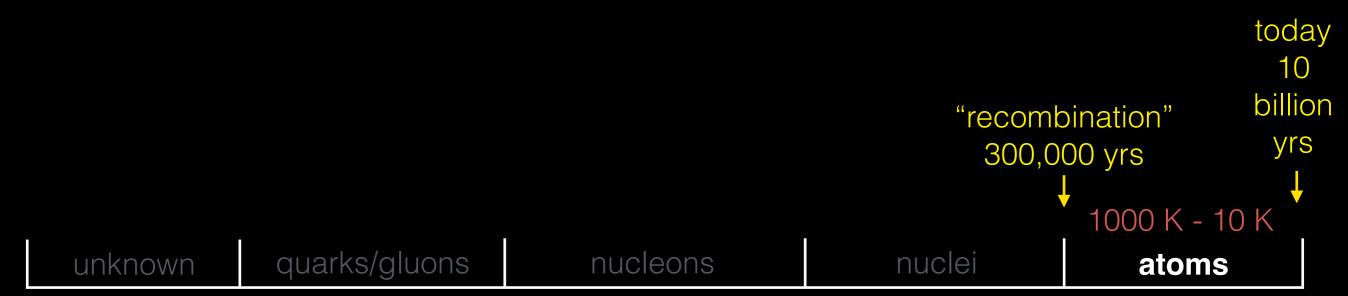


Cosmological paradigm

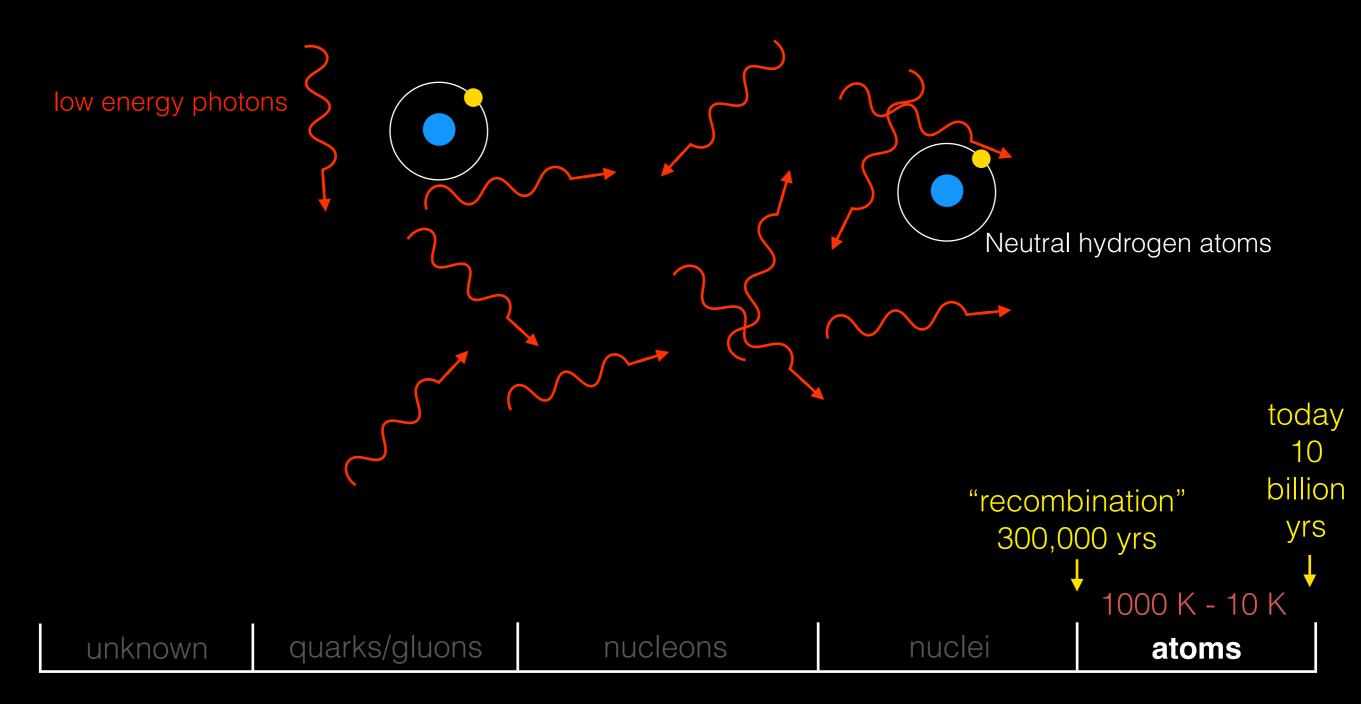
The standard cosmological paradigm is an expanding Universe containing dark energy (A) and cold dark matter.

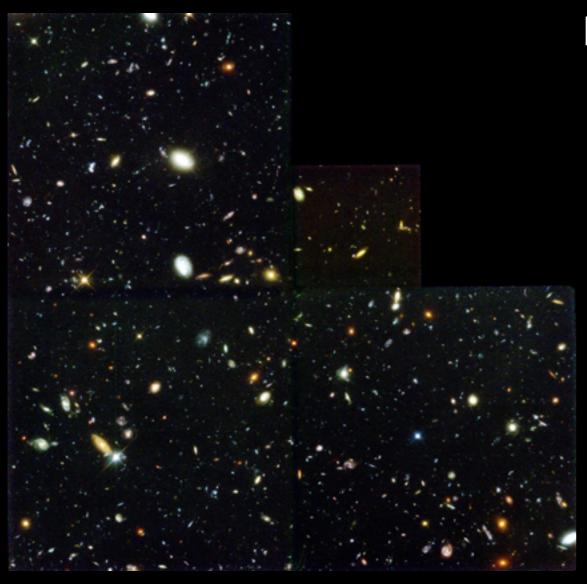
"\CDM"

If the Universe is expanding, then it used to be smaller, denser, and hotter.



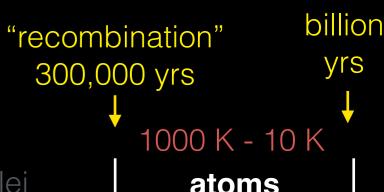
The universe at **low** temperature





Hubble Deep Field

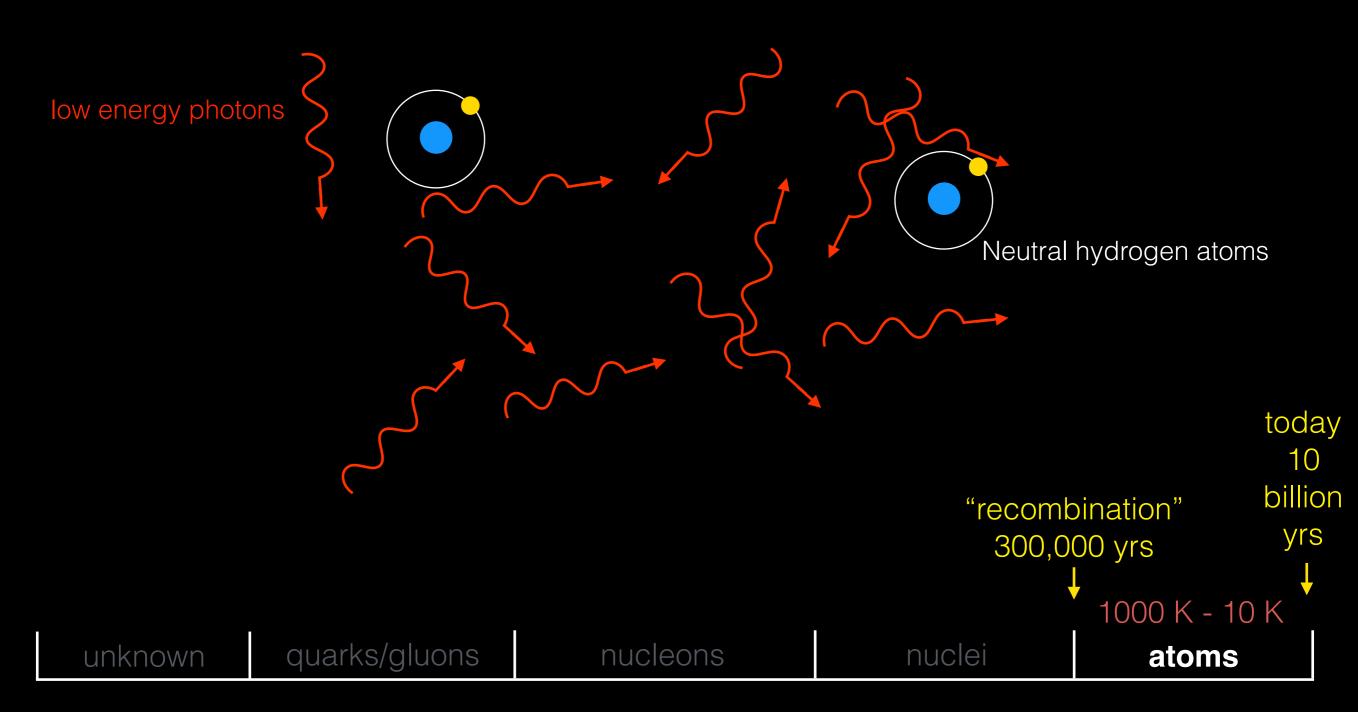
- sees back to first generations of stars and galaxies
- between the present and when the Universe is ~300,000 years old, the Universe is cool enough that neutral atoms can exist

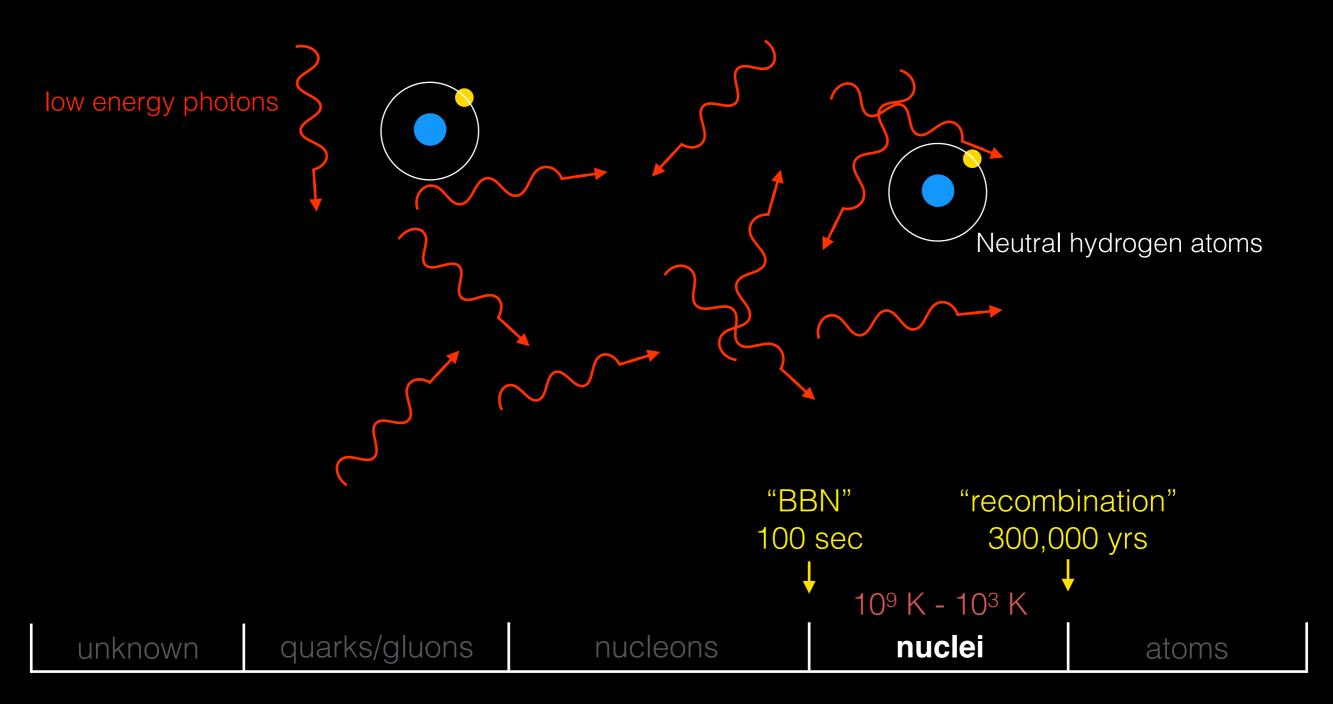


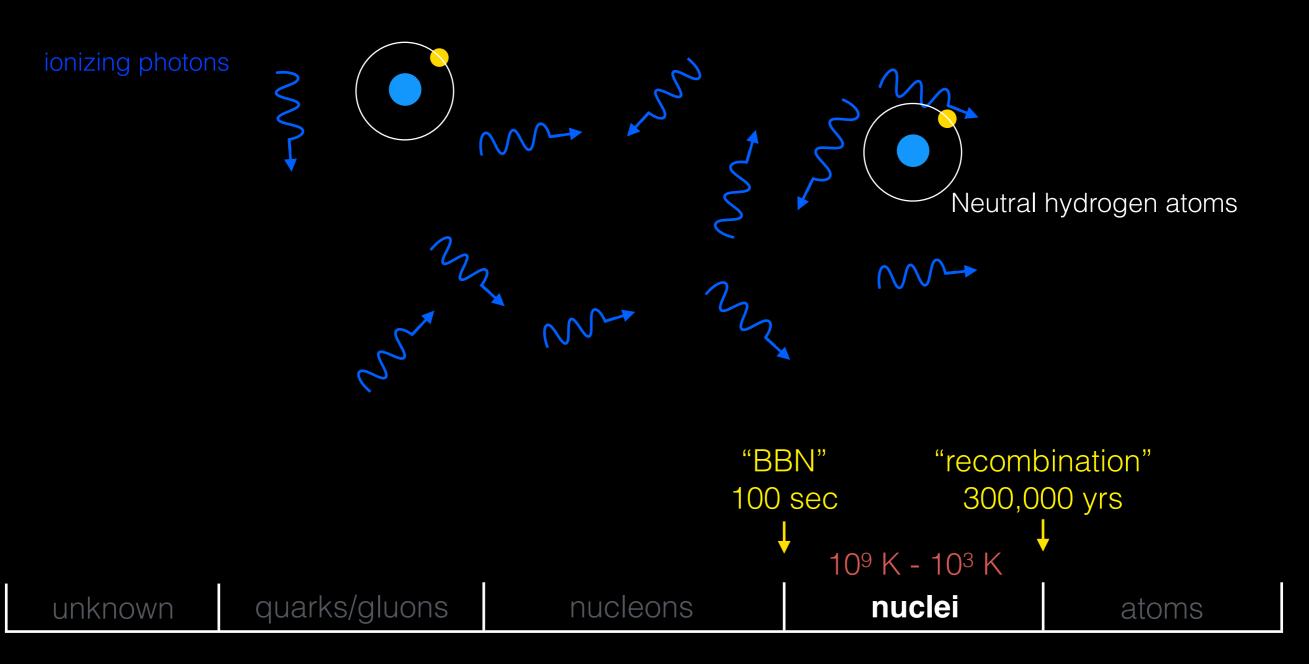
today

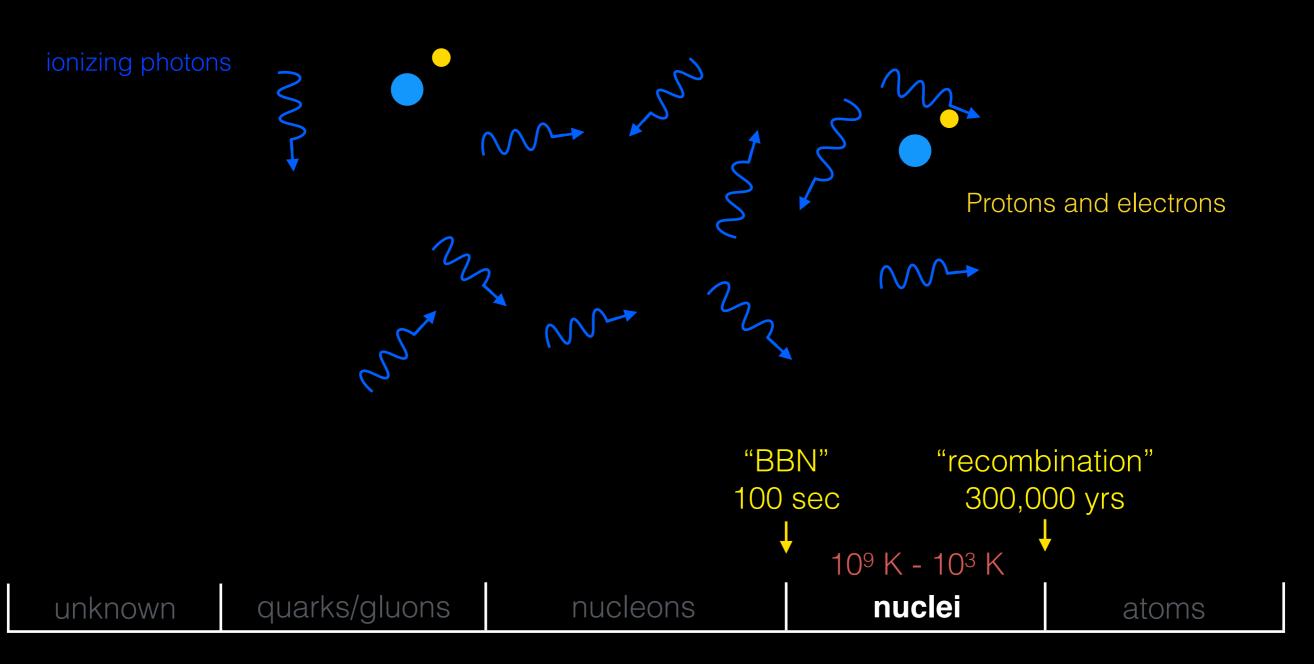
10

unknown quarks/gluons nucleons nuclei atoms

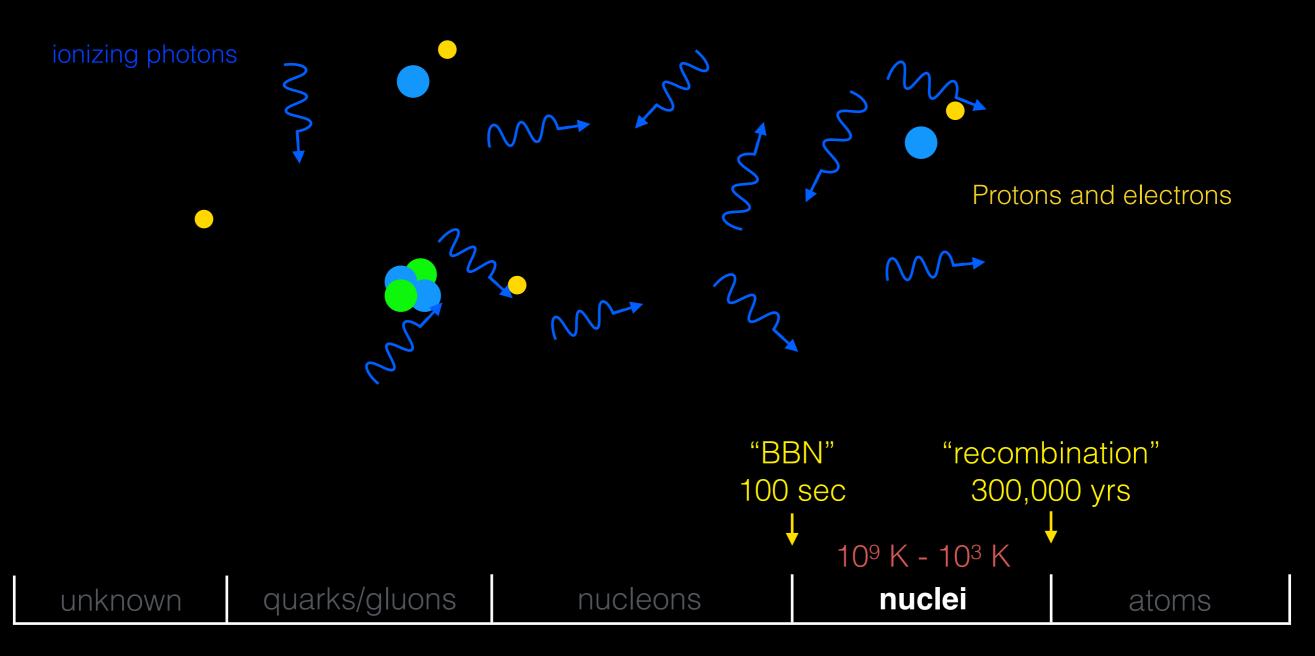




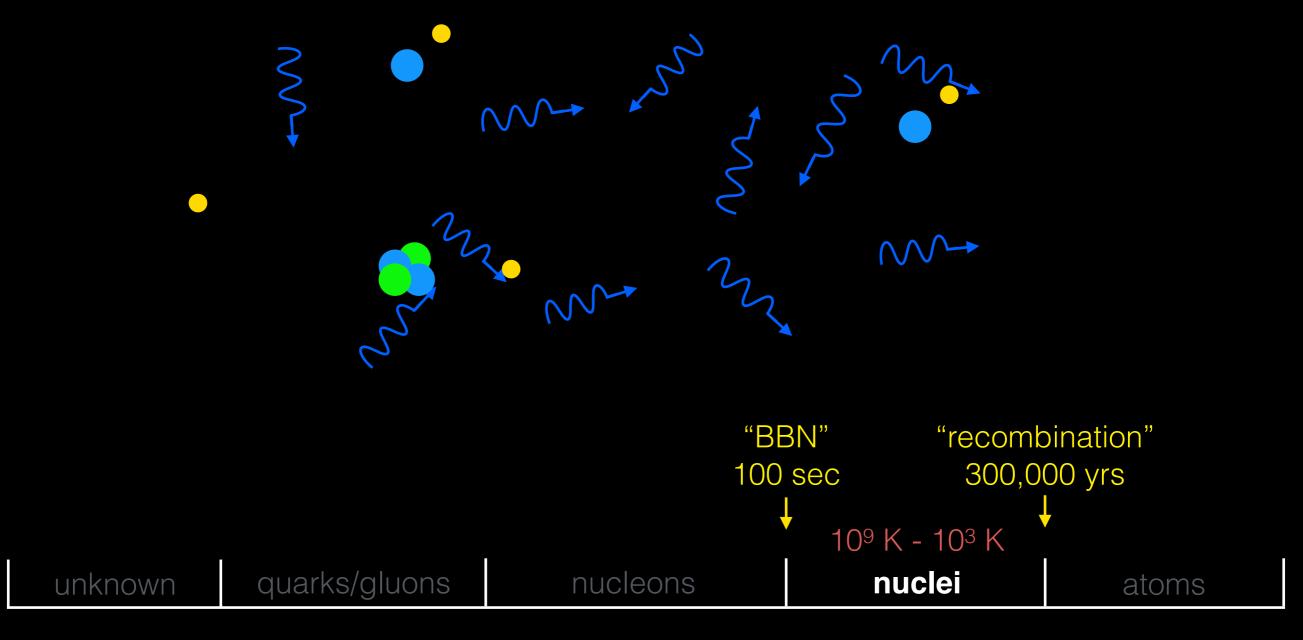




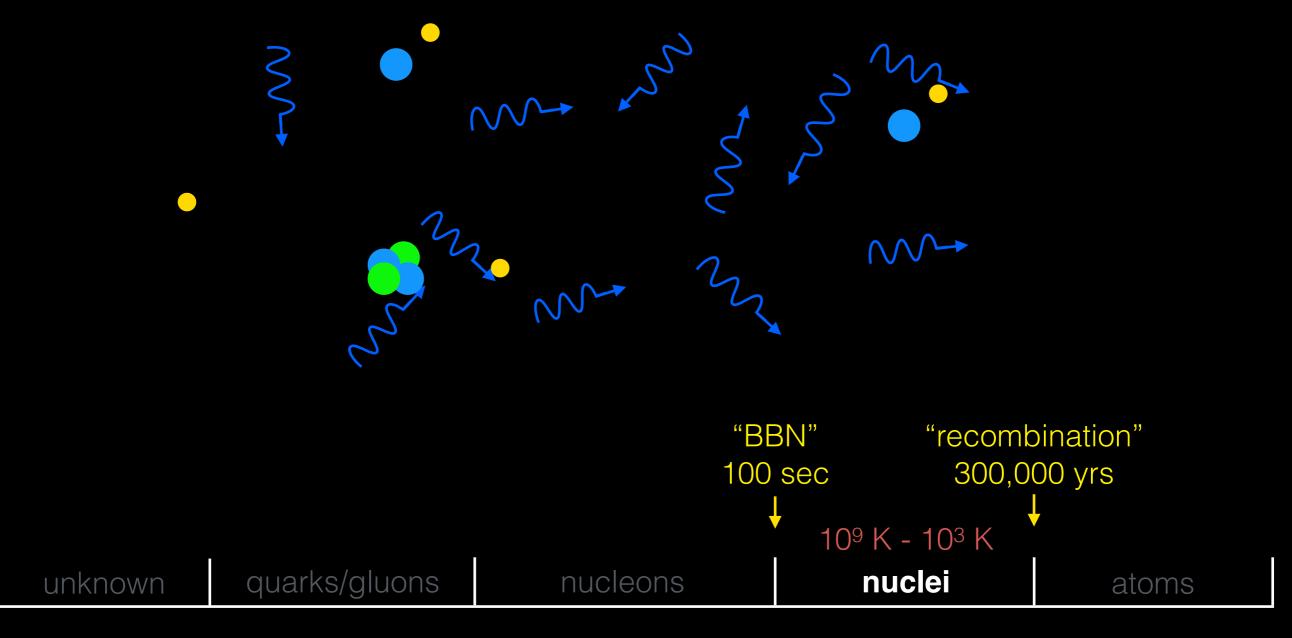
The universe at **high** (>3000 K) temperature: hydrogen and helium plasma + photons = the "photon/baryon fluid"



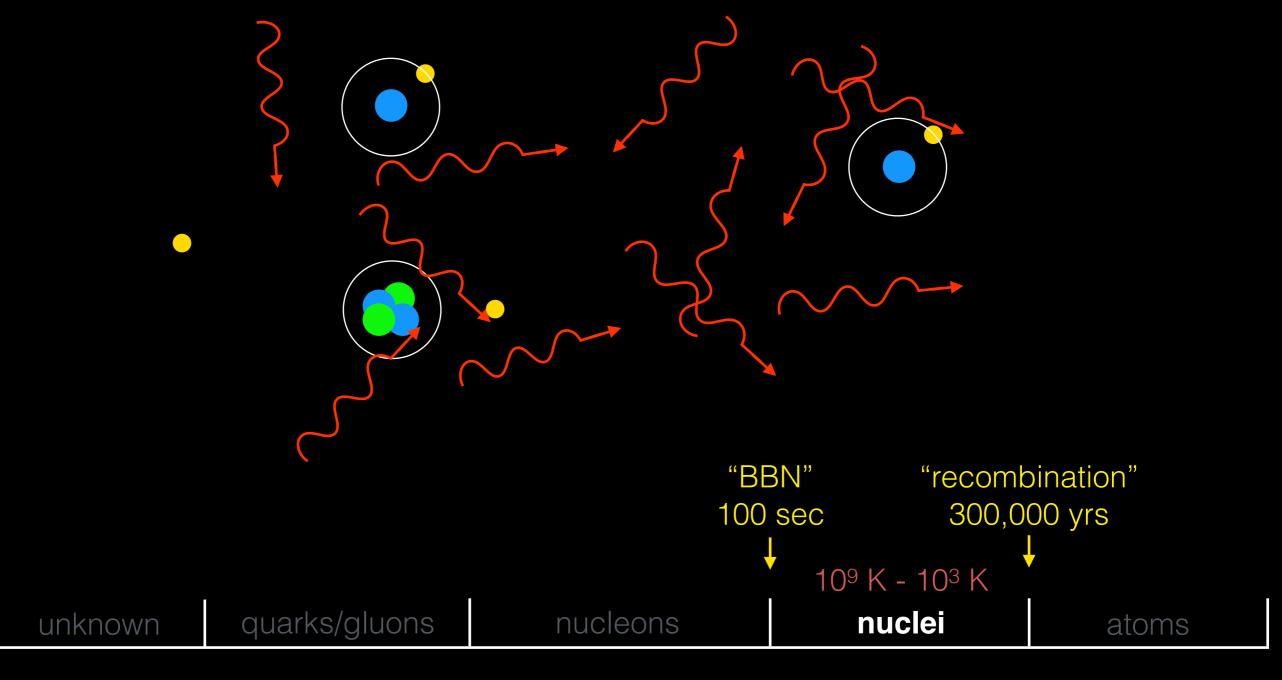
Free electrons have a high cross section to photons. Neutral hydrogen atoms do not. Efficient Thompson scattering makes the plasma opaque.



Going forward in time...



Going forward in time, when the Universe cools to ~3000 K, the protons and electrons "recombine," and the photons travel unimpeded through space.

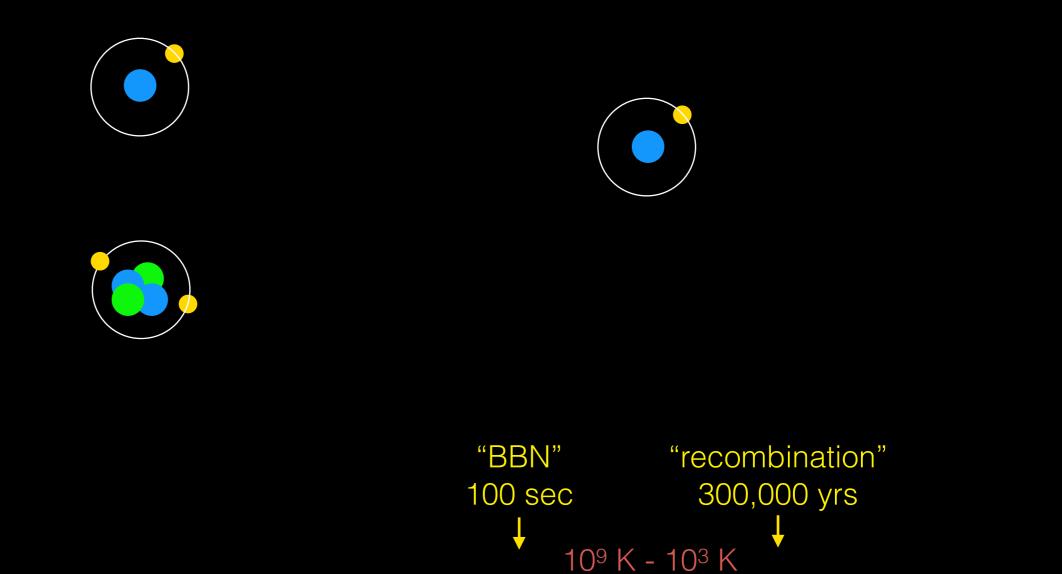


The photons heading in the right direction find their way to Earth.

nucleons

quarks/gluons

unknown

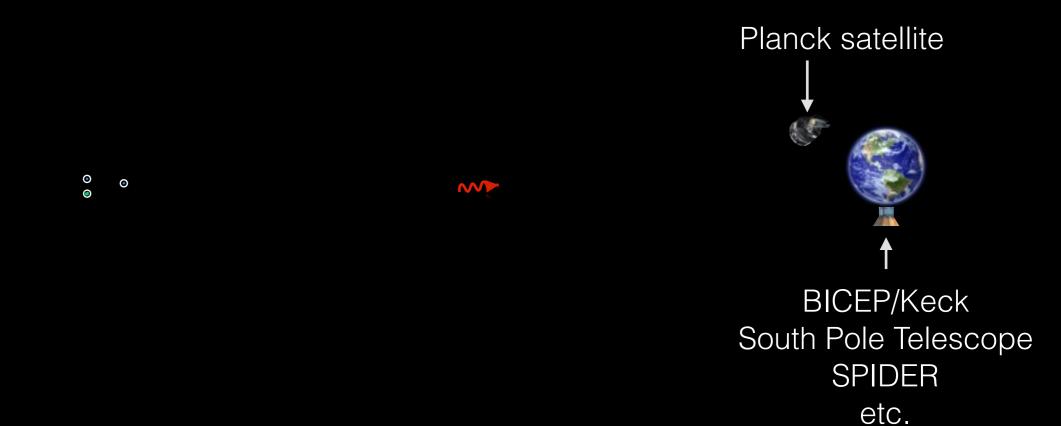


nuclei

going back in time (getting hotter)

atoms

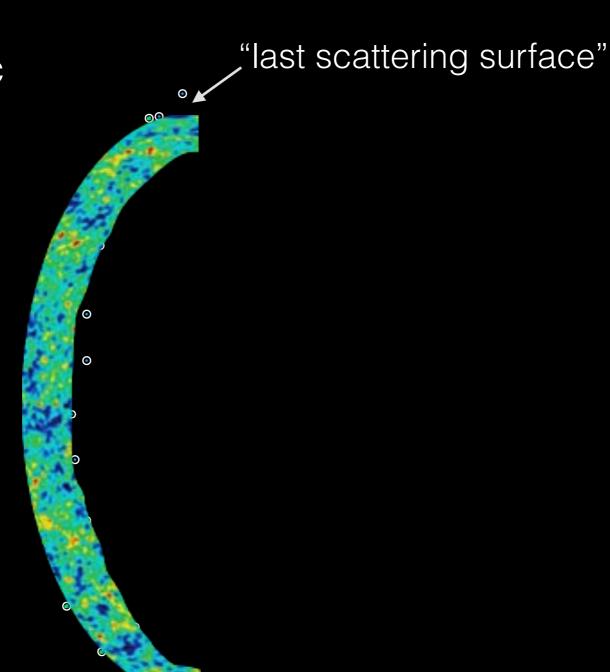
The photons heading in the right direction find their way to Earth.

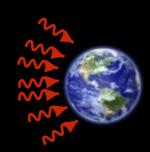


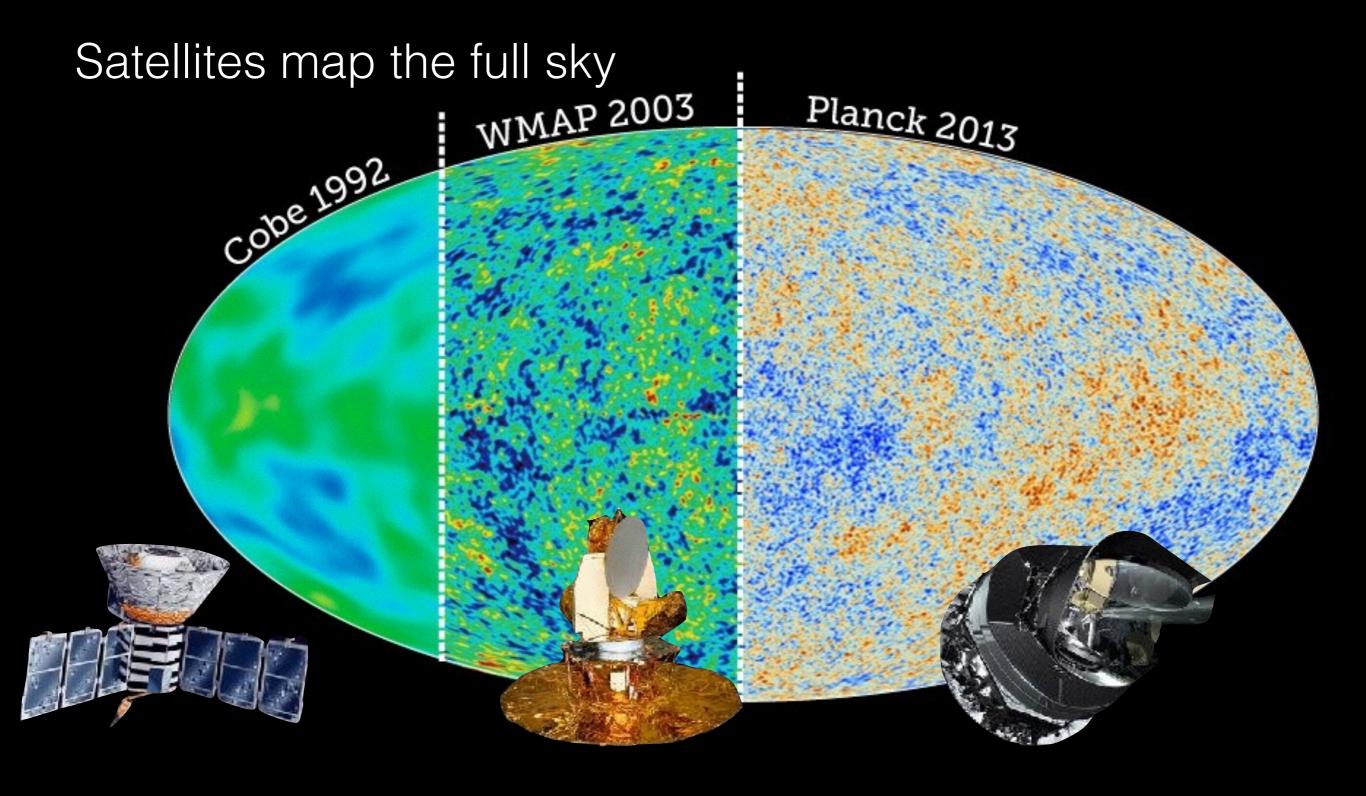
This is the Cosmic Microwave Background!

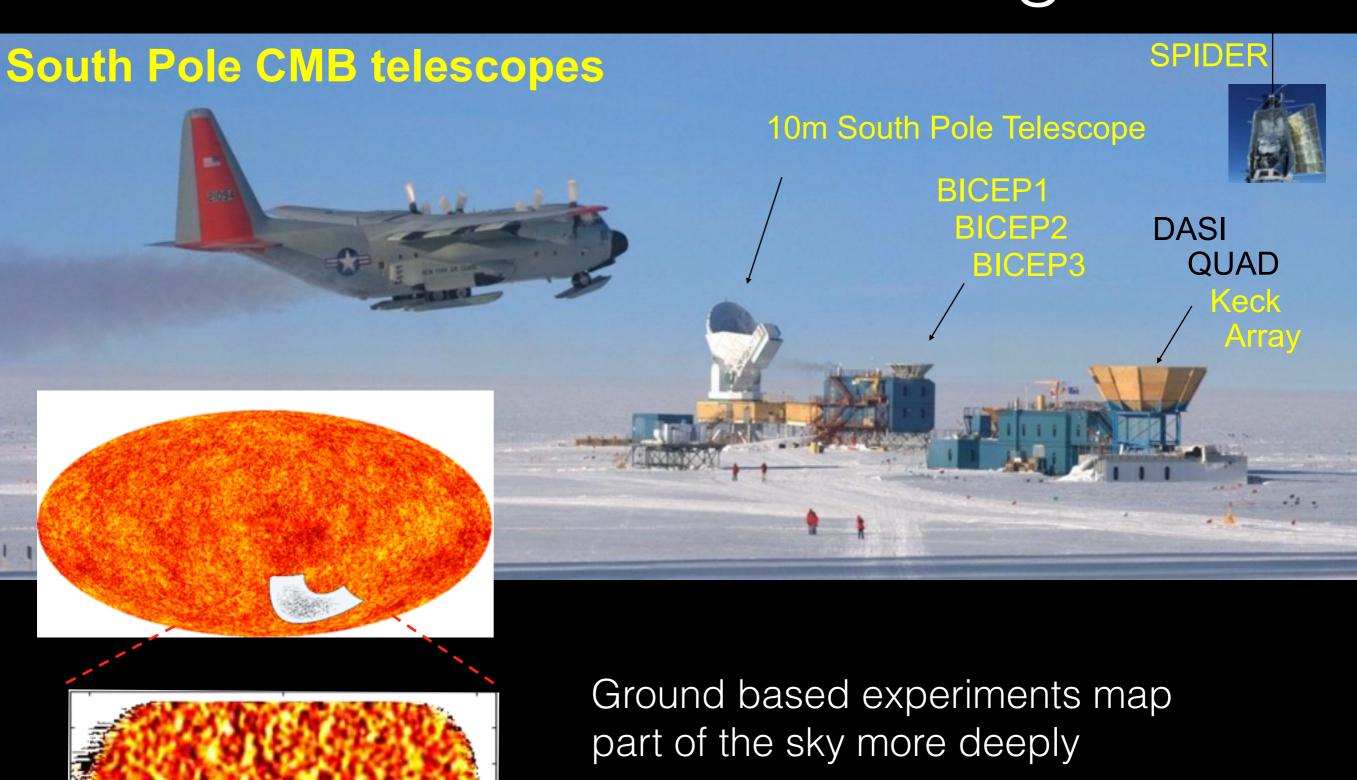
The fluctuations in intensity (anisotropy) trace the fluctuations in the density of the Universe.

$$\frac{\delta I}{I} \propto \frac{\delta \rho}{\rho} \sim 10^{-5}$$

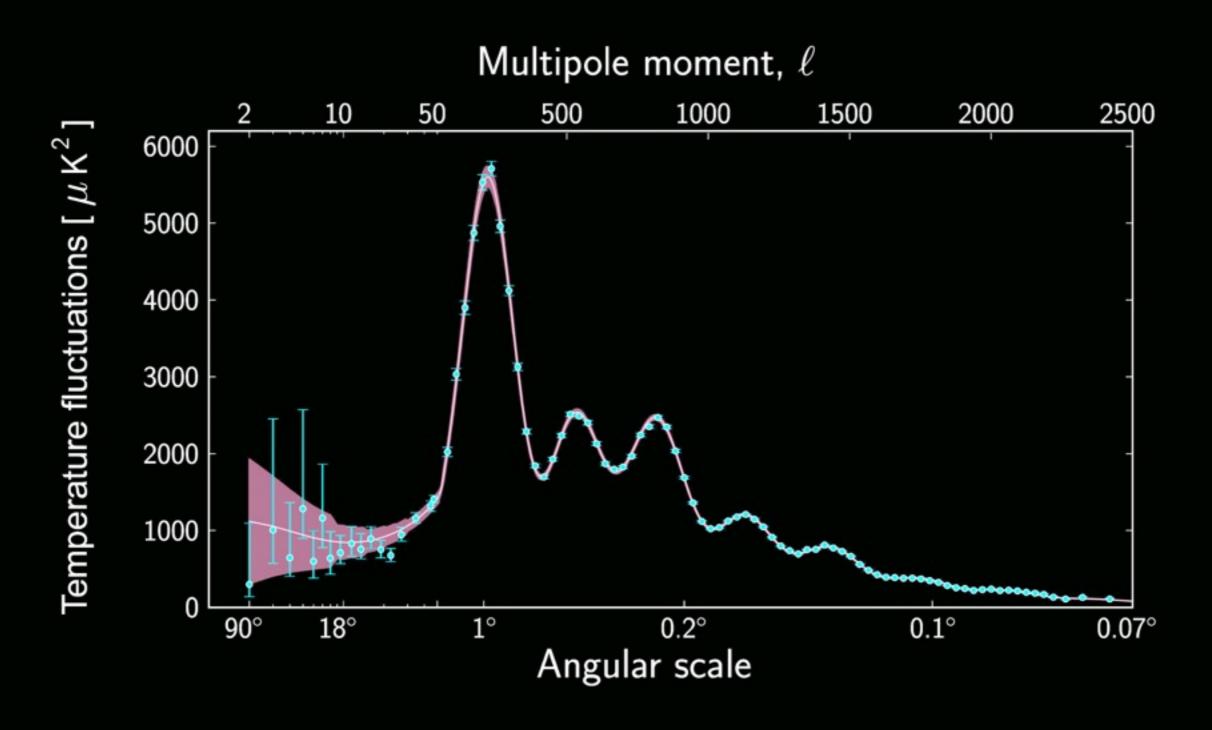








Planck temperature "angular power spectrum"



$$\mathsf{T}(\theta,\Phi) = \sum_{\ell=0}^{\infty} \sum_{m=-\ell}^{+\ell} a_{\ell,m} \, \mathsf{Y}_{\ell,m} \, (\theta,\Phi)$$

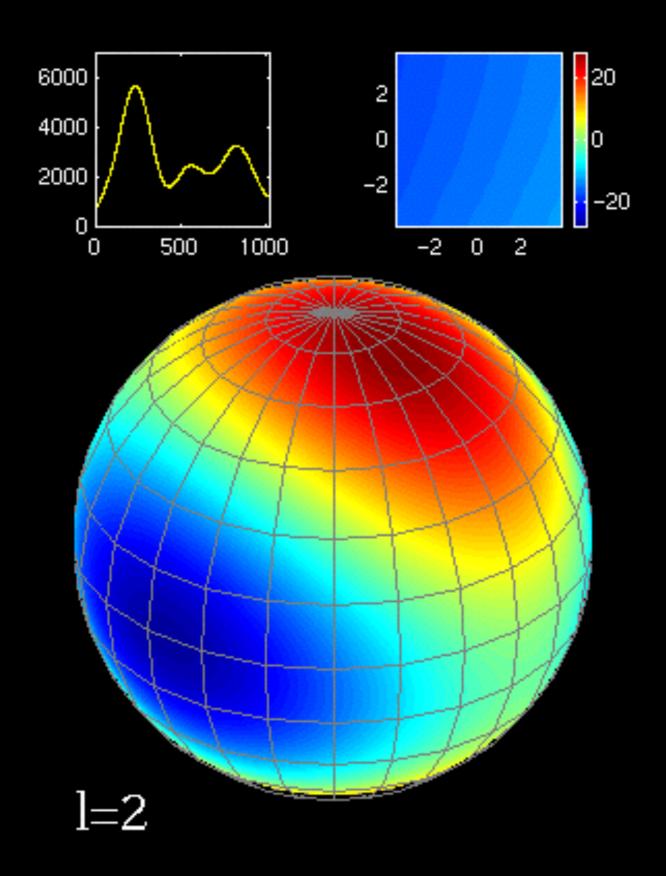
$$\ell = 0$$

$$\ell = 1$$

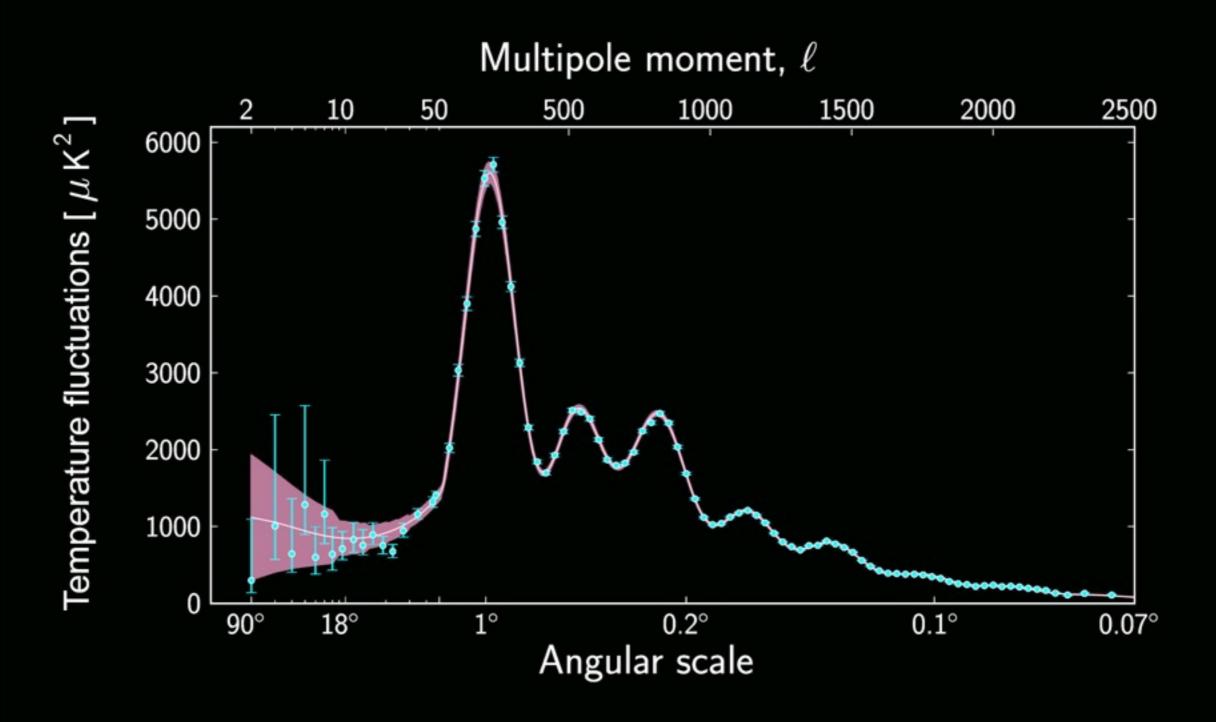
$$\ell = 2$$

$$\ell = 3$$

$$\ell =$$



Planck temperature "angular power spectrum"



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$$\ell = 0$$

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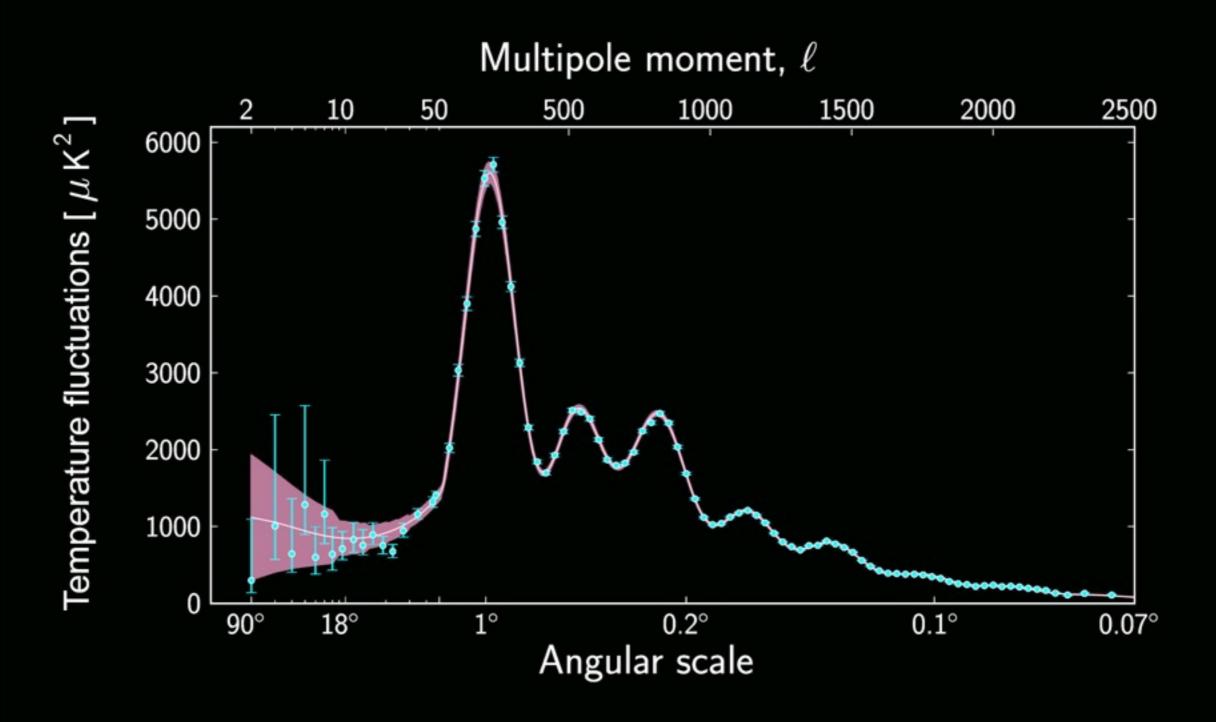
Typically, one sees the power spectrum plotted as

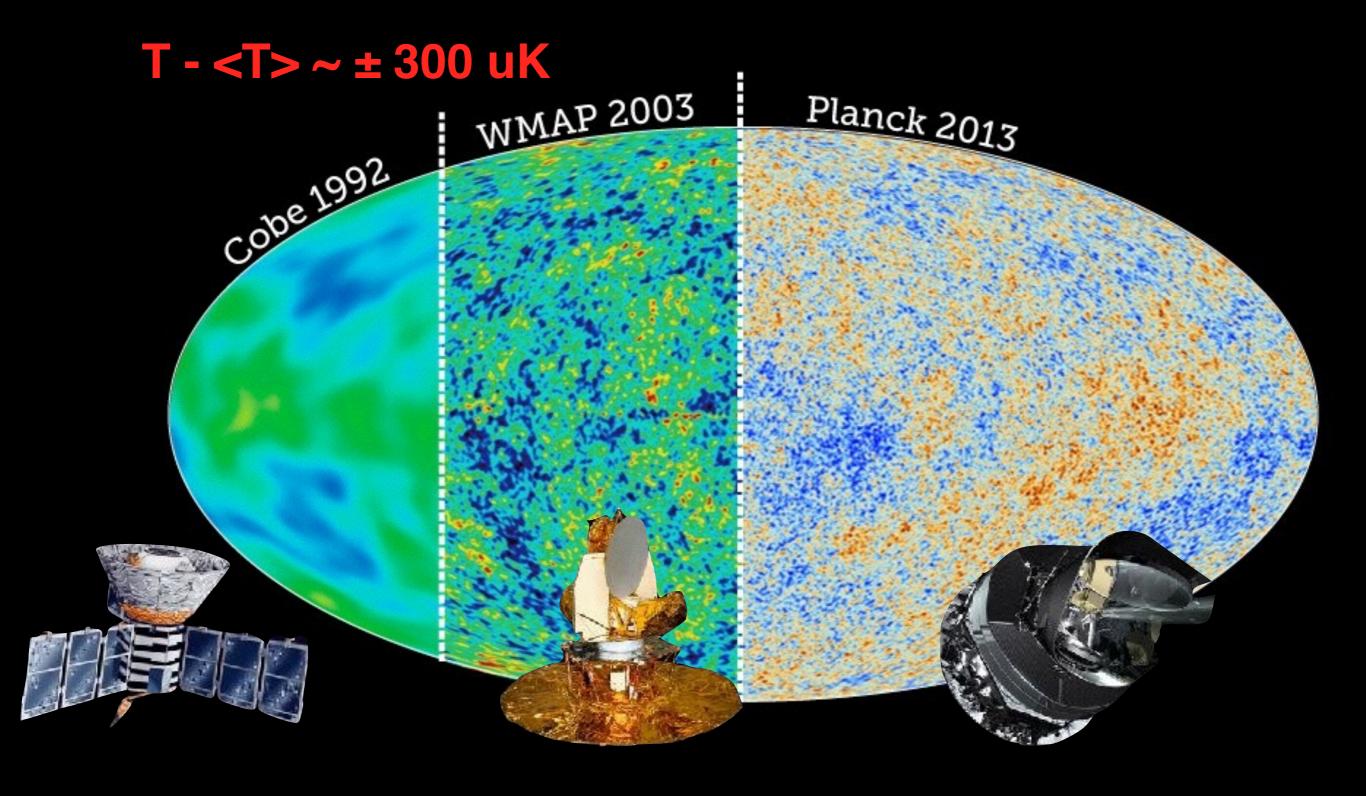
$$C_1 = \langle a_{lm}^2 \rangle$$

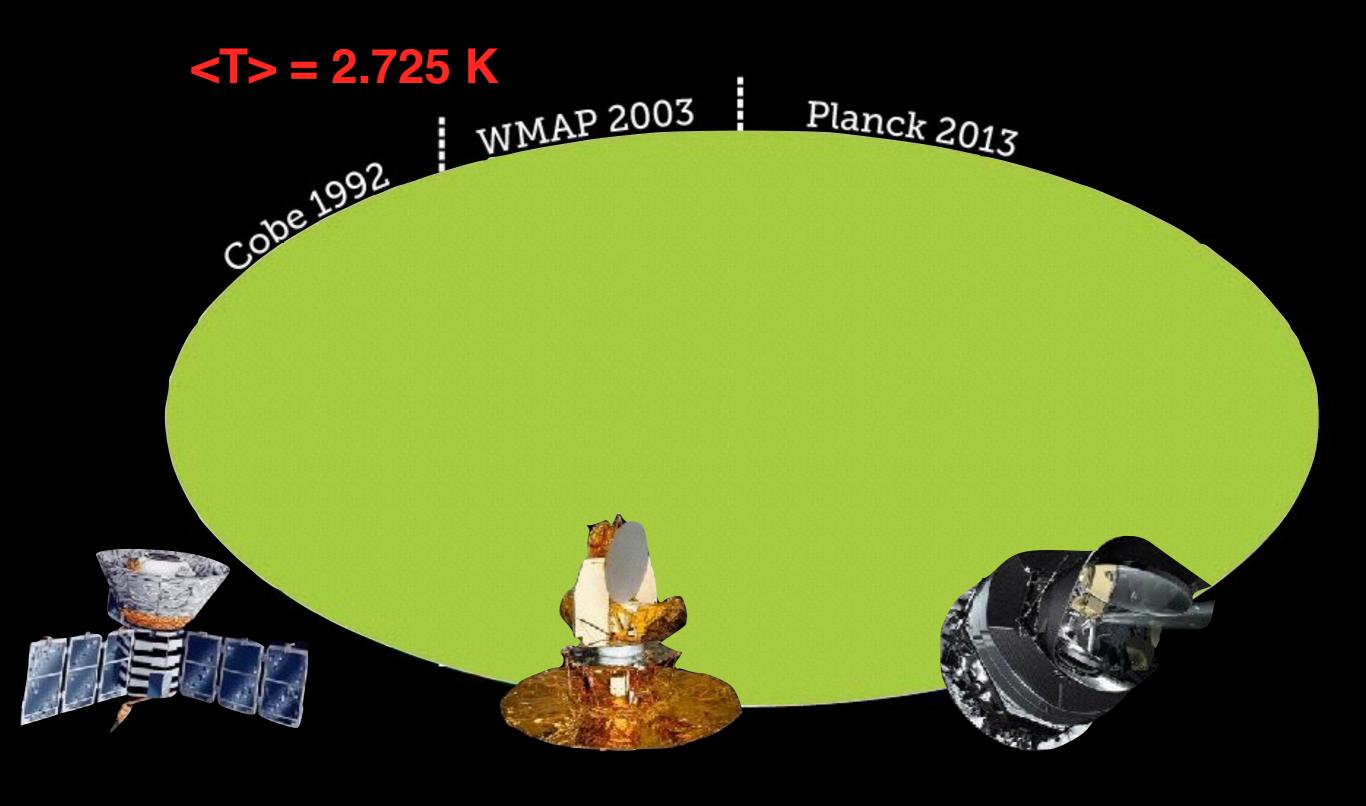
(e.g. the variance of the alm's).

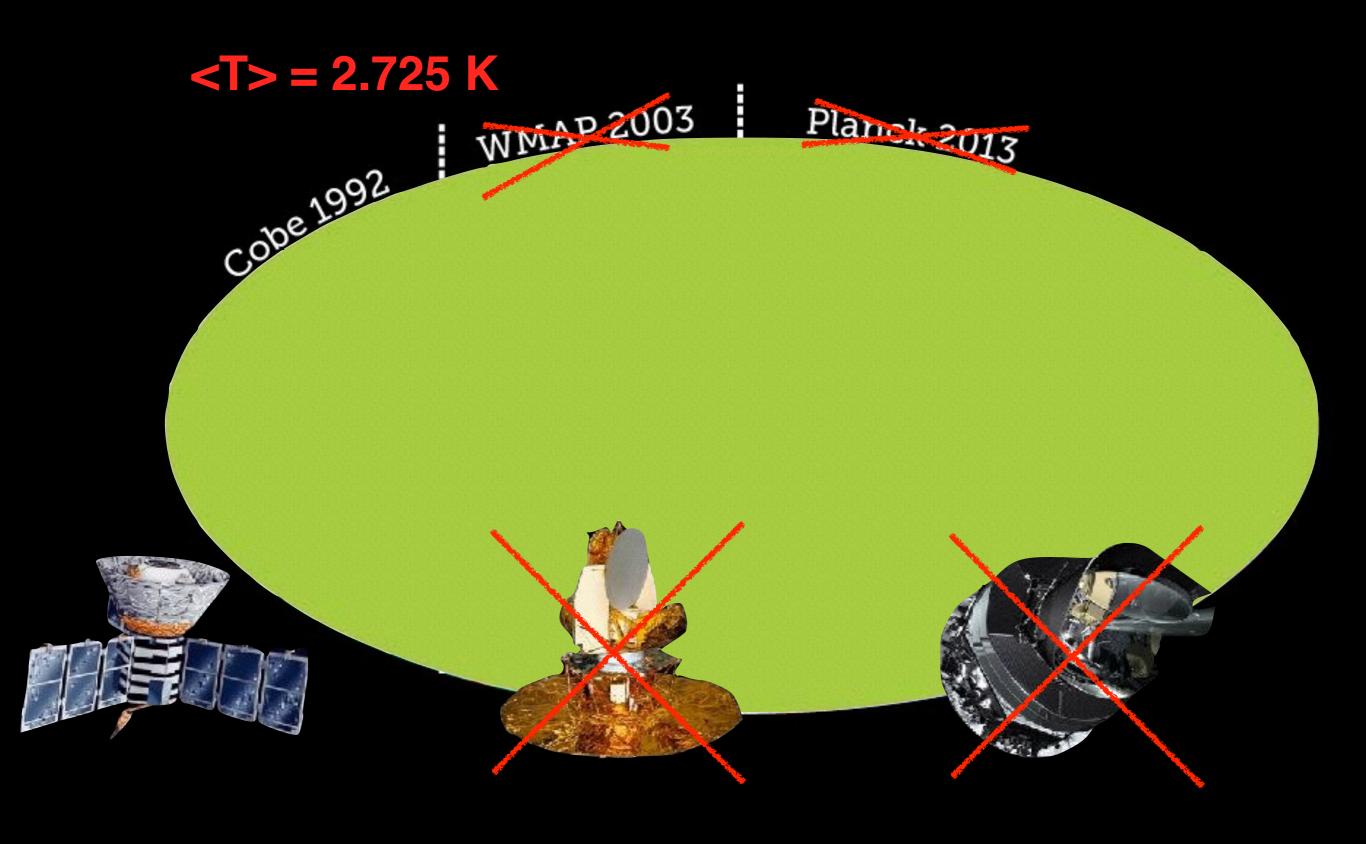
Oftentimes this is binned in to I bins and/or multiplied by the factor I(I+1)/2pi.

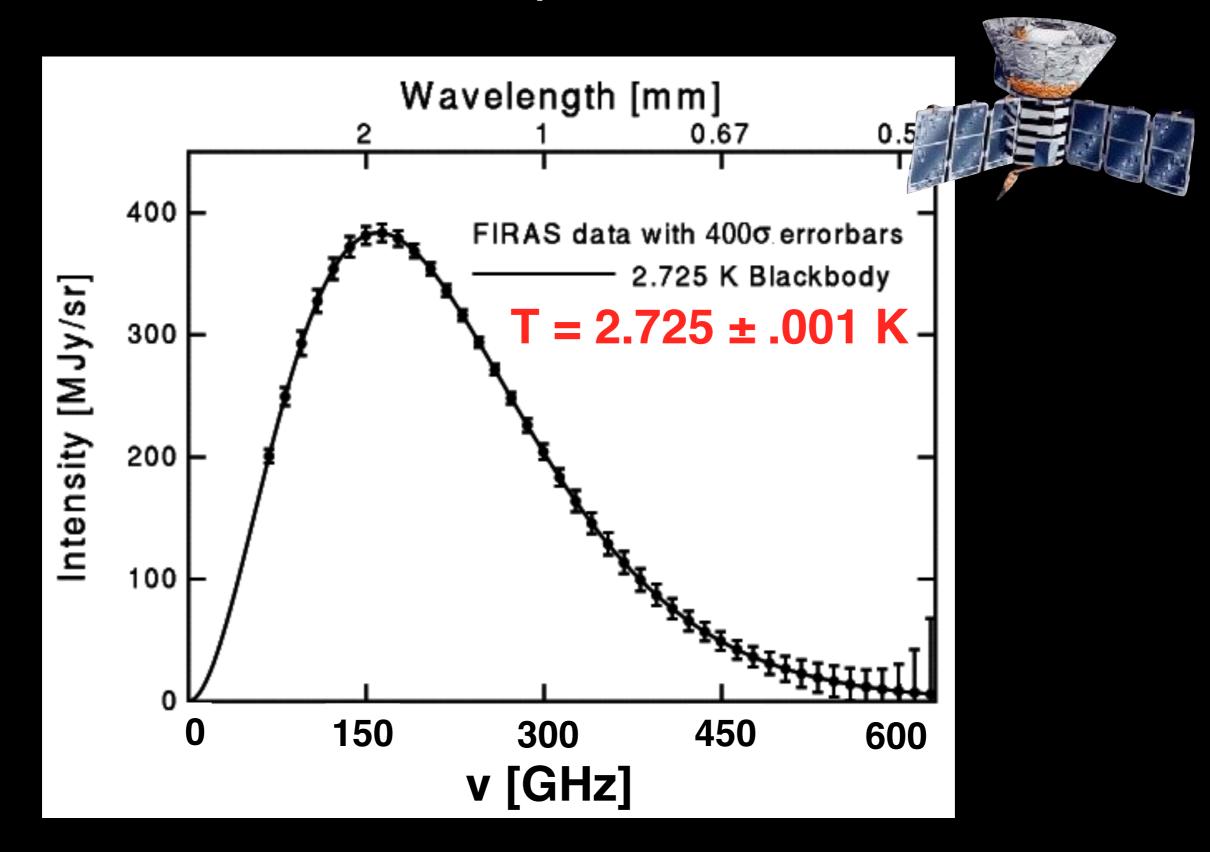
Planck temperature "angular power spectrum"





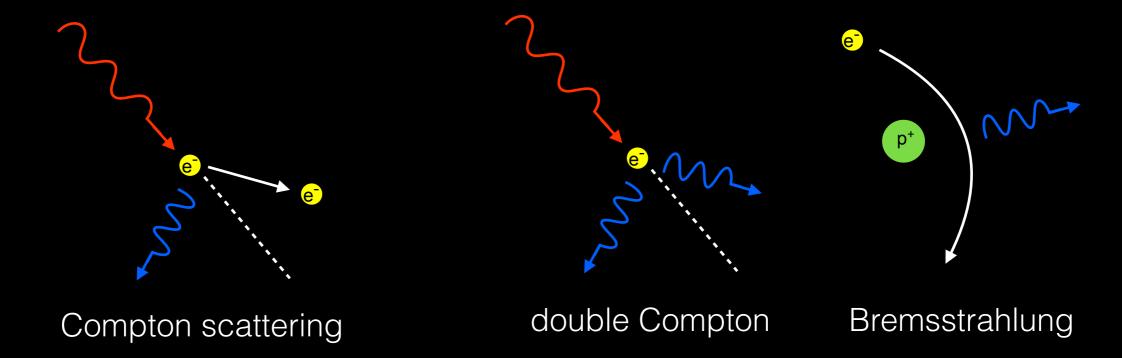






Why should the CMB be a blackbody?

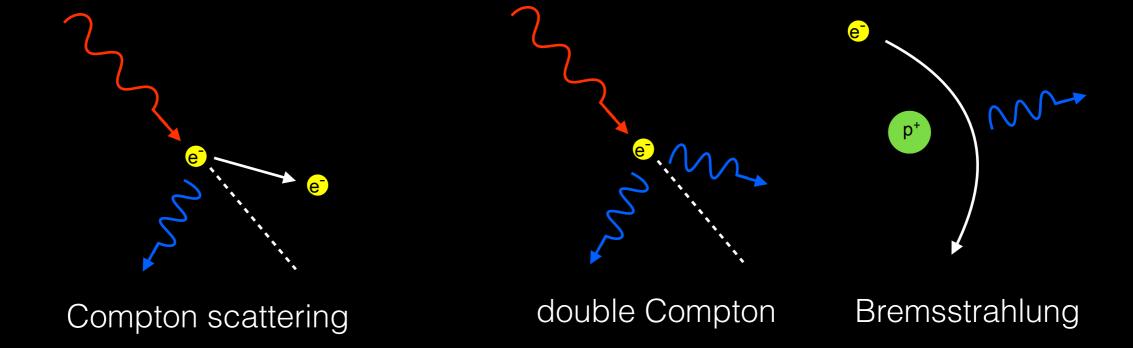
- Imagine some energy is injected into the primordial plasma
- Two things need to happen to "maintain" the blackbody photon spectrum:
 - photons and baryons are redistributed in energy by Compton scattering
 - 2. new photons are created by double Compton scattering and Bremsstrahlung

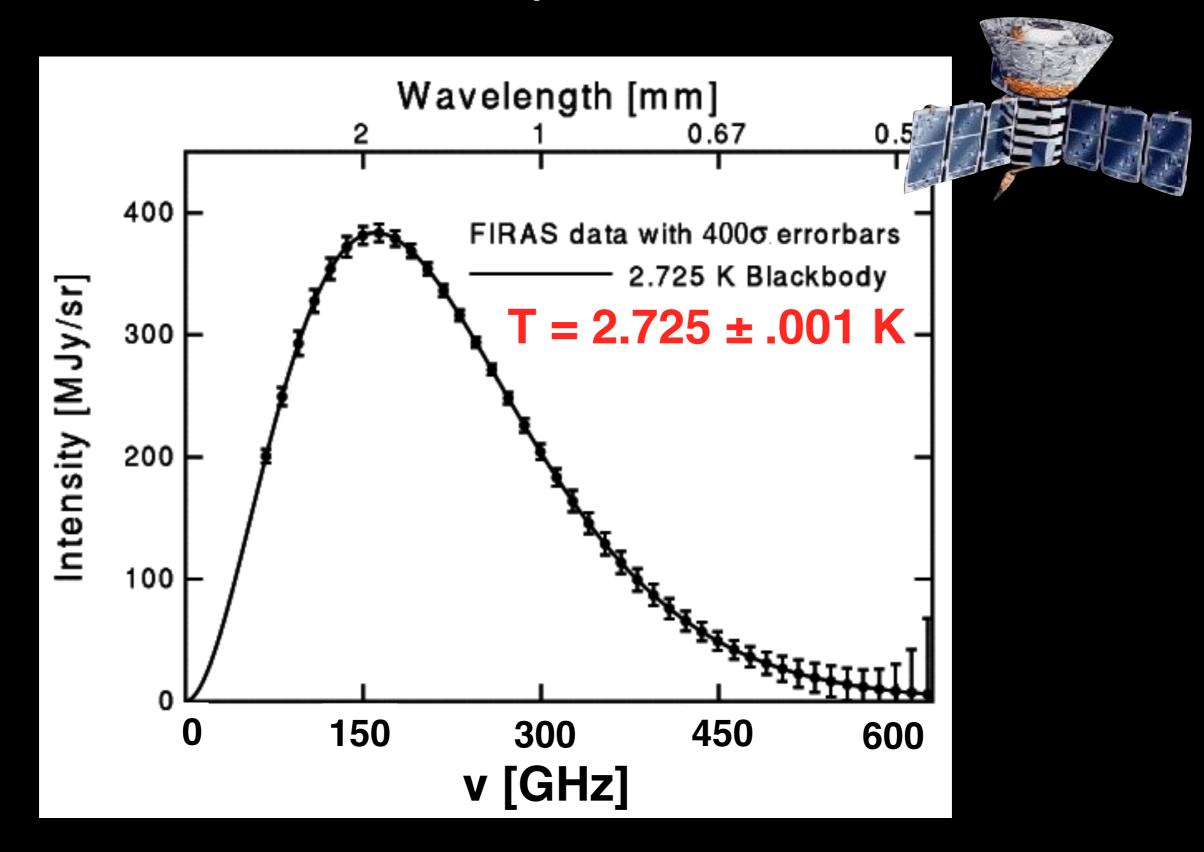


• At z > 2 x 10⁶, both processes are very efficient and any energy injected into the plasma is quickly thermalized. One parameter, T, is needed to describe the distribution of photons:

$$n(E) = 1 / [e^{E/kT}-1]$$
 (Planck spectrum)

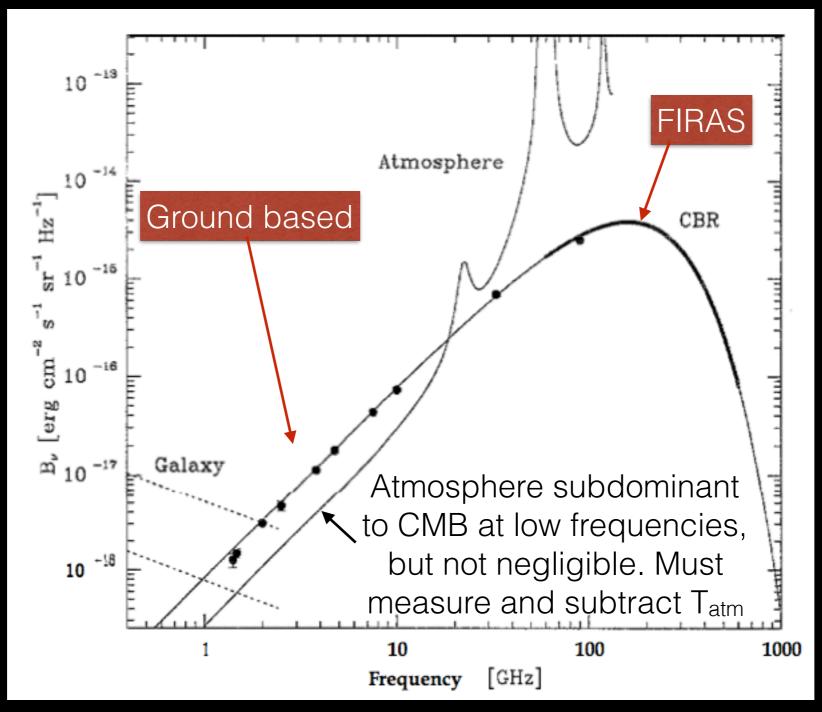
 At z < 2 x 10⁶, these processes become inefficient and any energy injected in the plasma (particle annihilation, heating, etc.) would not be able to thermalize and a deviation from a blackbody would be observed.





Ground based CMB spectrum

Even before FIRAS, we knew $T_{CMB} \pm .06$ K from ground based measurements and $\pm .02$ K from balloons



The CMB spectrum data is 30 years old and has not been improved upon since then! These instruments need very good cryogenic calibrators.

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All the CMB telescopes you hear about now do not measure absolute intensity, they measure the "angular anisotropy" of the CMB.

This includes the ground based and space based missions.

But if you can't measure T to better than 0.02 K from the ground, how do the ground based telescopes make sub-uK level measurements of the anisotropy?

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Answer: don't make absolute intensity measurements, make a differential measurement between two different points on the sky.

BICEP2 and Keck Array



Keck Array 2011-present





South Pole is high (~10,000 ft) and dry and has a very stable atmosphere during the 6 month long night.

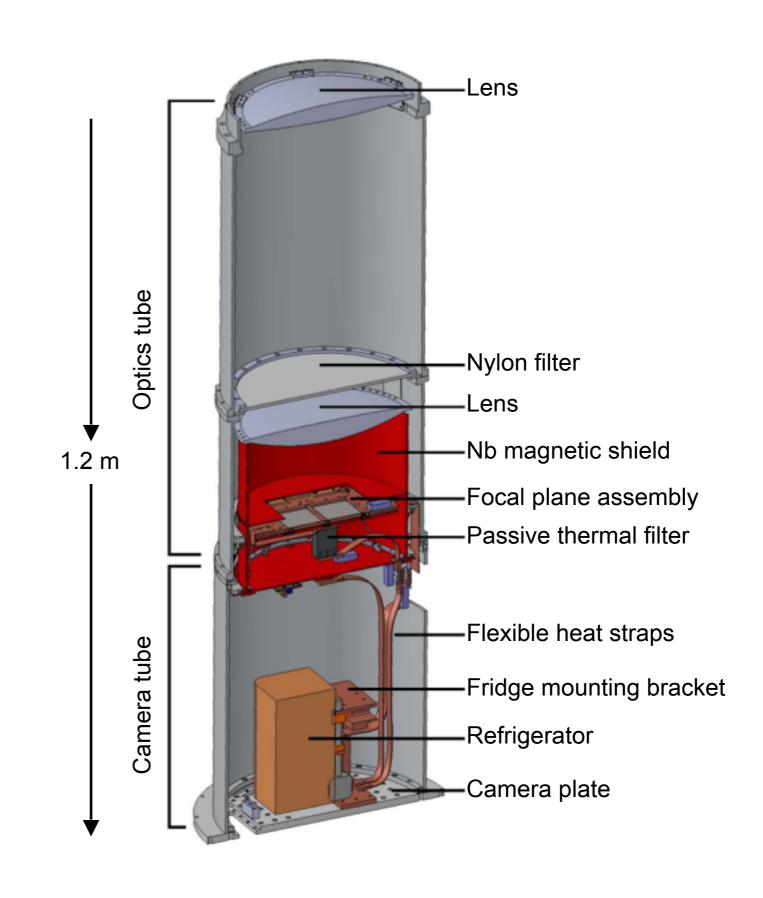
The BICEP2/Keck Telescopes

Telescope as compact as possible while still having the angular resolution to observe degree-scale features.

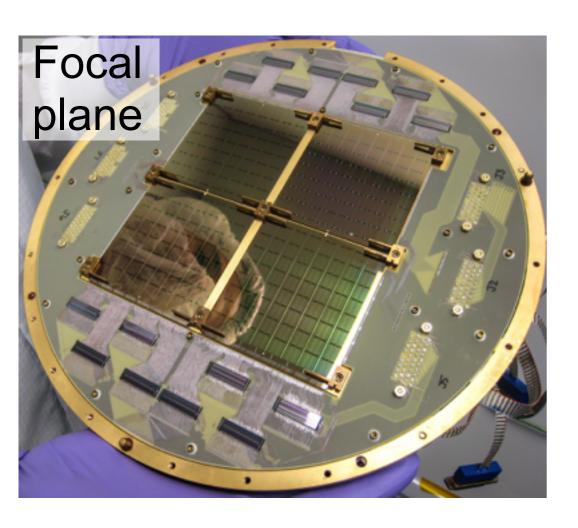
On-axis, refractive optics allow the entire telescope to rotate around boresight for polarization modulation.

Liquid helium cools the optical elements to 4.2 K.

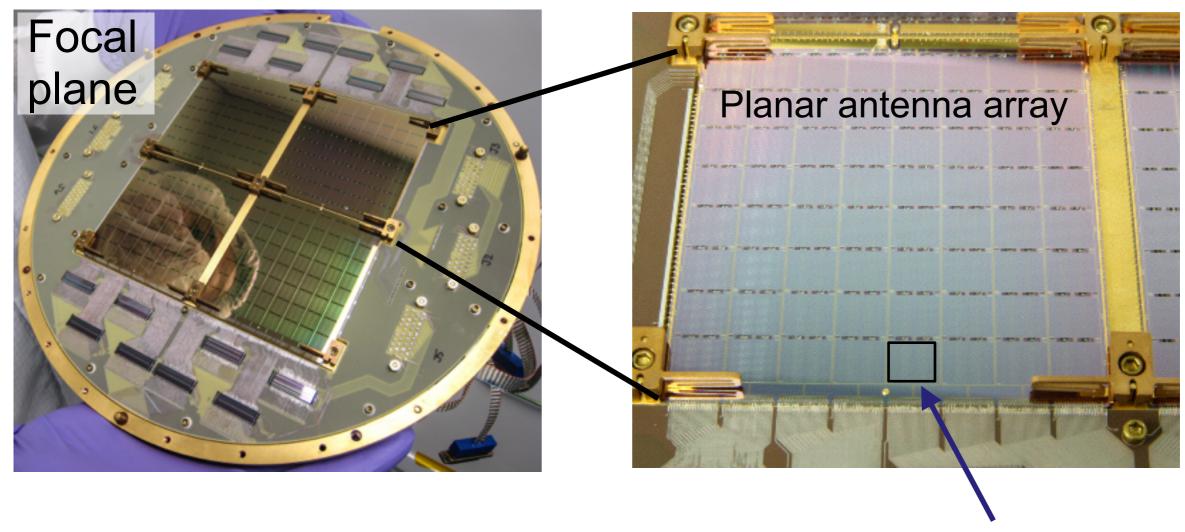
A 3-stage helium sorption refrigerator further cools the detectors to 0.27 K.



Mass-produced Superconducting Detectors

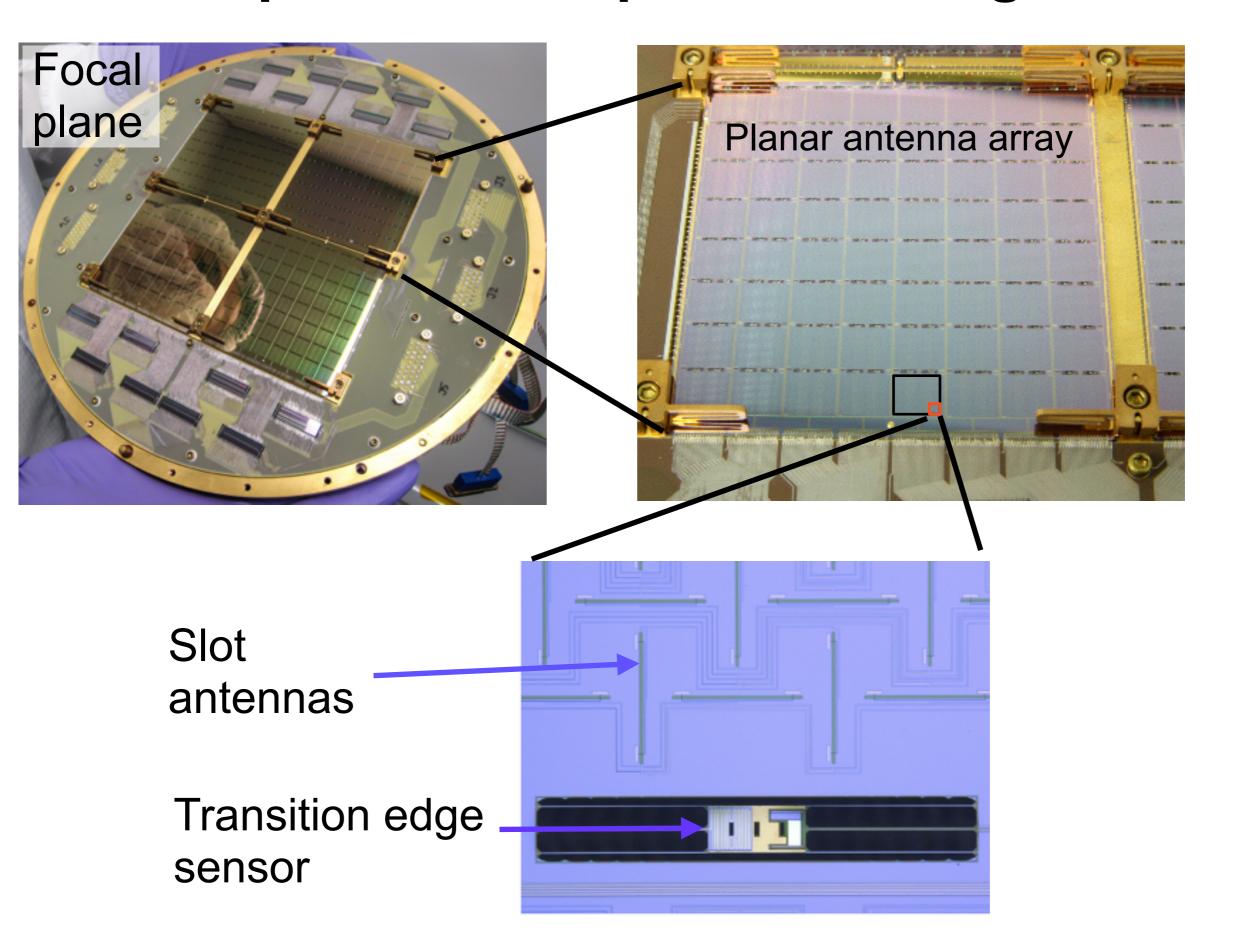


Mass-produced Superconducting Detectors

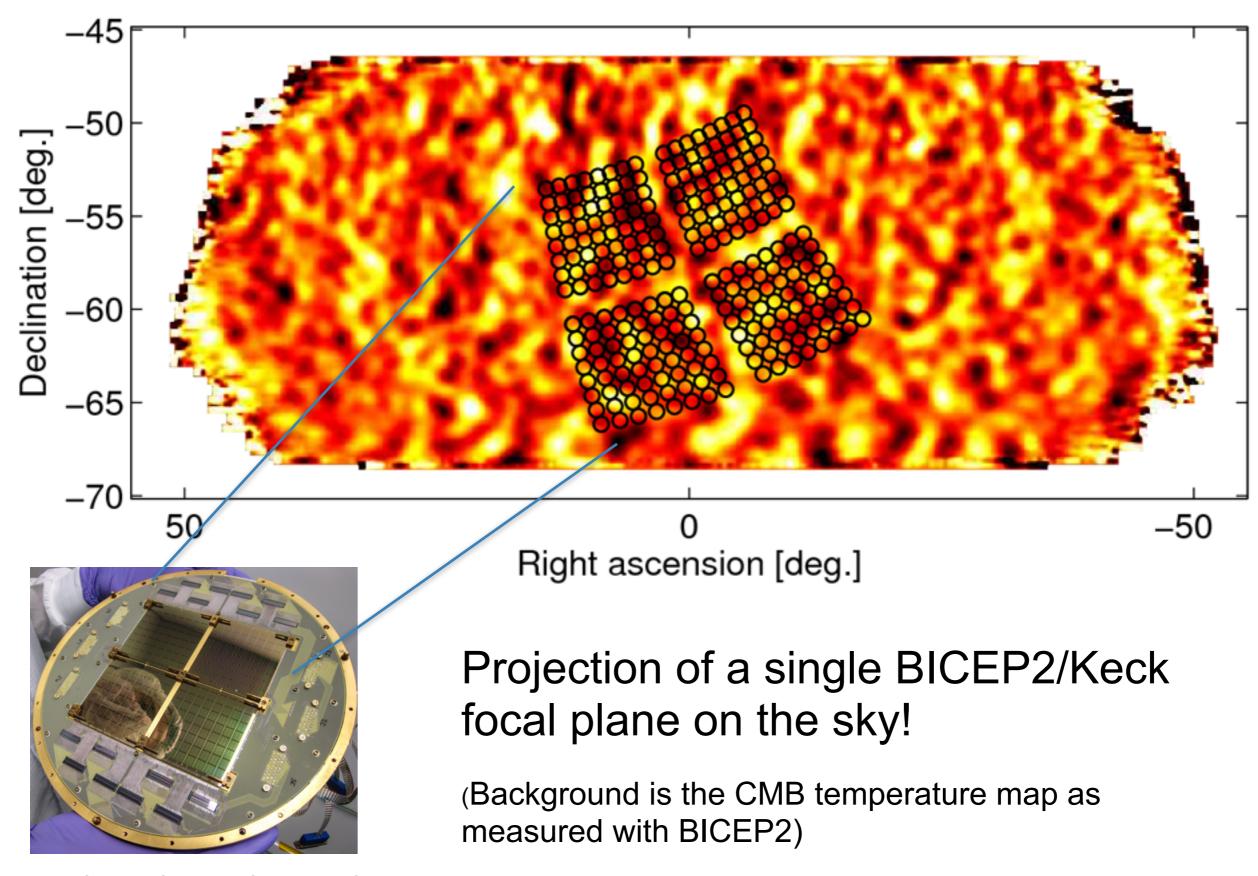


One camera "pixel"

Mass-produced Superconducting Detectors



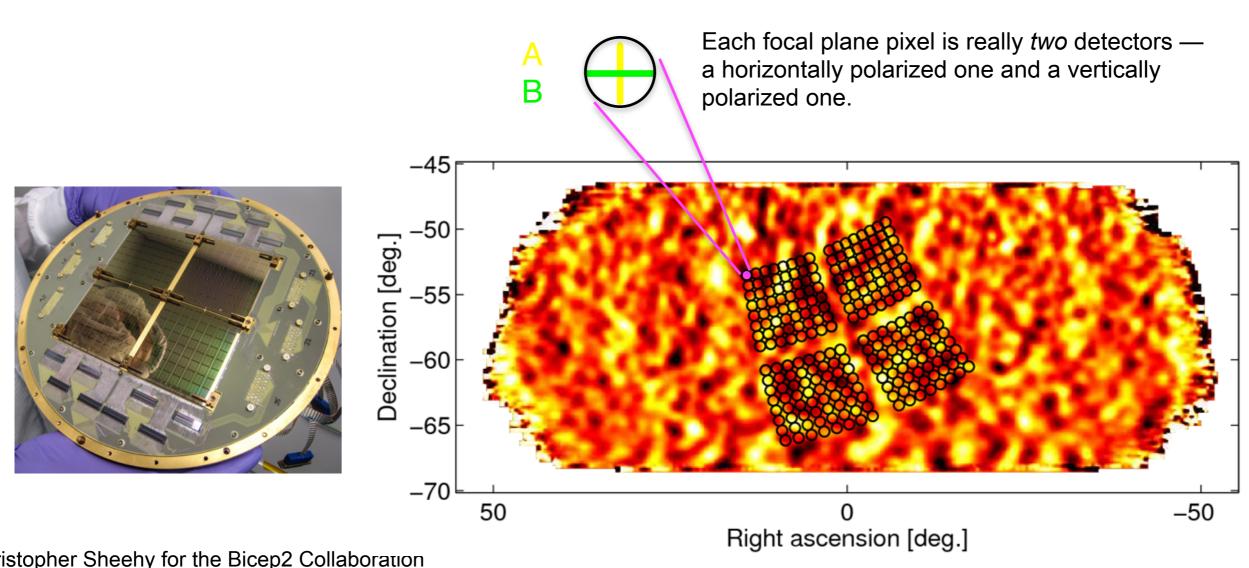
BICEP2 and Keck Array on the Sky



BICEP2 and Keck Array on the Sky

Measure CMB T by summing the signal from orthogonally polarized detector pairs.

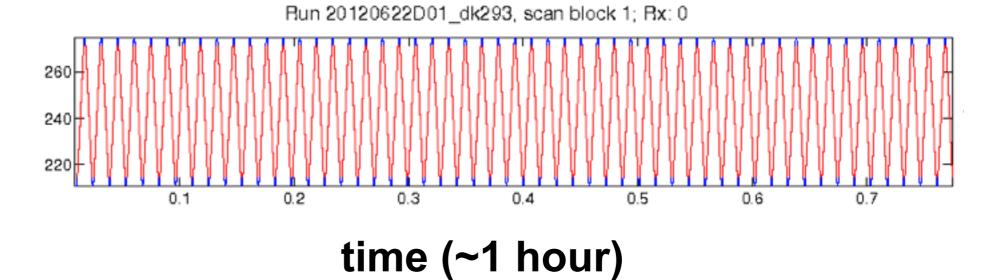
Measure CMB polarization by differencing the signal.



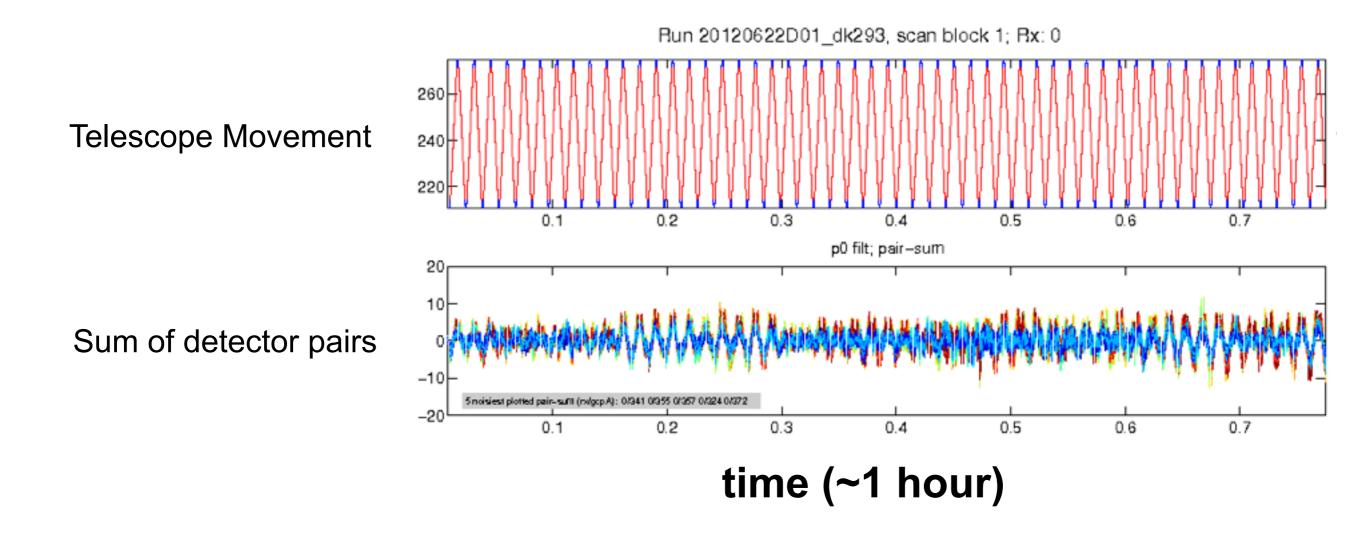


Raw Data

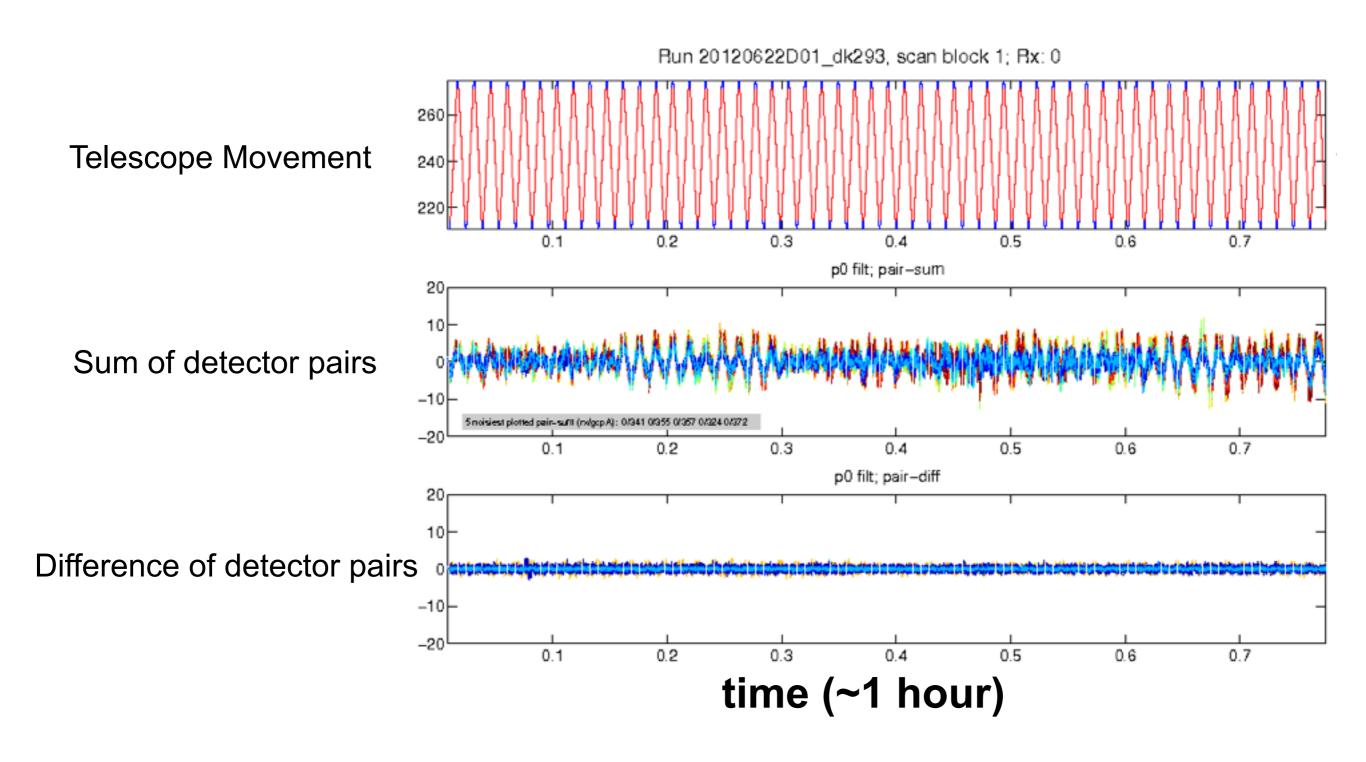
Telescope Movement



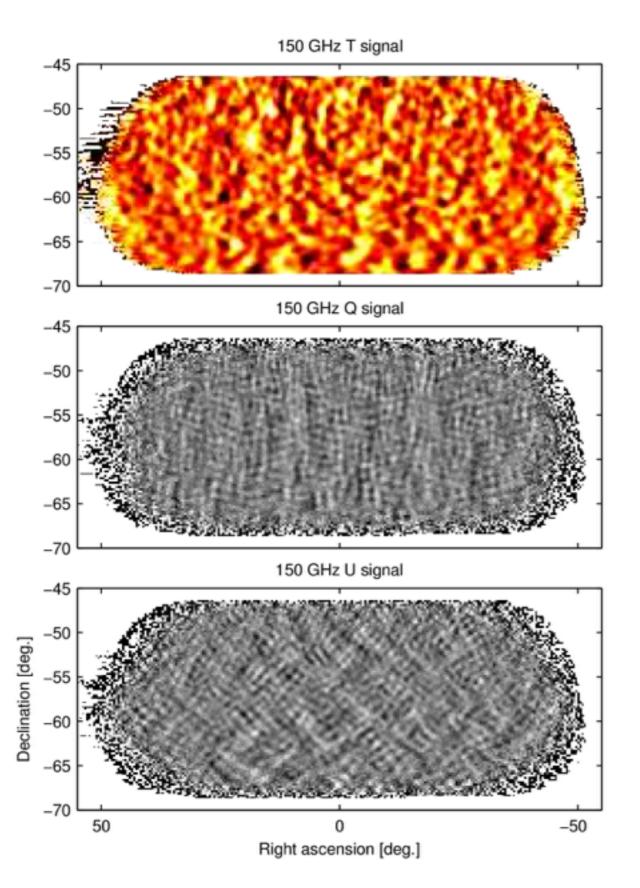
Raw Data



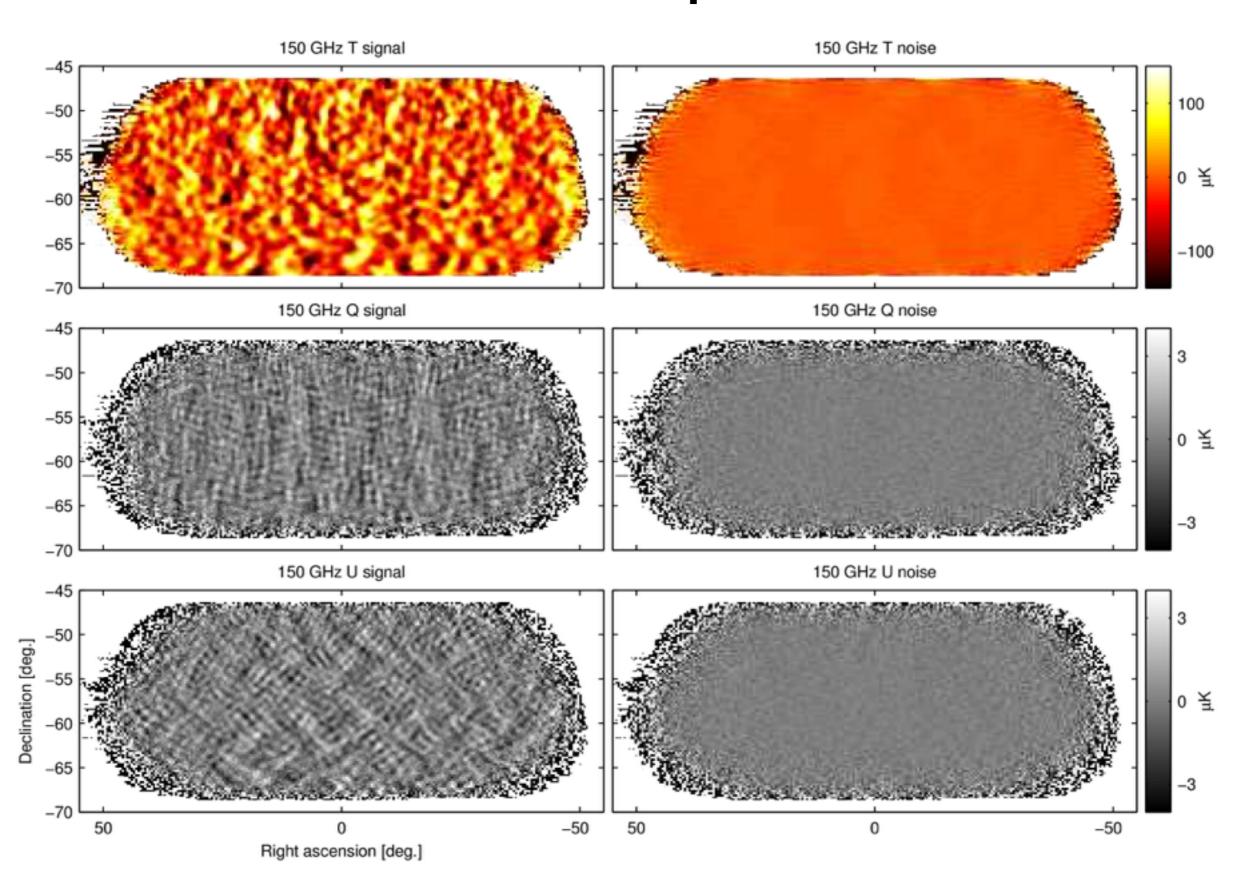
Raw Data



150 GHz maps



150 GHz maps



Let's turn these maps into a power spectrum

Forget about the fact the sky is curved! Just make a map projection and proceed with Fourier transforms.

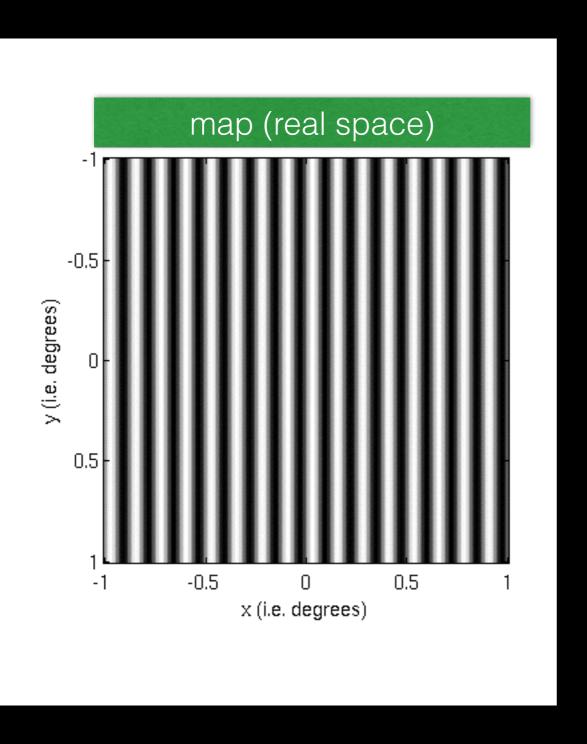
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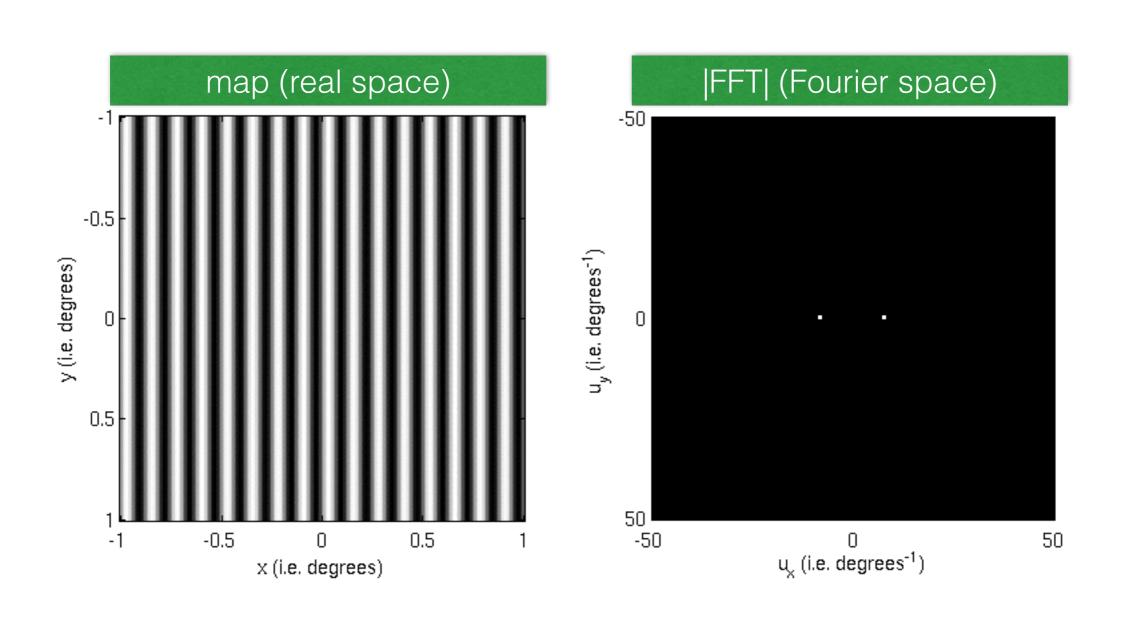
spherical harmonic transform -> Fourier transform Y_{lm} 's -> sines and cosines a_{lm} 's -> Fourier coefficients

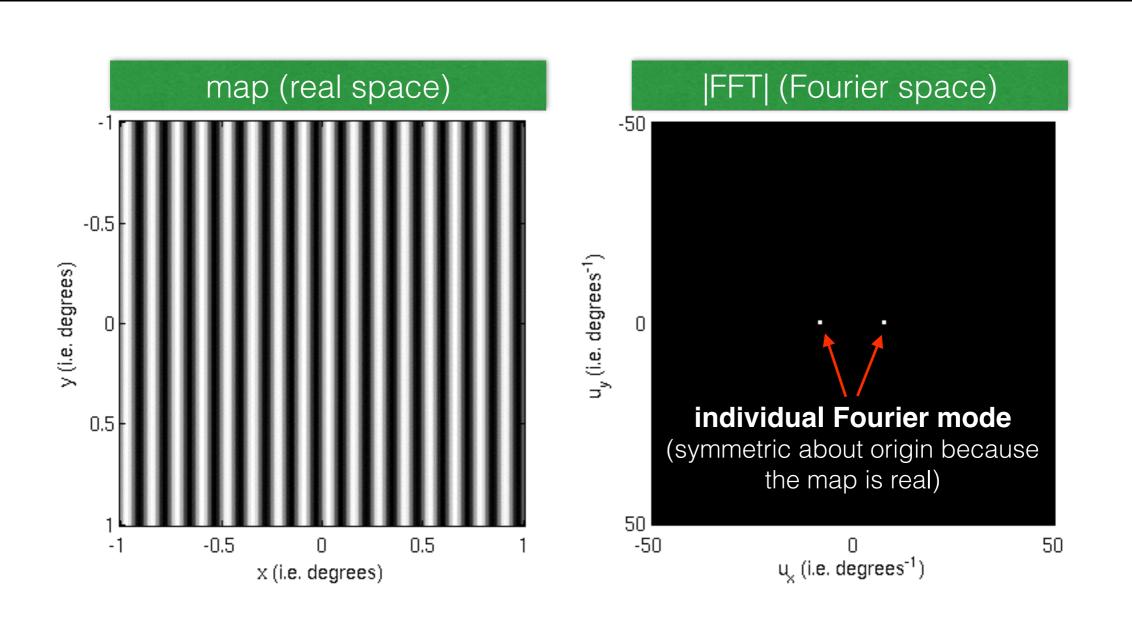
Conceptually, Fourier analysis gives us all the intuition we need about the analysis of "full sky", spherical maps.

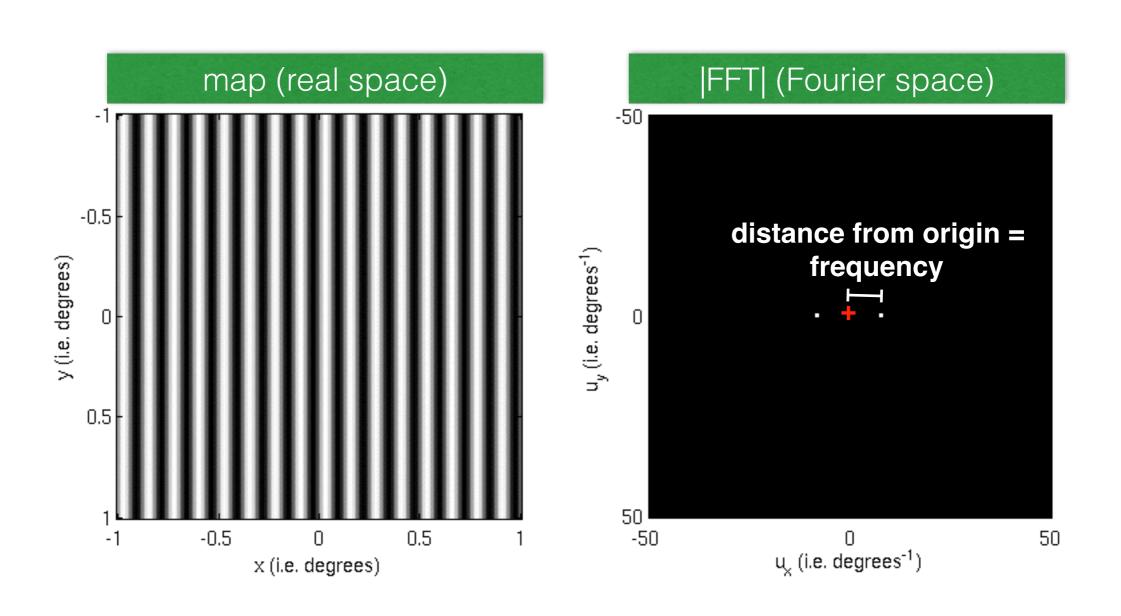
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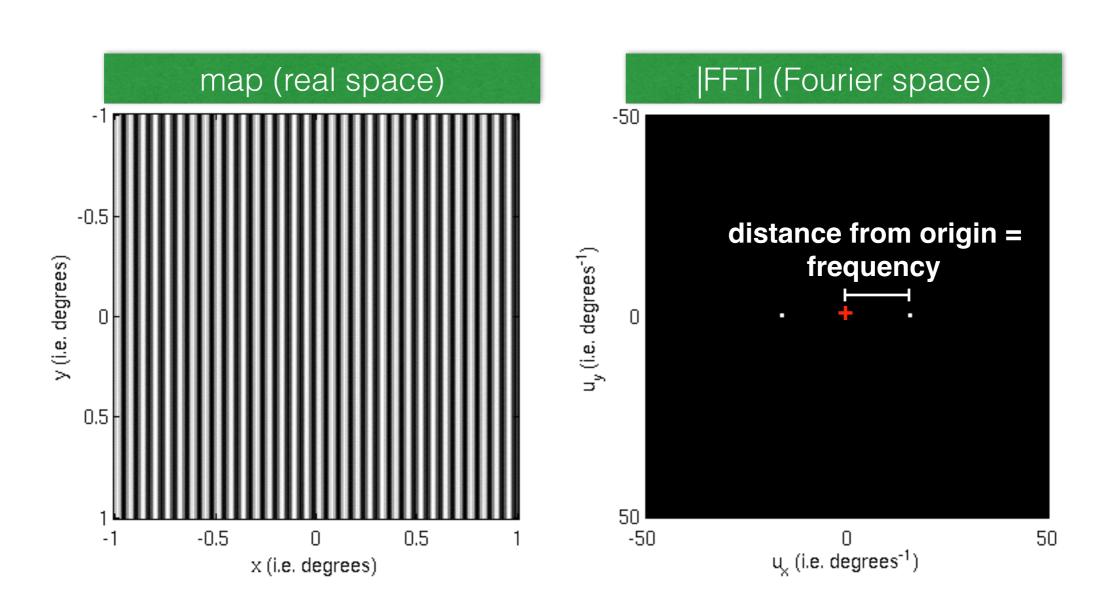
In fact, many experiments that do not do make maps of the full sky do Fourier analysis and never compute a spherical harmonic transform.

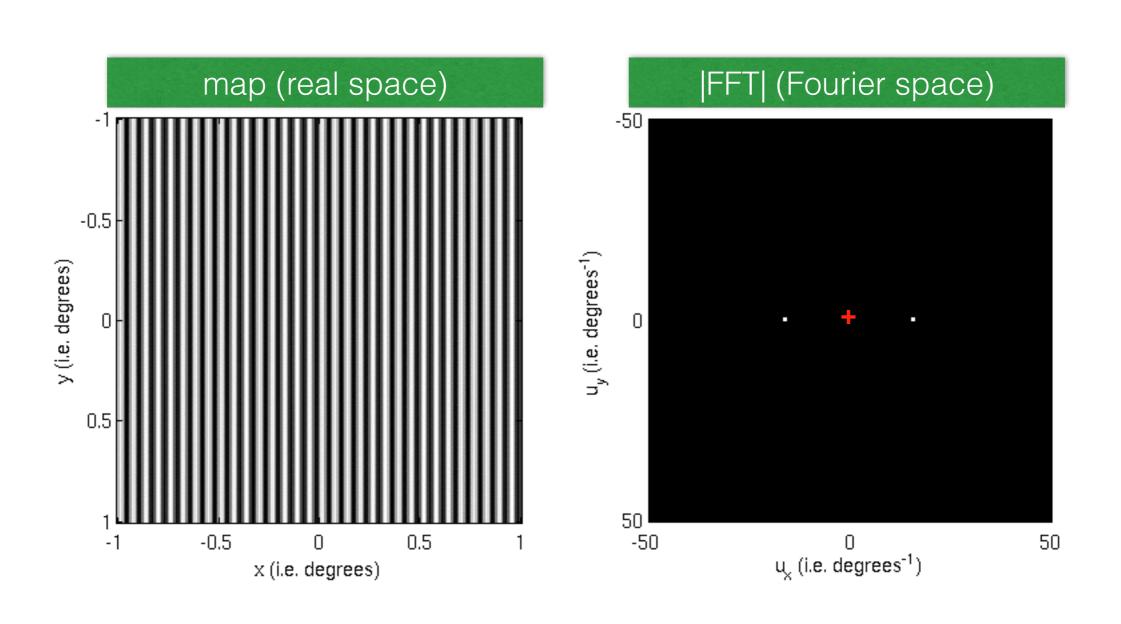


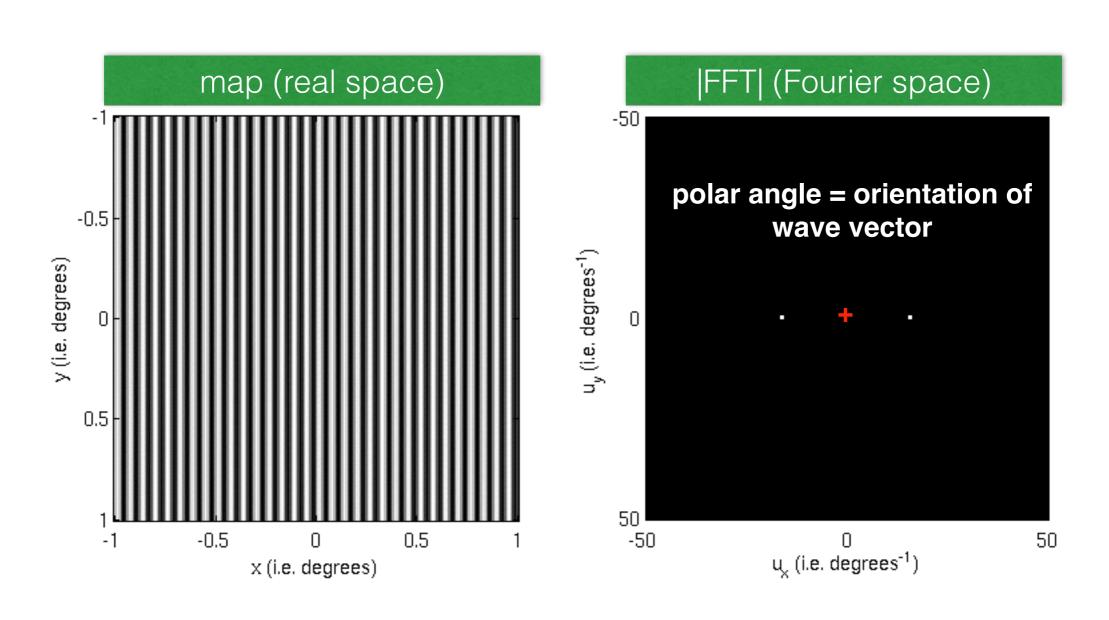


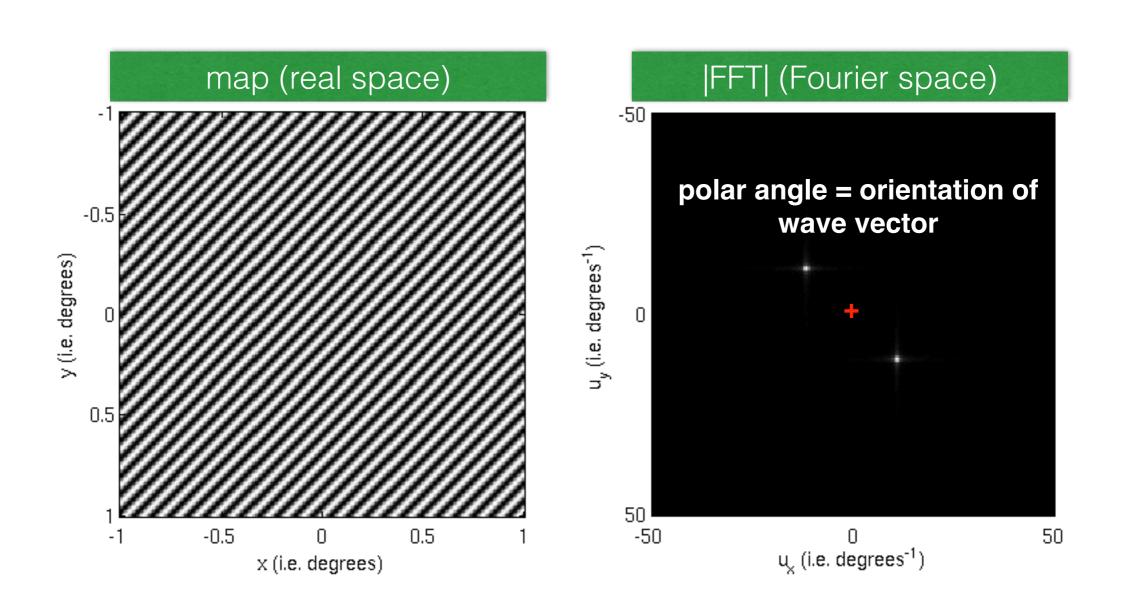


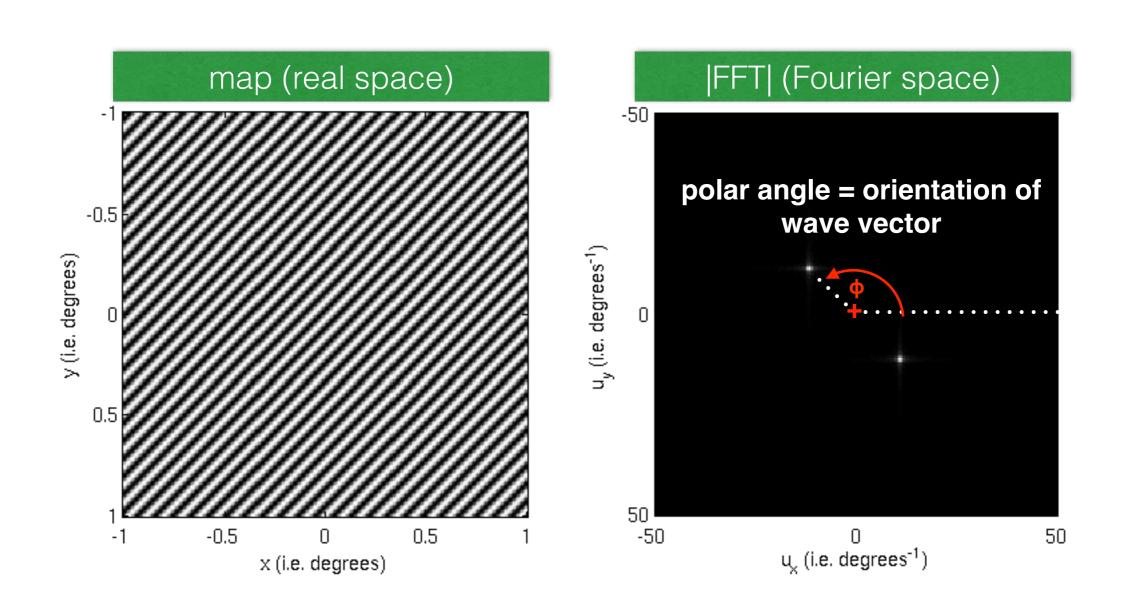


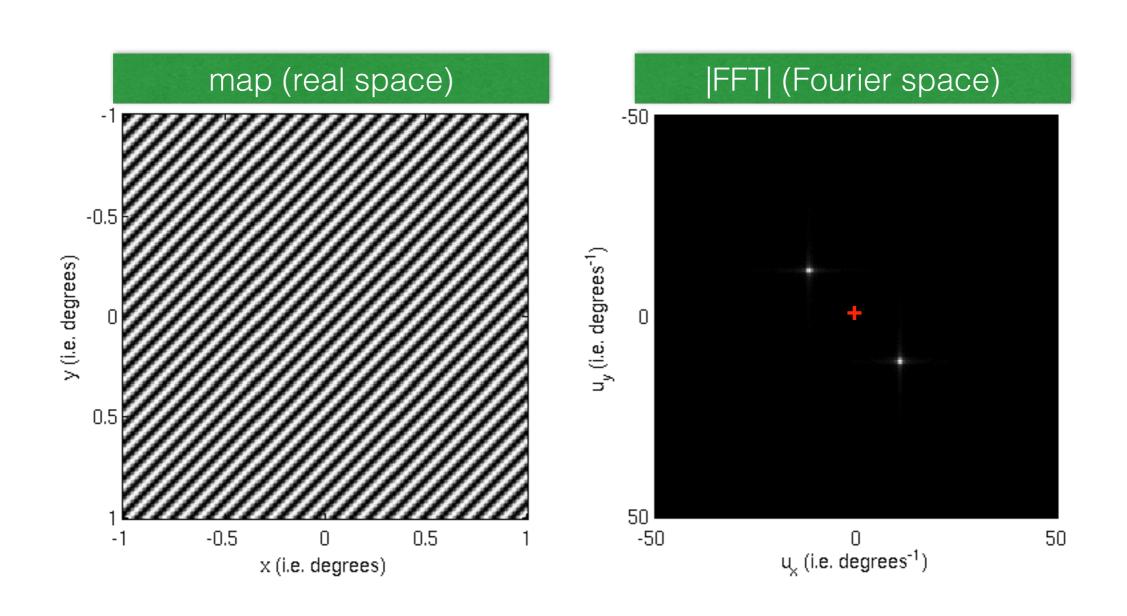


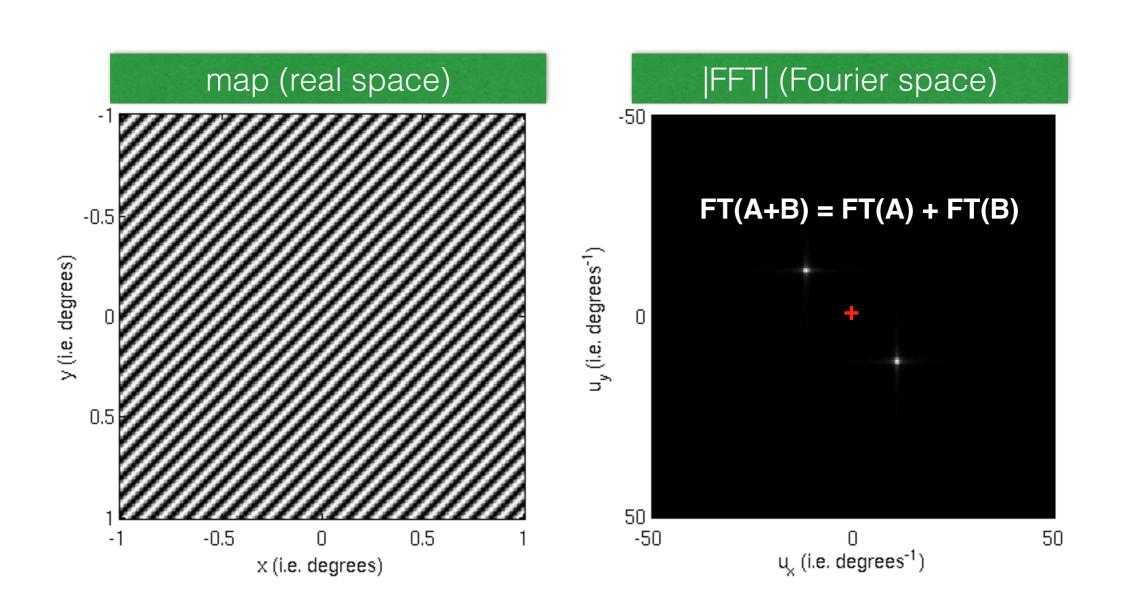


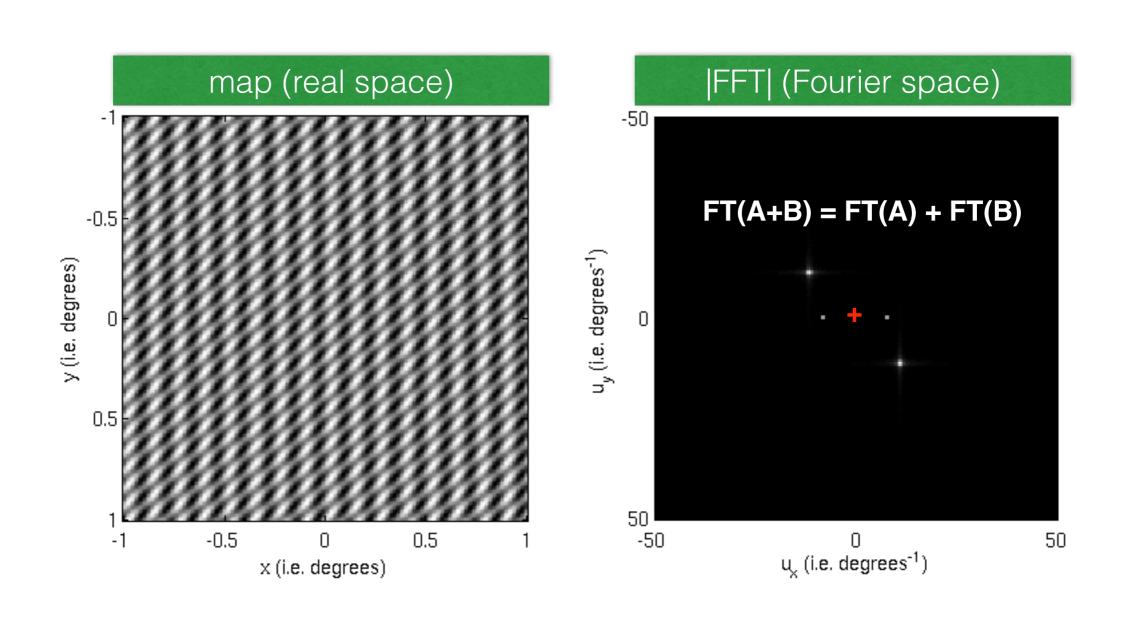


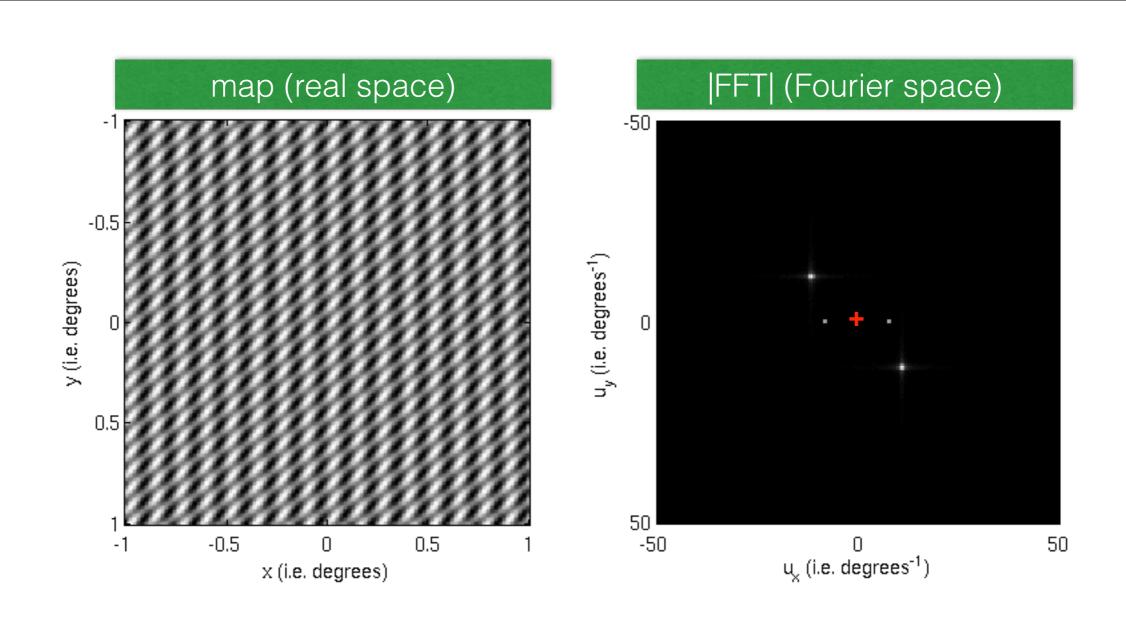


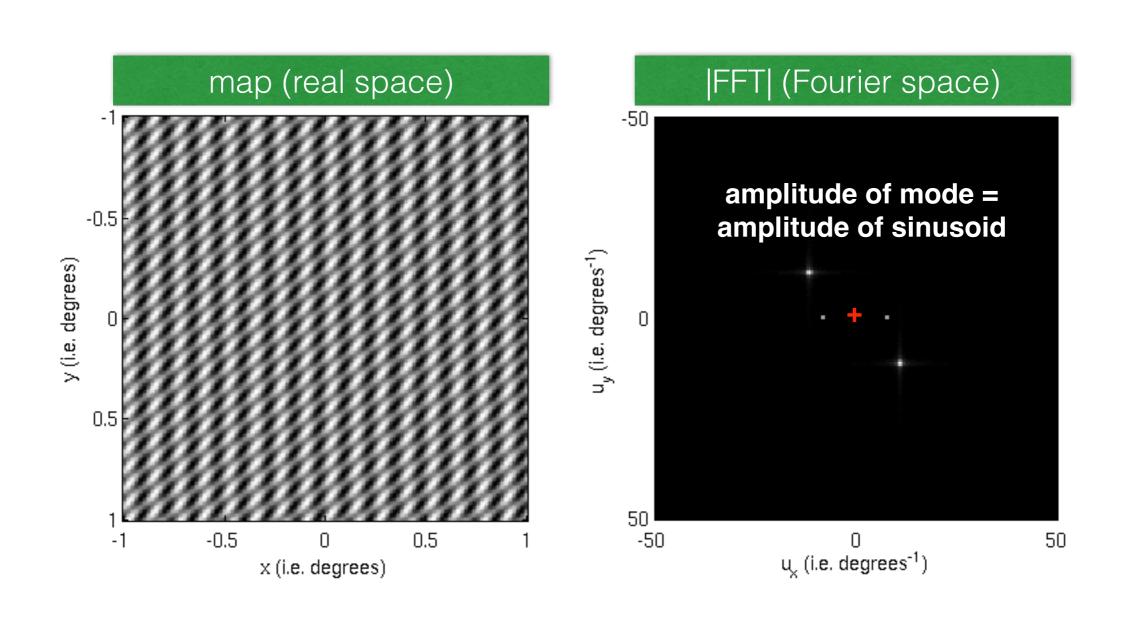




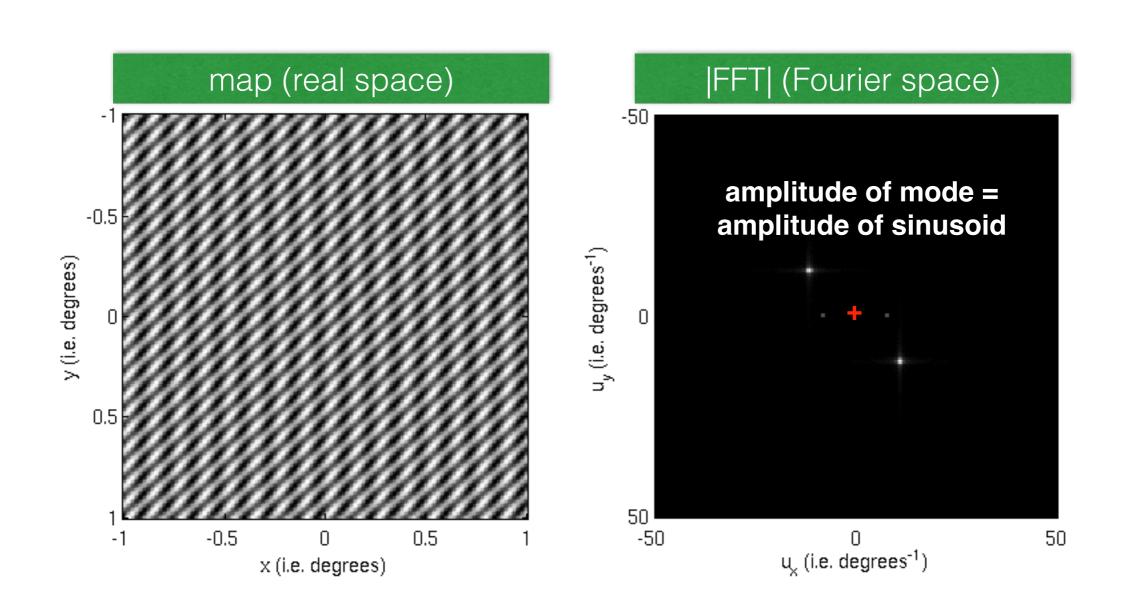




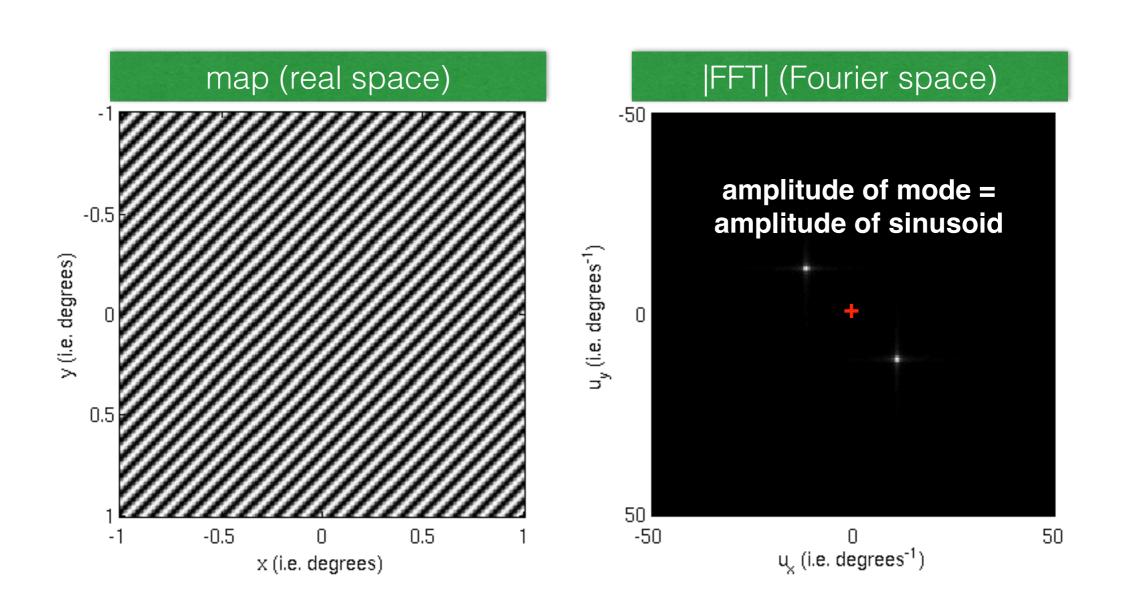




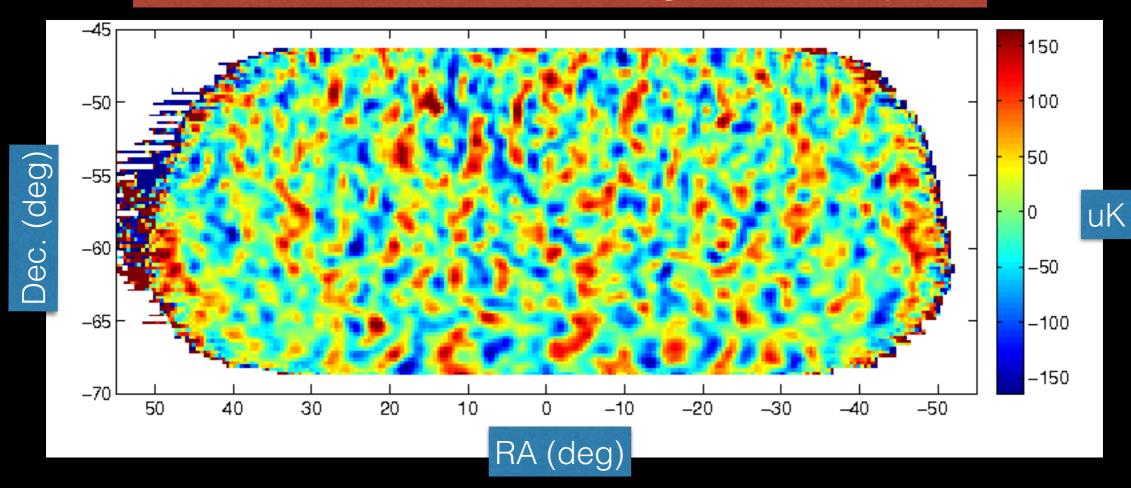
Flat sky approximation



Flat sky approximation

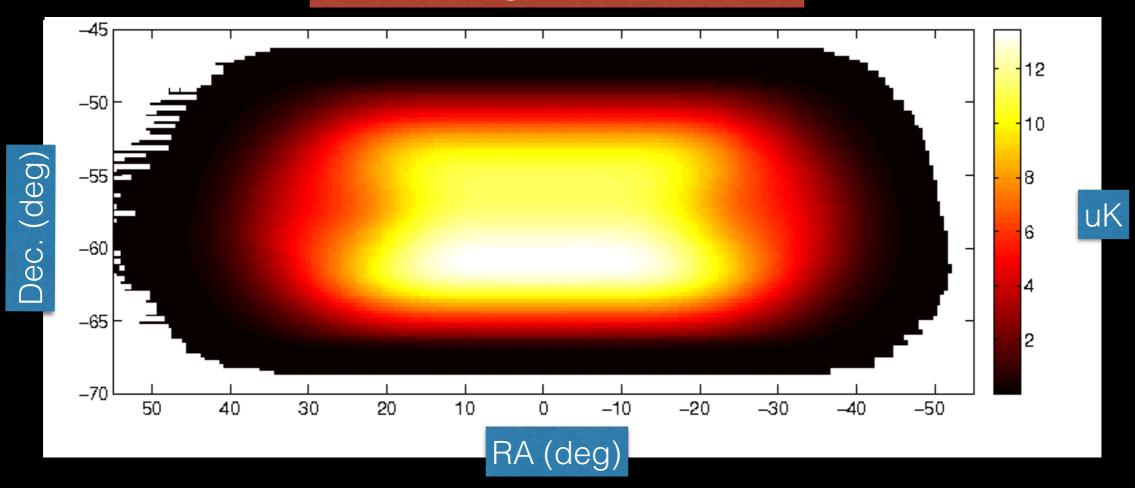


Cosmic Microwave Background map (T)

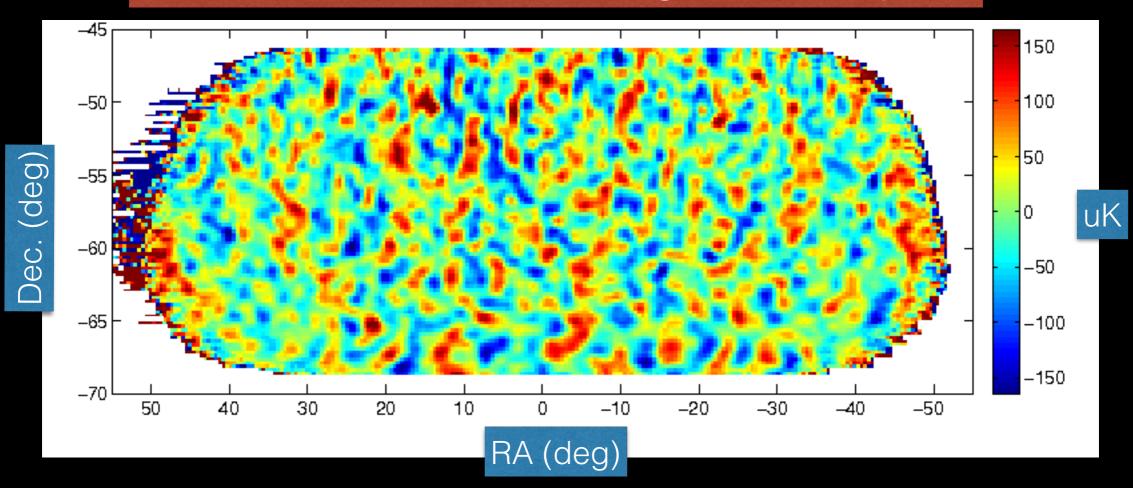


(thanks to the WMAP satellite, the CMB is often displayed with this colormap)

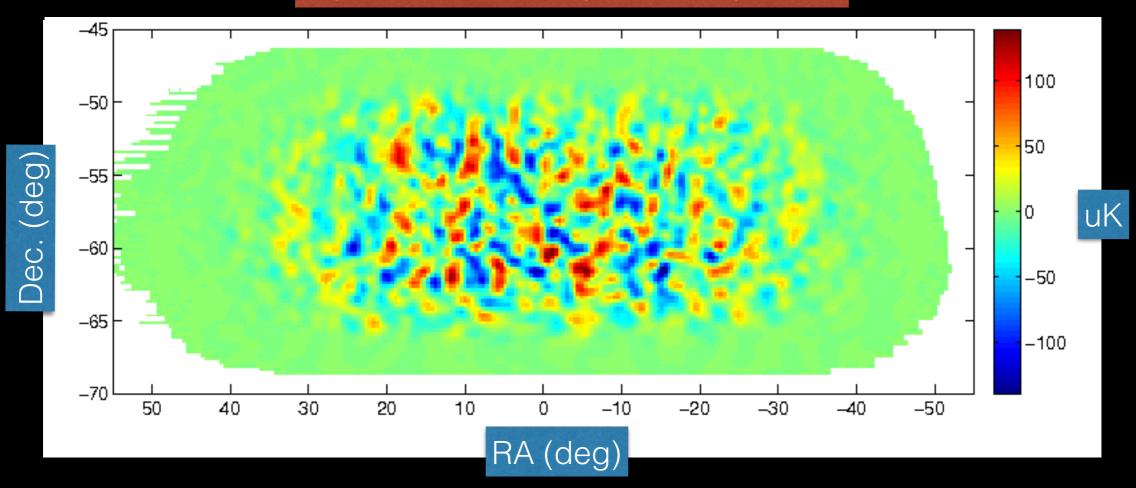
Pixel weight map $(1/\sigma)^2$

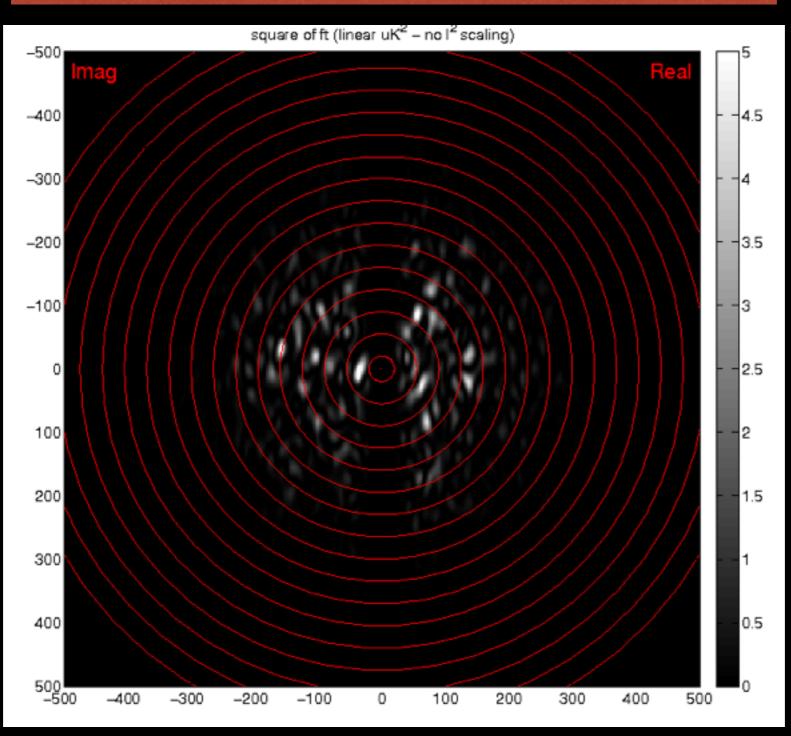


Cosmic Microwave Background map (T)

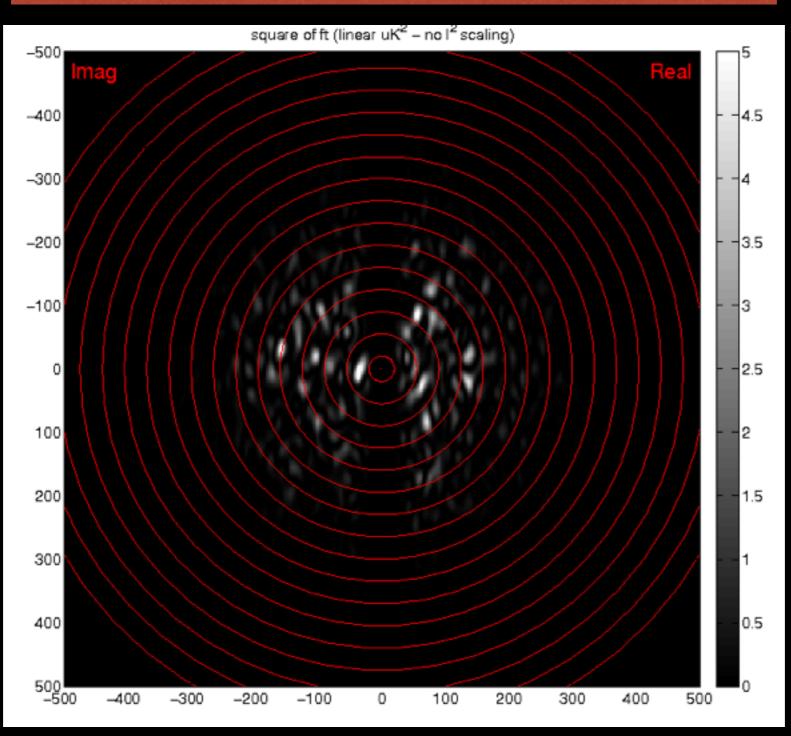


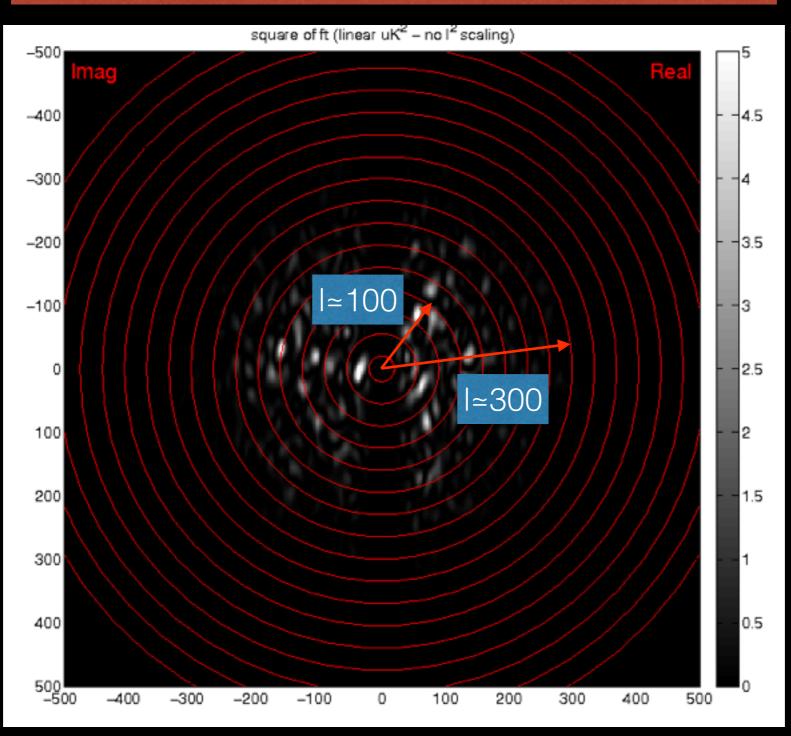
Apodized map = map / σ^2



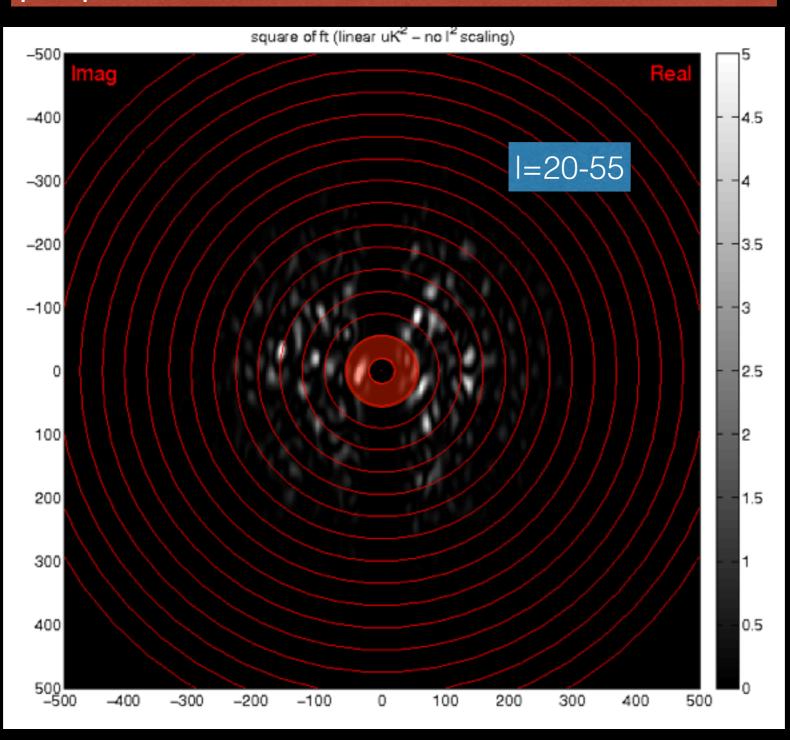


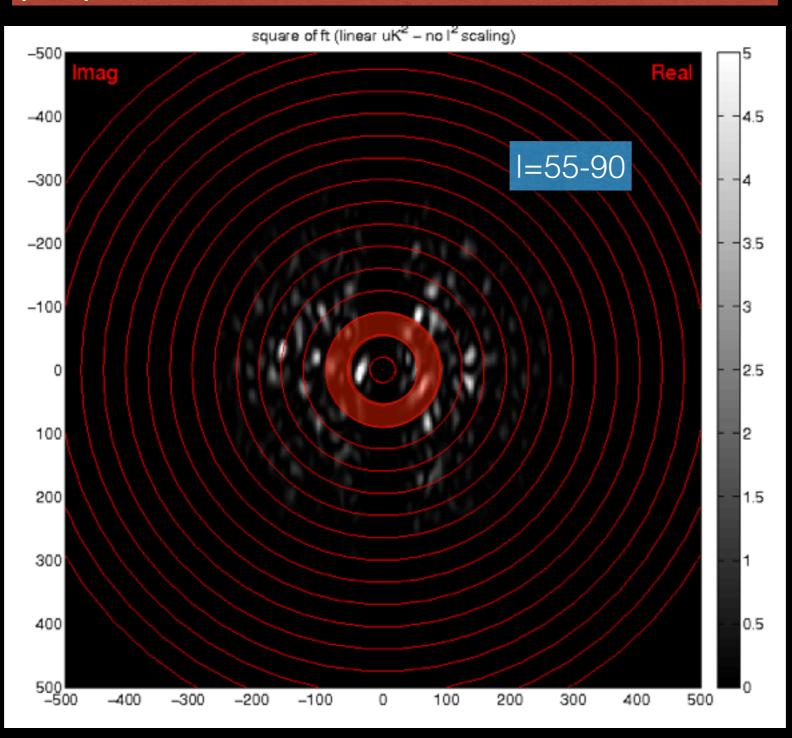
- coordinate units of map are degrees
- coordinate units of 2d Fourier plane are degrees-1
- convert 2d Fourier plane coordinates to radians⁻¹
- multipole $I = 2\pi^* \text{radians}^{-1}$

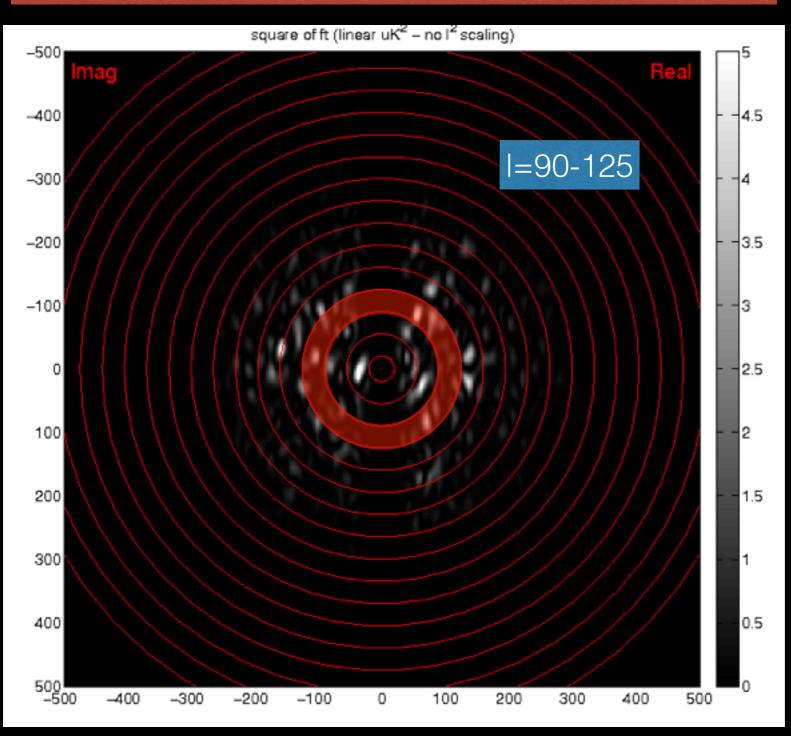


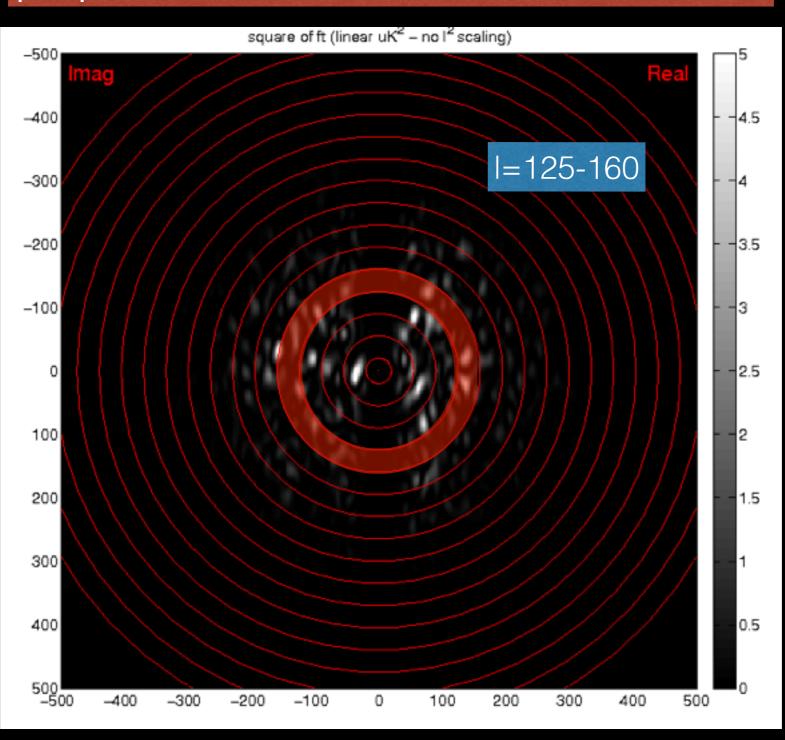


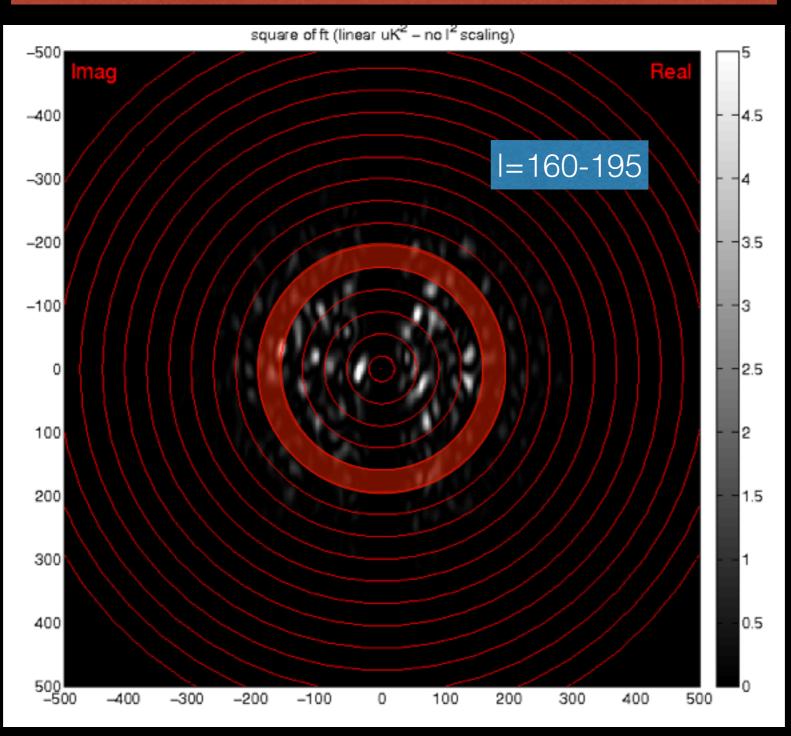
Average the signal in annular bins to make "bandpowers"





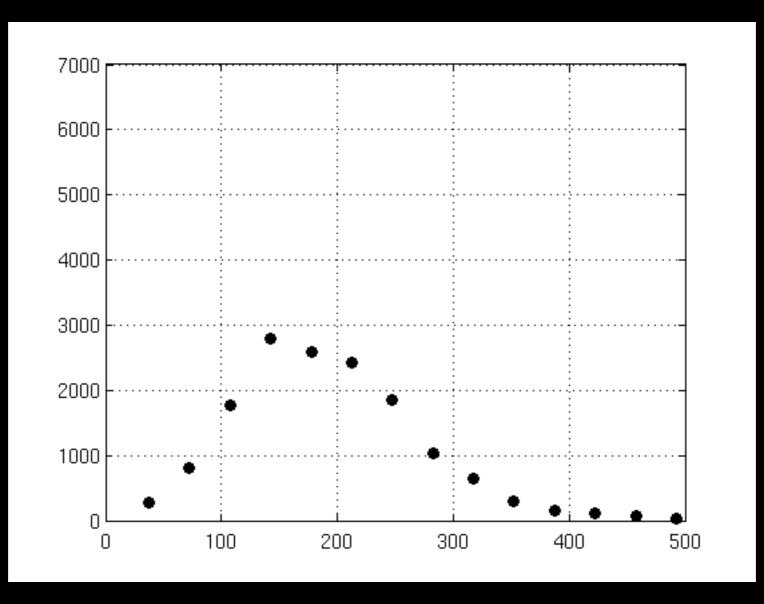






This gets us a power spectrum — just data points without error bars.

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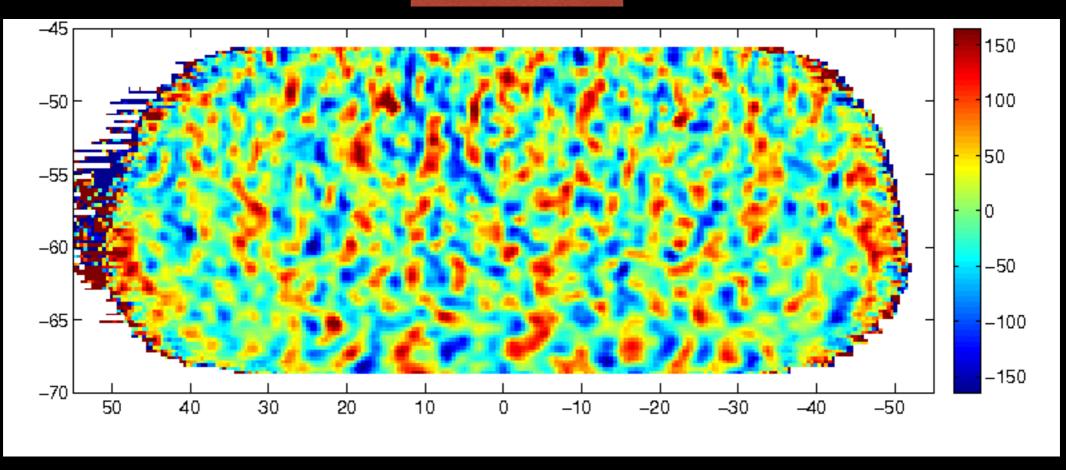


multipole I

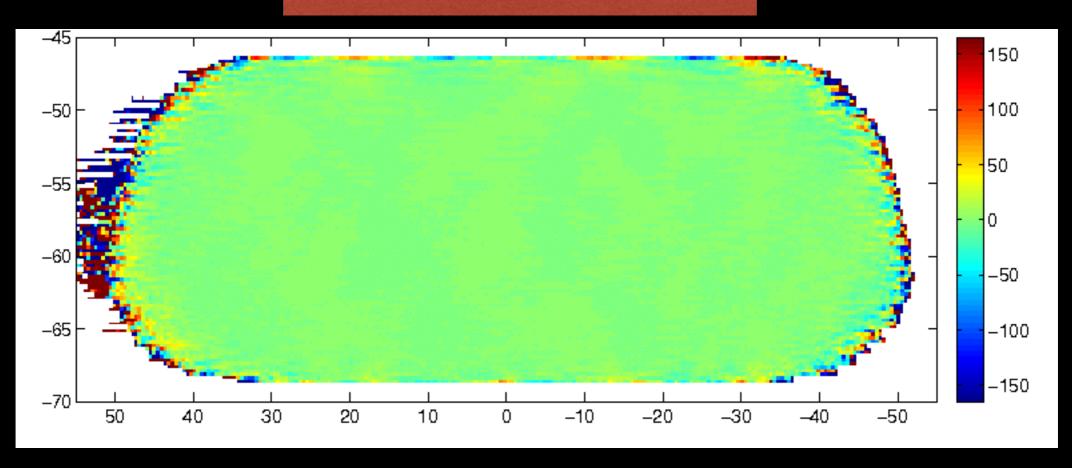
Now we need to assign error bars.

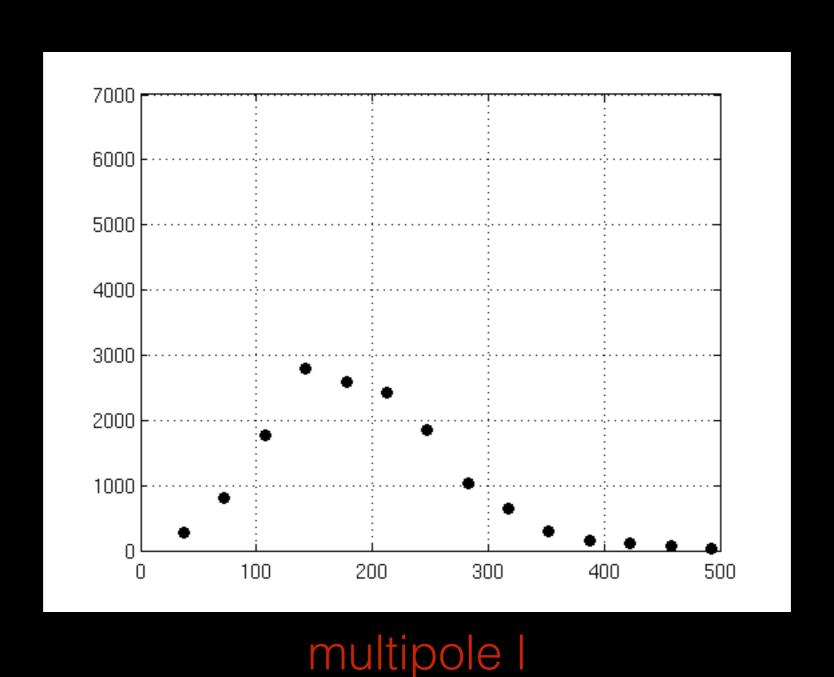
 One simple way to estimate noise is to make a map from one half of the data set, make a map from the second half, and difference them. Signal goes away but resulting map has same noise properties as the real map.

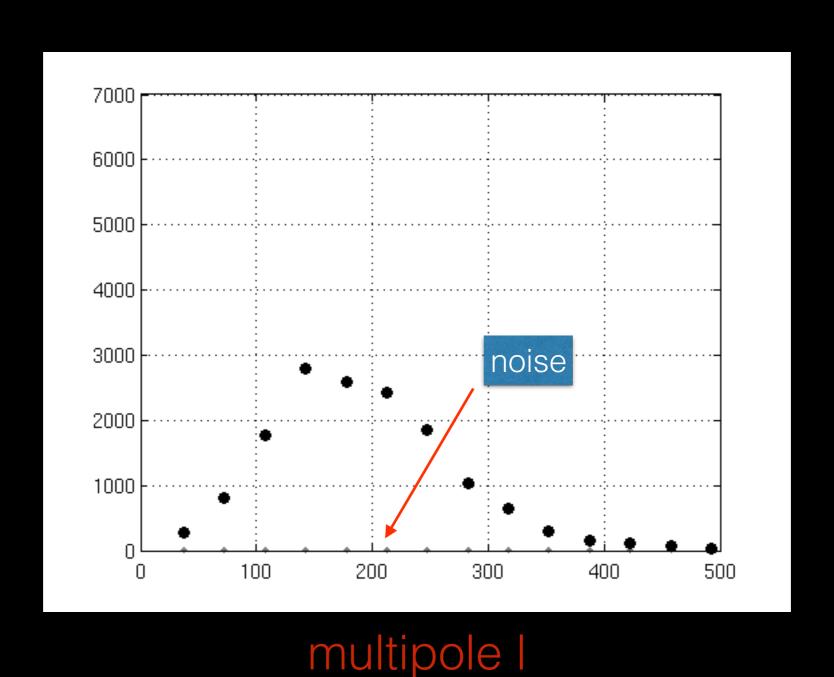
Real map



Noise realization 0001

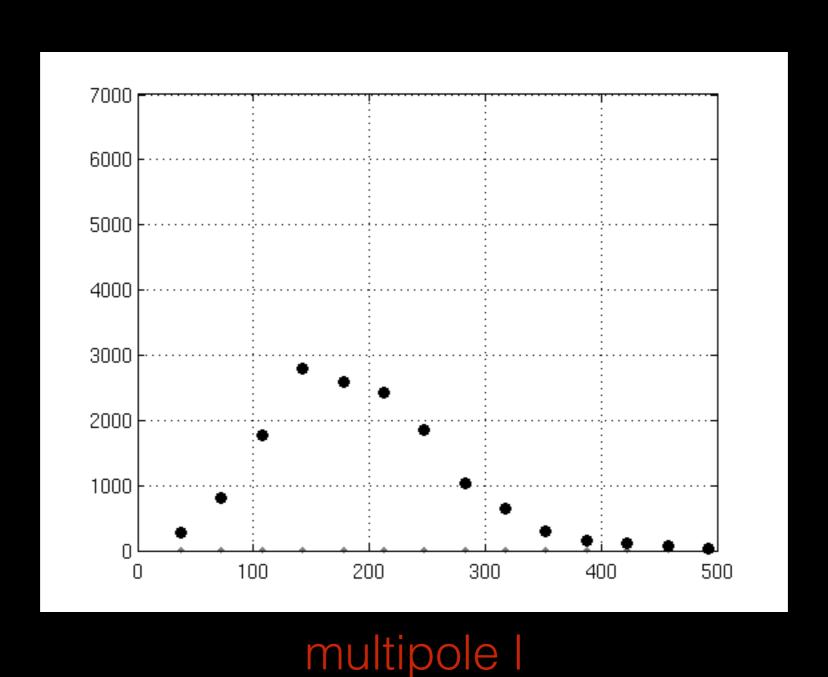


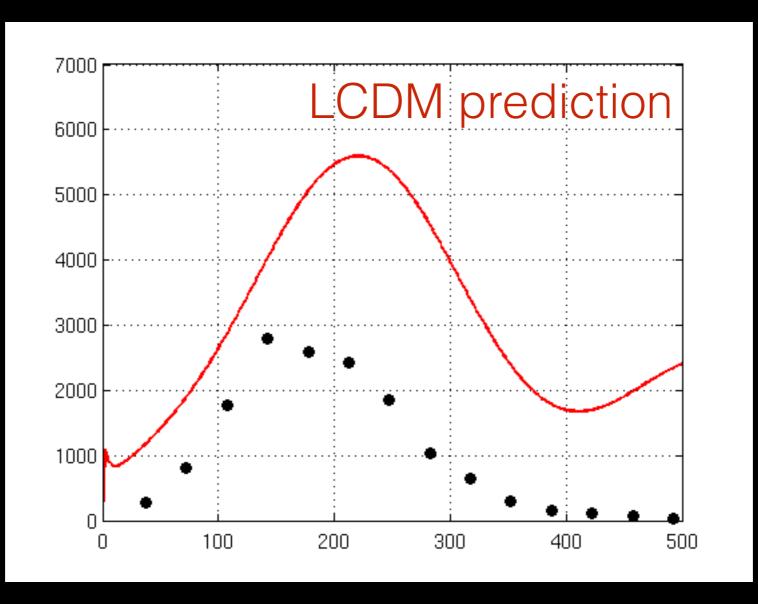




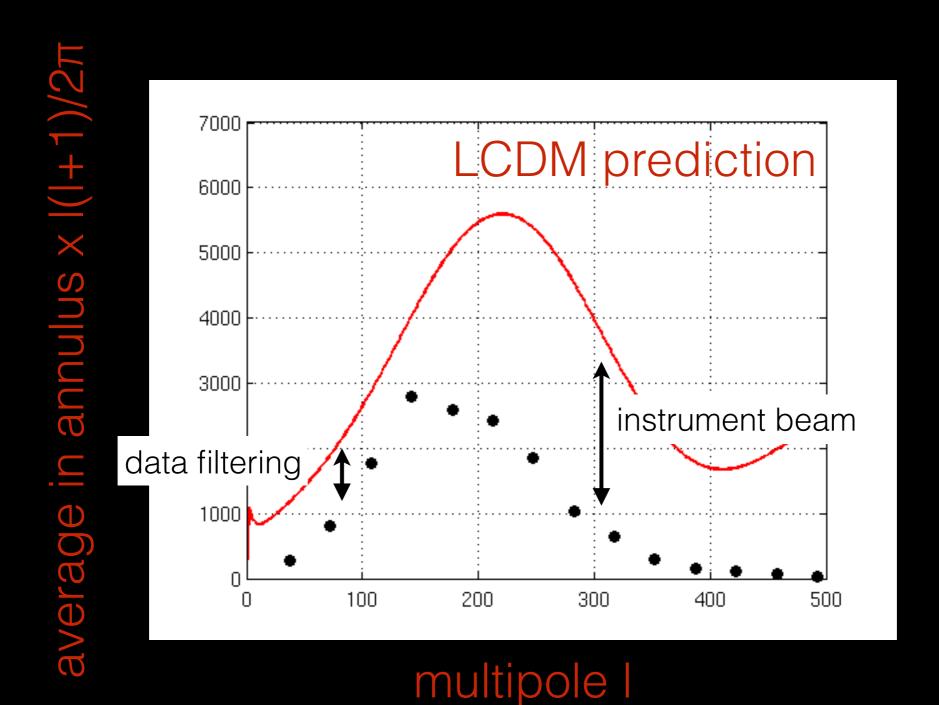
This is a ridiculously significant detection of power.

Let's just assume for the moment it's not instrumental systematics. We need to compare to models. Let's call every cosmologist's favorite model "LCDM"





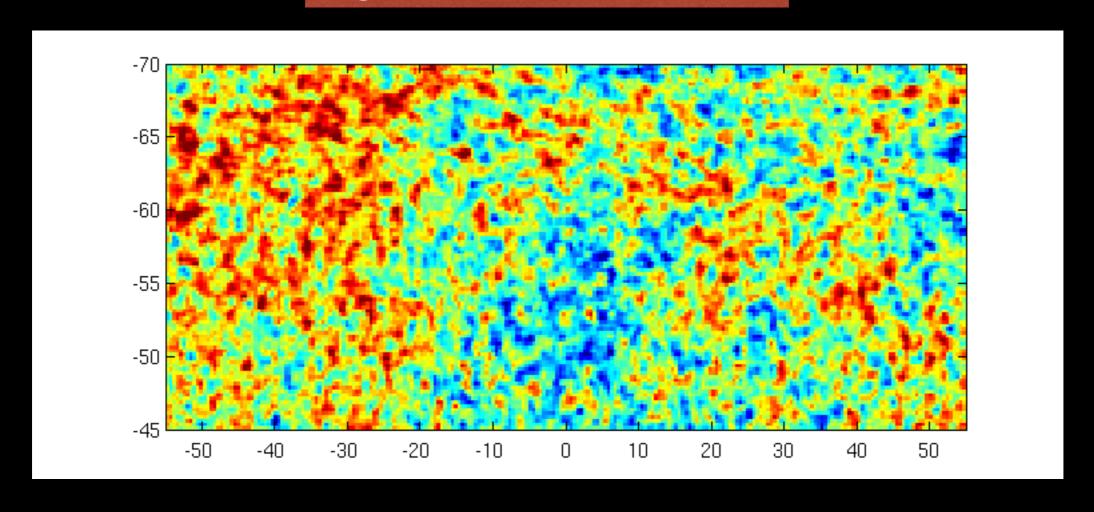
multipole I



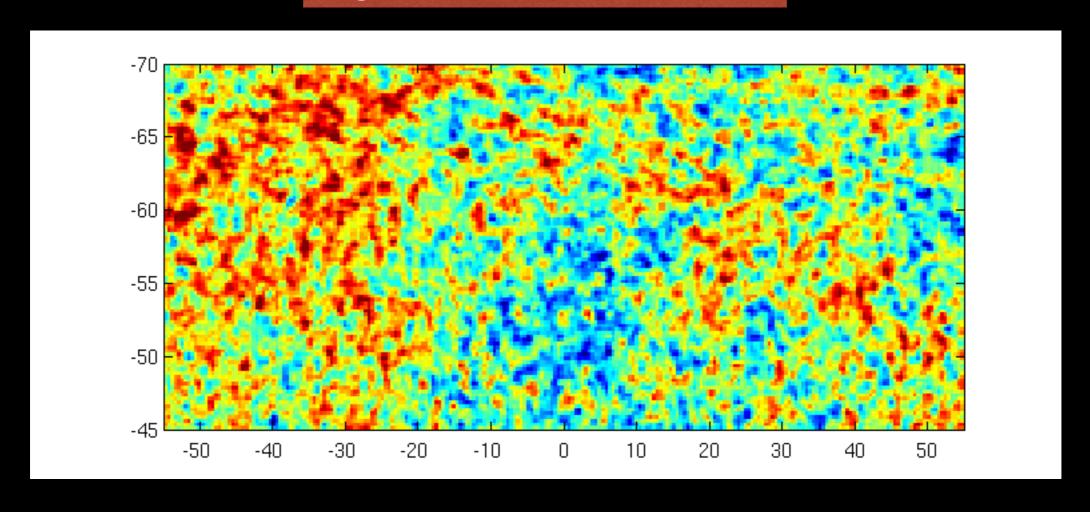
We must model the effect of the instrument.

One way to do this is to create noiseless simulated input realizations and pass it them through the same data reduction pipeline that the real data uses.

Signal realization 0001

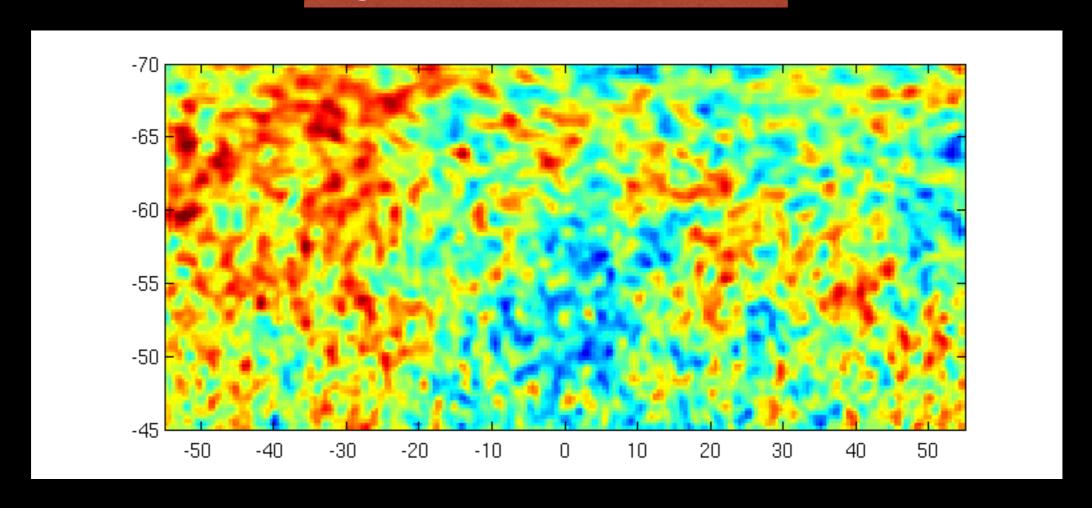


Signal realization 0001



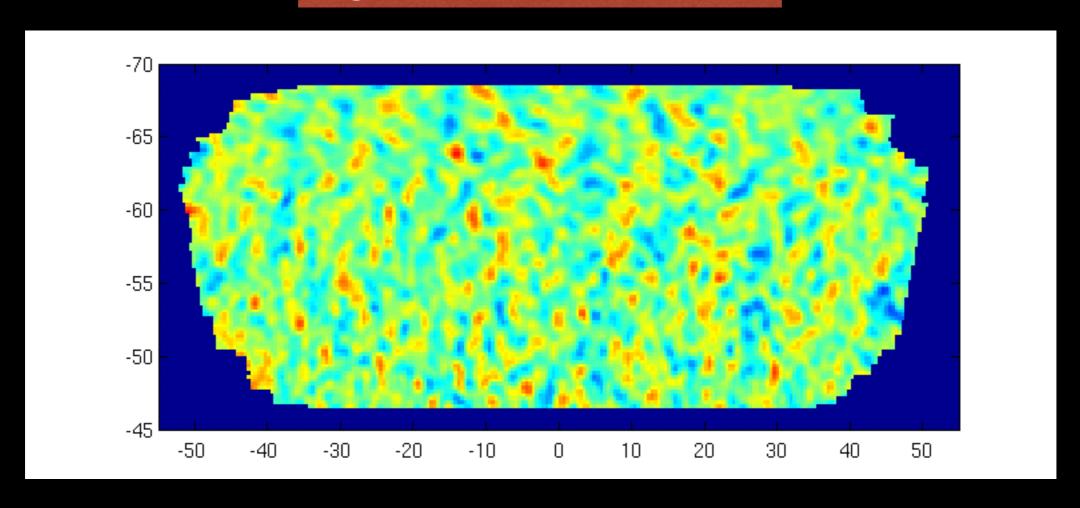
Generate random Gaussian numbers whose underlying power spectrum matches the fiducial theory spectrum.

Signal realization 0001

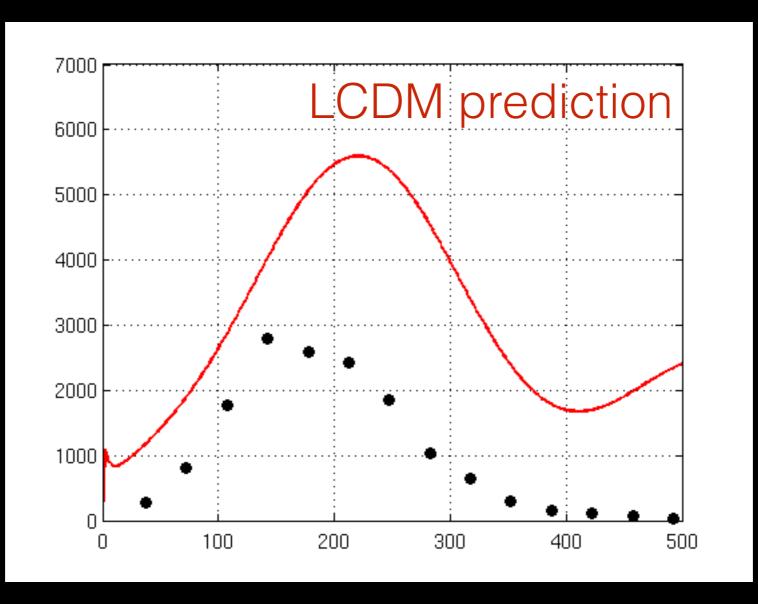


Now convolve the input map with by the instrument's angular response pattern (i.e. "beam" or "point spread function")

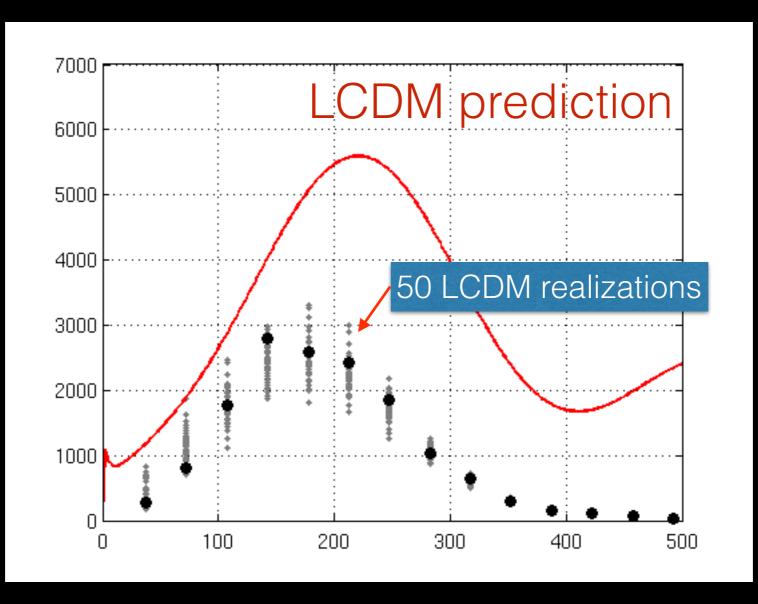
Signal realization 0001



Now pass through the same data reduction pipeline as the real data. This imposes the same filtering on the simulation as on the data.



multipole I

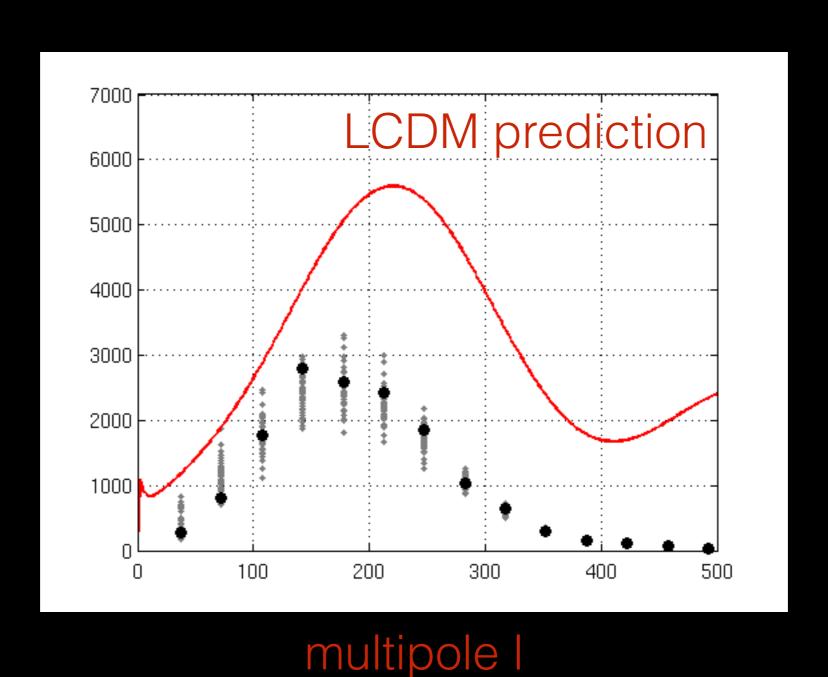


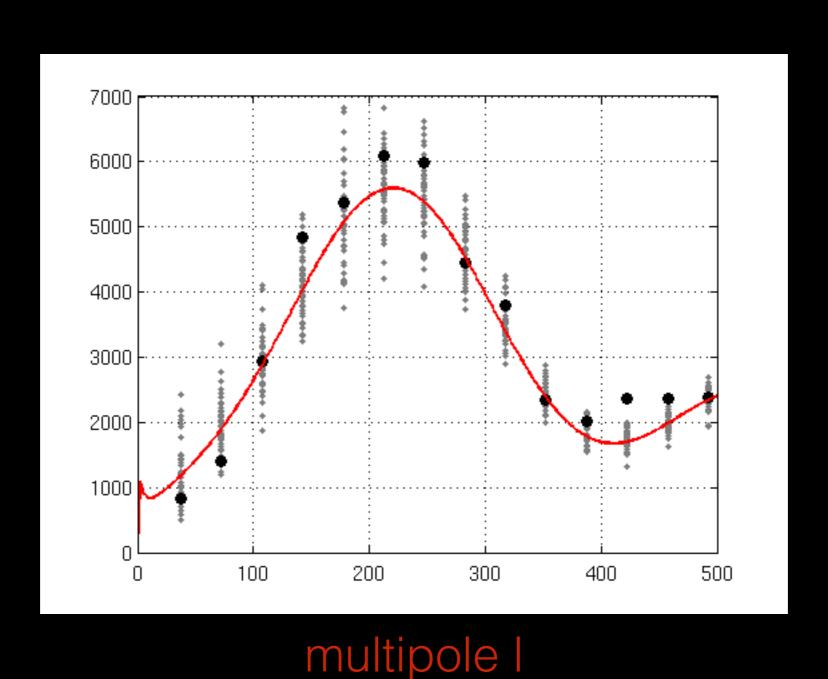
multipole I

The spread in the simulations is so-called "cosmic variance", which enters the Monte Carlo analysis as different random realizations for the original input map.

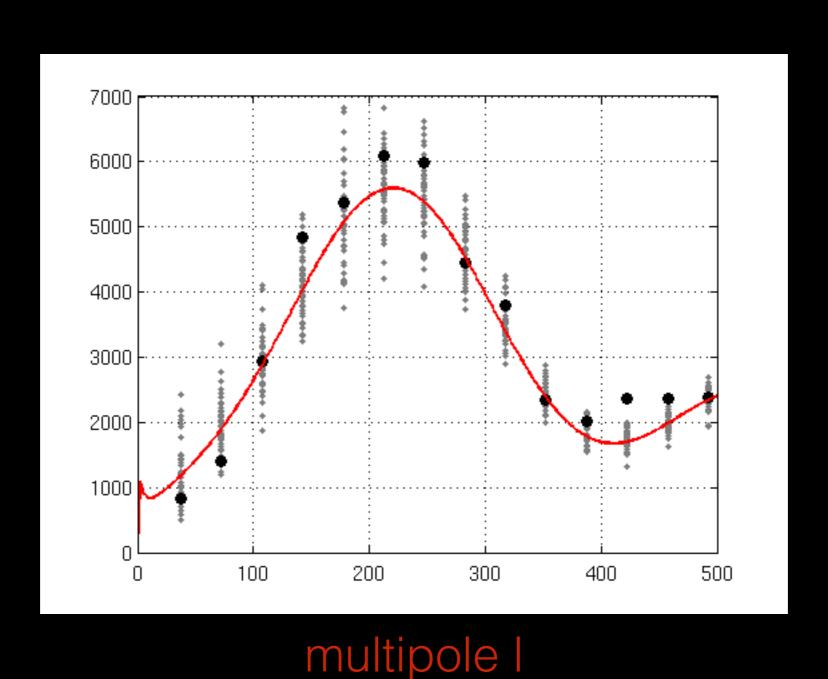
Remove the mean effect of power suppression by dividing both the real data and the simulations by the mean of the signal simulations.

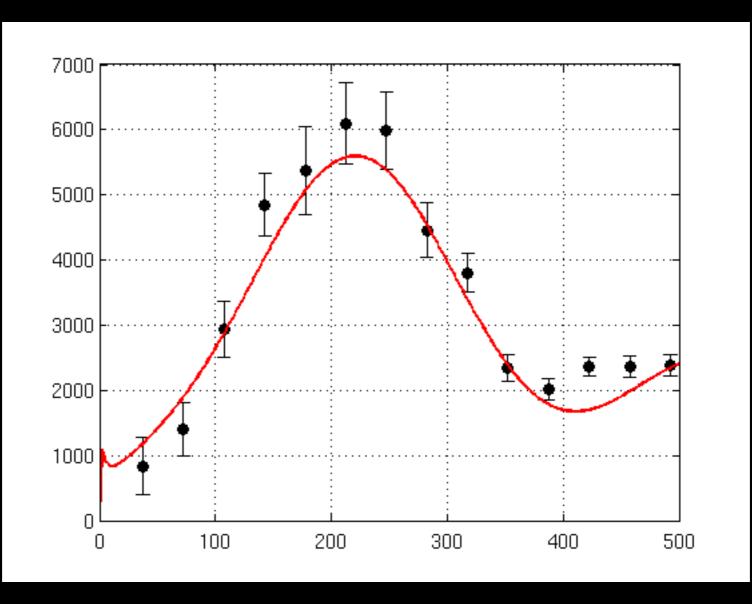
(The analysis insensitive to the choice of fiducial model.)



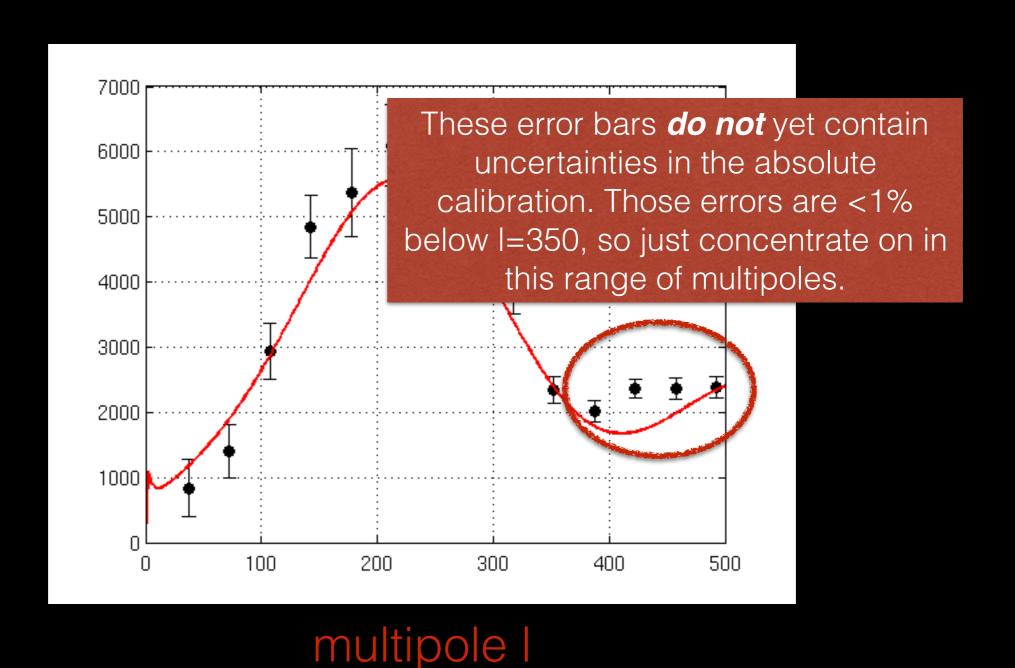


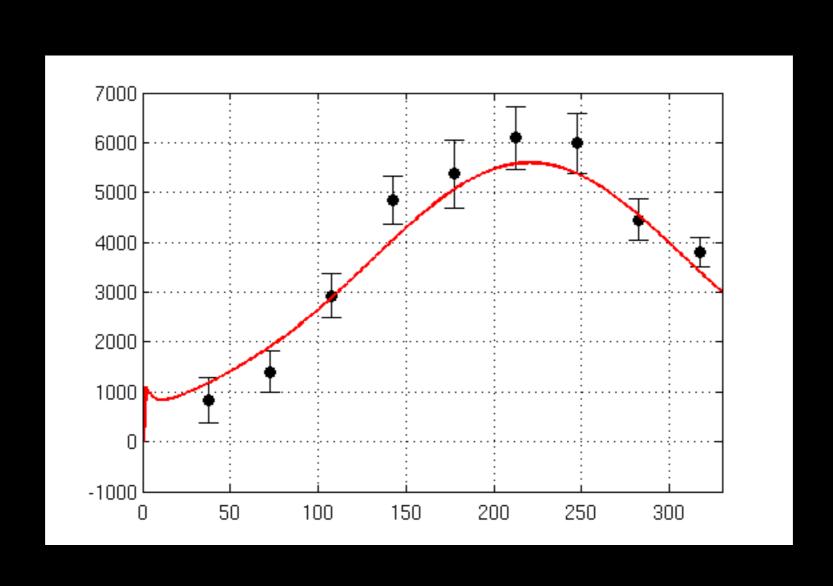
Replace the simulations with error bars equal to their standard deviation, centered on the real data points





multipole I





multipole I

If you can demonstrate you don't have to worry about instrumental systematics, derive some model parameter likelihoods and publish.

Revisit models as necessary, but the data points and uncertainties stand.

PRL 112, 241101 (2014)

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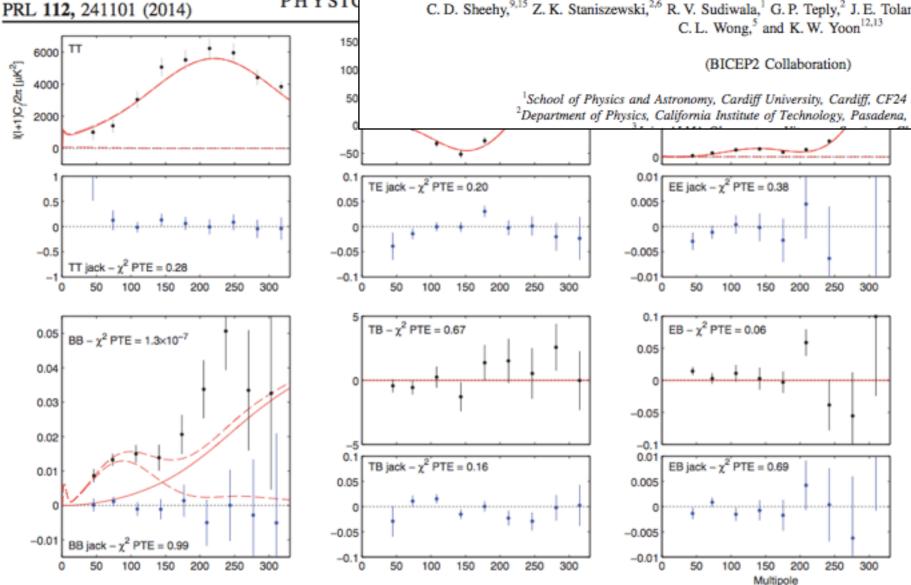
week ending 20 JUNE 2014



Detection of B-Mode Polarization at Degree Angular Scales by BICEP2

P. A. R. Ade, R. W. Aikin, D. Barkats, S. J. Benton, C. A. Bischoff, J. J. Bock, A. Brevik, I. Buder, E. Bullock, C. D. Dowell, L. Duband, J. P. Filippini, S. Fliescher, S. R. Golwala, M. Halpern, M. Hasselfield, M. Hasse S. R. Hildebrandt, ^{2,6} G. C. Hilton, ¹¹ V. V. Hristov, ² K. D. Irwin, ^{12,13,11} K. S. Karkare, ⁵ J. P. Kaufman, ¹⁴ B. G. Keating, ¹⁴ S. A. Kernasovskiy, ¹² J. M. Kovac, ^{5,*} C. L. Kuo, ^{12,13} E. M. Leitch, ¹⁵ M. Lueker, ² P. Mason, ² C. B. Netterfield, ^{4,16} H. T. Nguyen, ⁶ R. O'Brient, ⁶ R. W. Ogburn IV, ^{12,13} A. Orlando, ¹⁴ C. Pryke, ^{9,7,†} C. D. Reintsema, ¹¹ S. Richter, ⁵ R. Schwarz, ⁹ C. D. Sheehy, ^{9,15} Z. K. Staniszewski, ^{2,6} R. V. Sudiwala, ¹ G. P. Teply, ² J. E. Tolan, ¹² A. D. Turner, ⁶ A. G. Vieregg, ^{5,15} C. L. Wong, ⁵ and K. W. Yoon ^{12,13}

> School of Physics and Astronomy, Cardiff University, Cardiff, CF24 3AA, United Kingdom Department of Physics, California Institute of Technology, Pasadena, California 91125, USA



PHYSIC

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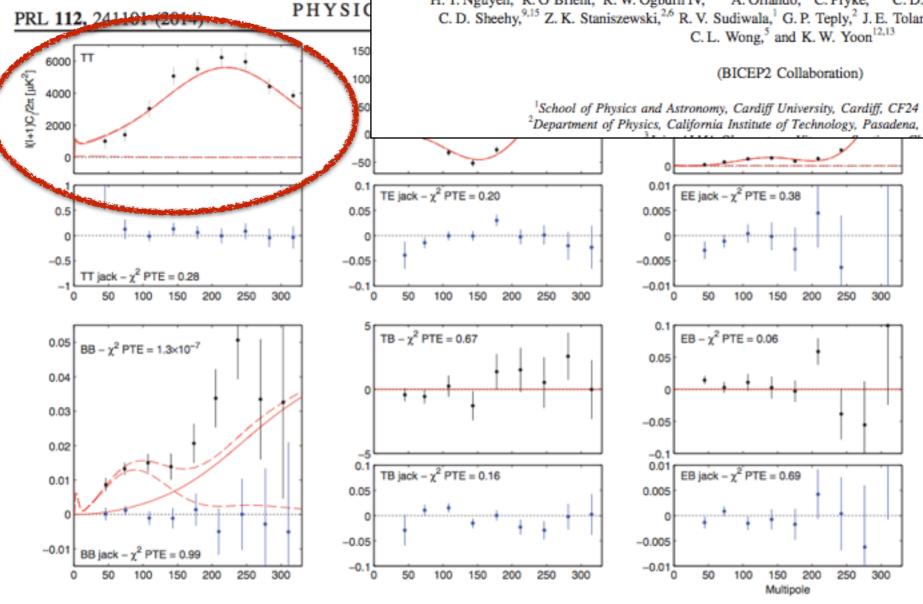
week ending 20 JUNE 2014

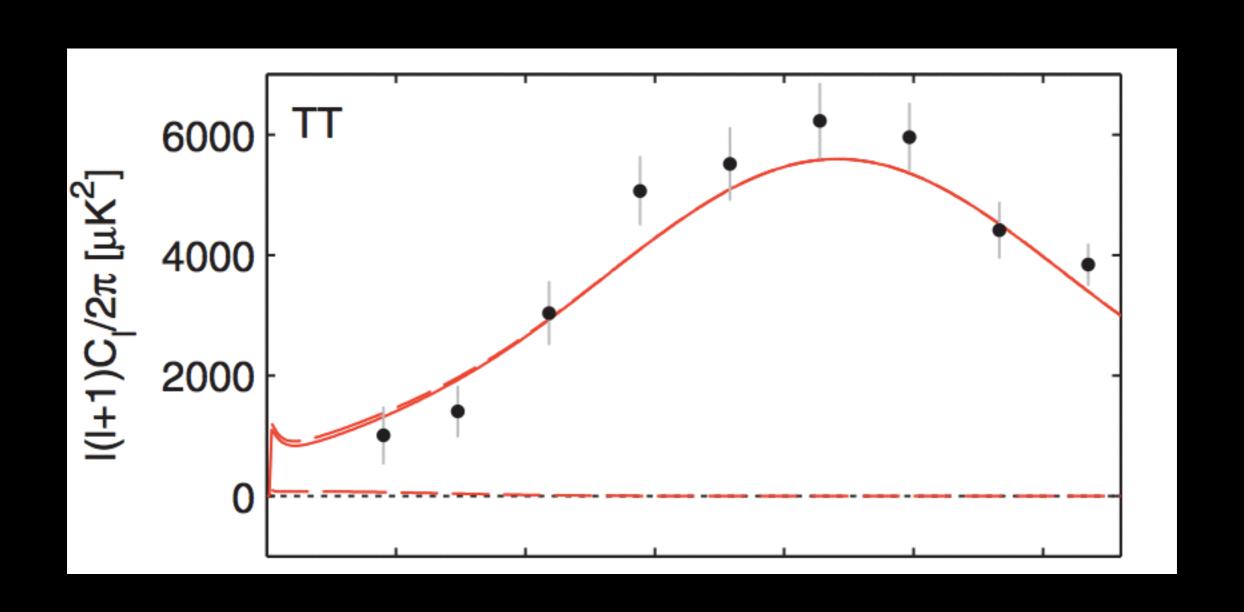


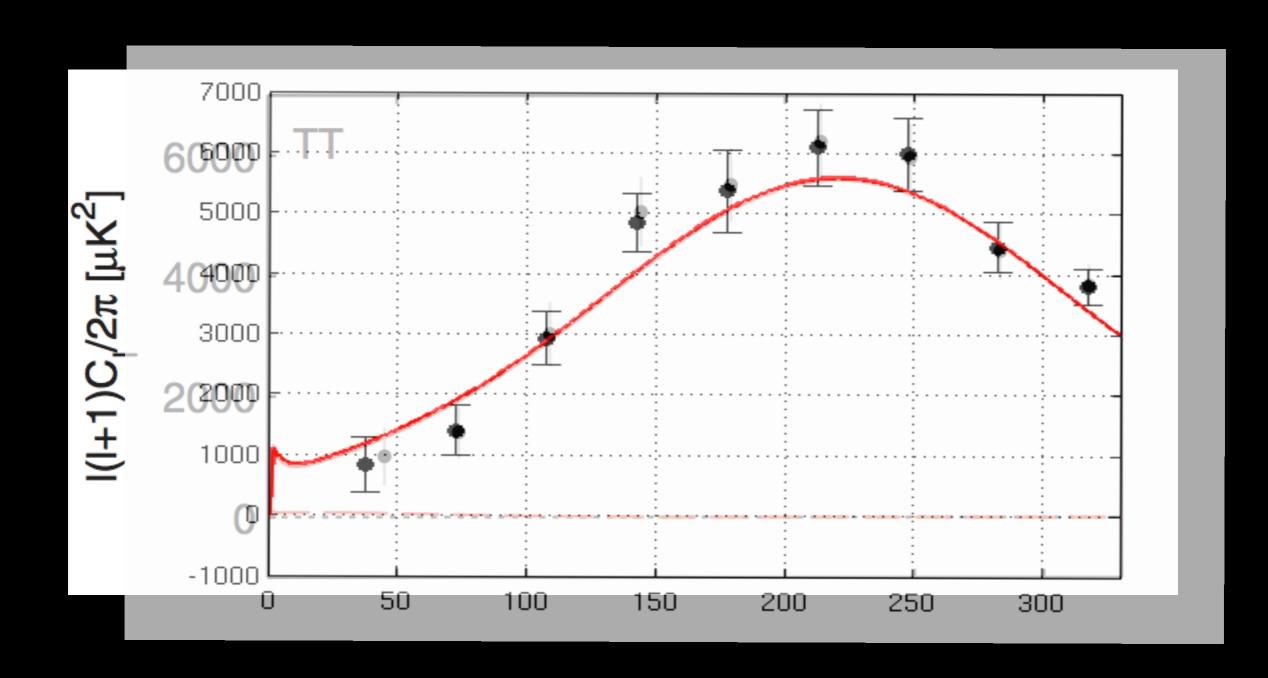
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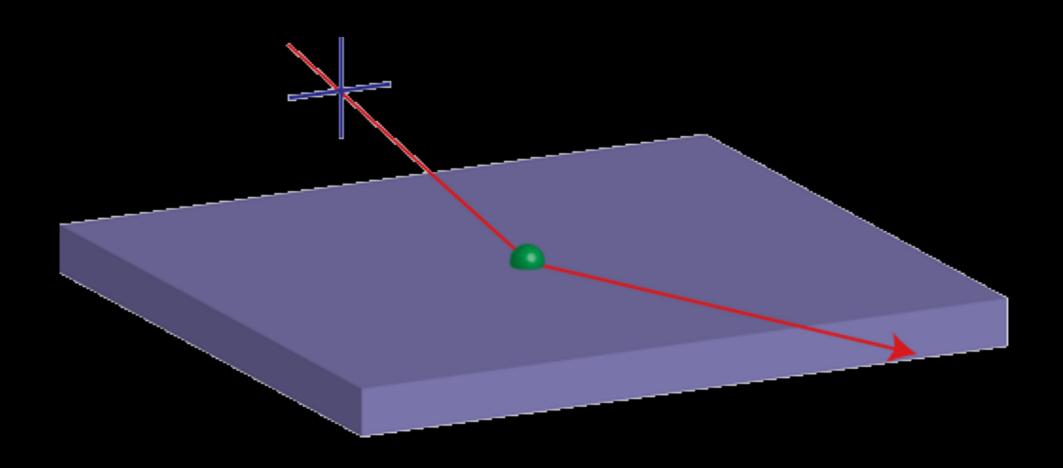


There are some subtle differences arising from the fact that this worked example did not include effects of mode mixing, which changes things slightly (for instance the lowest point should not be plotted at the exact bin center like we did), but it's pretty good!

The CMB is polarized

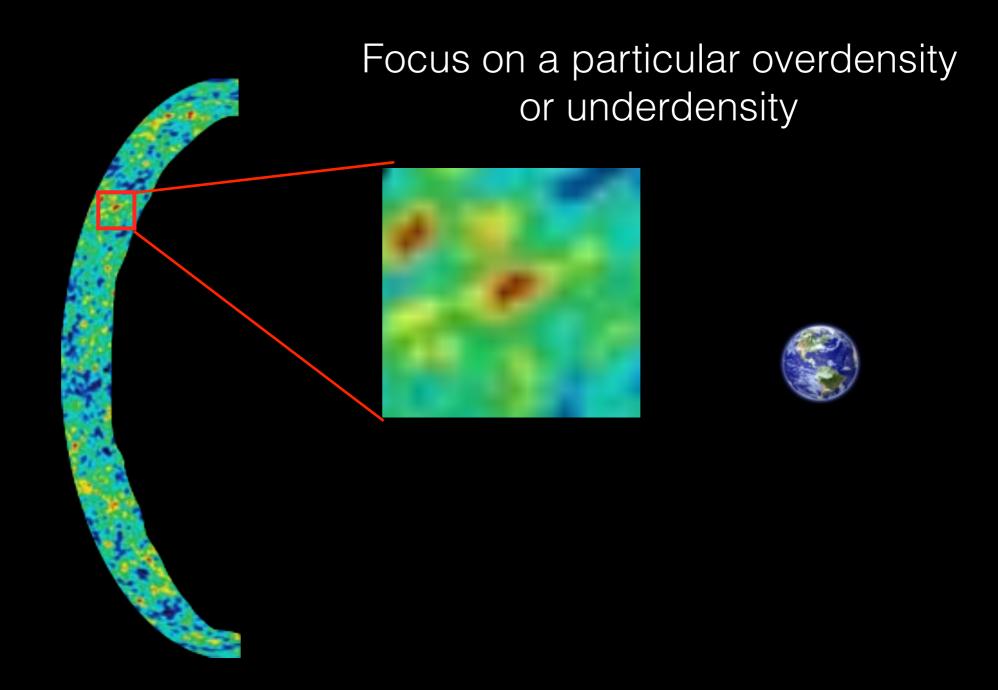
Generation of polarization by anisotropy

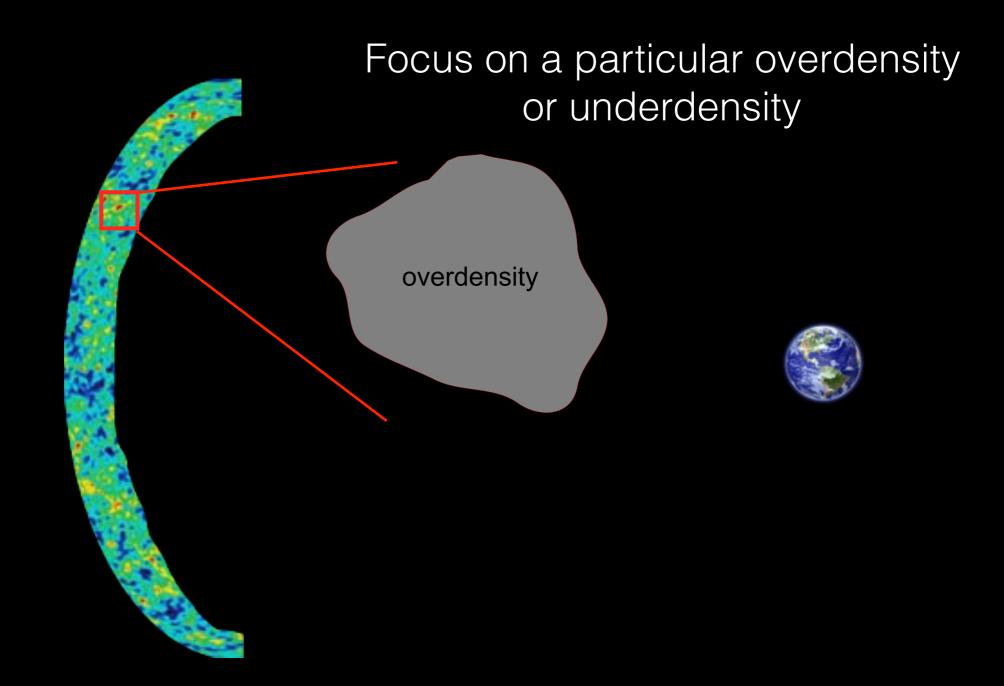
- Heuristically, scattering of light can be thought of as an incoming electric field "shaking" an electron that then re-radiates as a dipole
- Explains polarization of reflected light off a surface because the shaking occurs preferentially in one direction (anisotropy)



The plasma is not stationary.

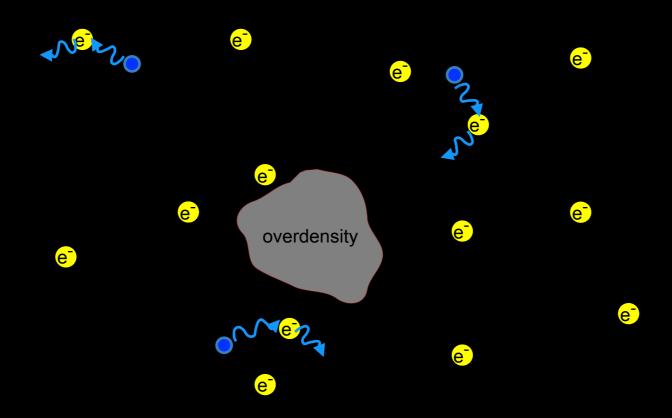
Motion in the plasma at the time of recombination imparts a small net polarization to the photons that scatter off it.



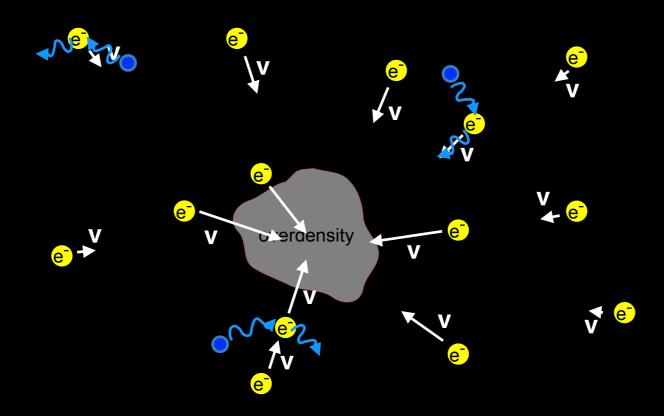




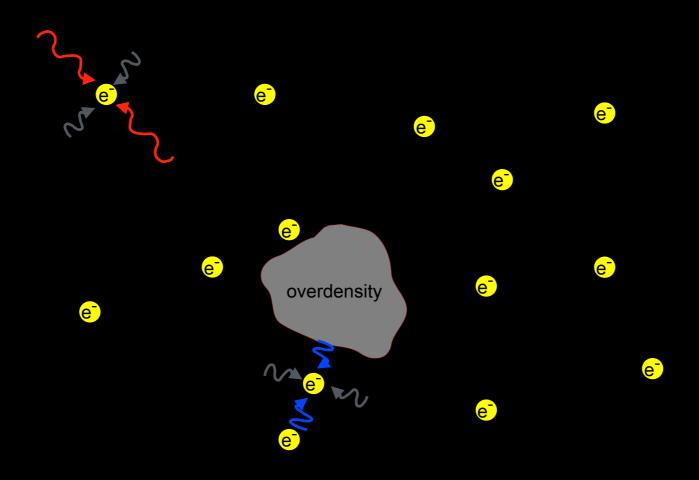
A CMB photon we see is one whose last scattering off of a free electron was in the direction of Earth.



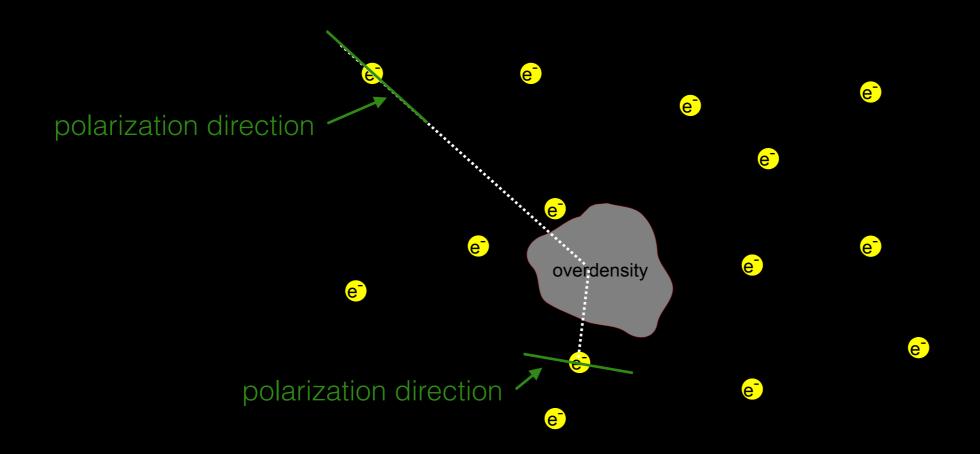
The scattering happens in a medium with a bulk velocity flow! There are *gradients* in the velocity field.



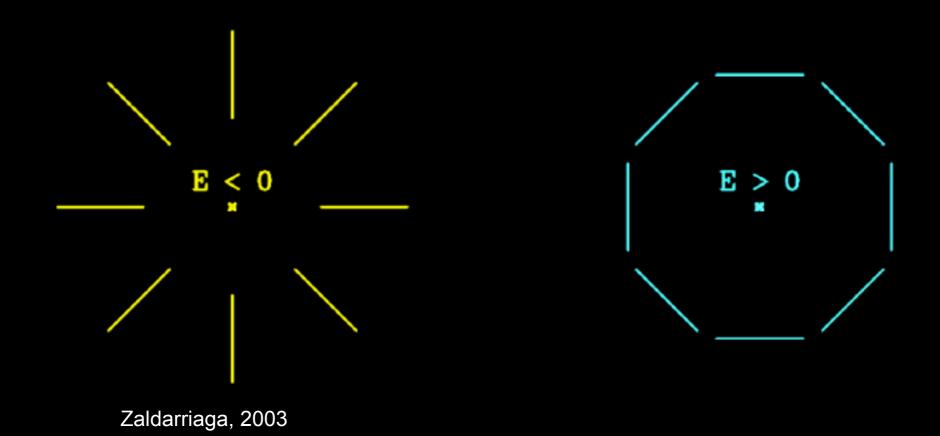
In the rest frame of an electron, diverging/converging flow causes redshifting/blueshifting in the direction of the overdensity.



This "local quadrupole anisotropy" imparts a net polarization to the scattered light. The polarization direction is *always* either parallel or perpendicular to the direction pointing toward the overdensity.



This is a pure "E-mode" (i.e. a vector pattern with no curl component)

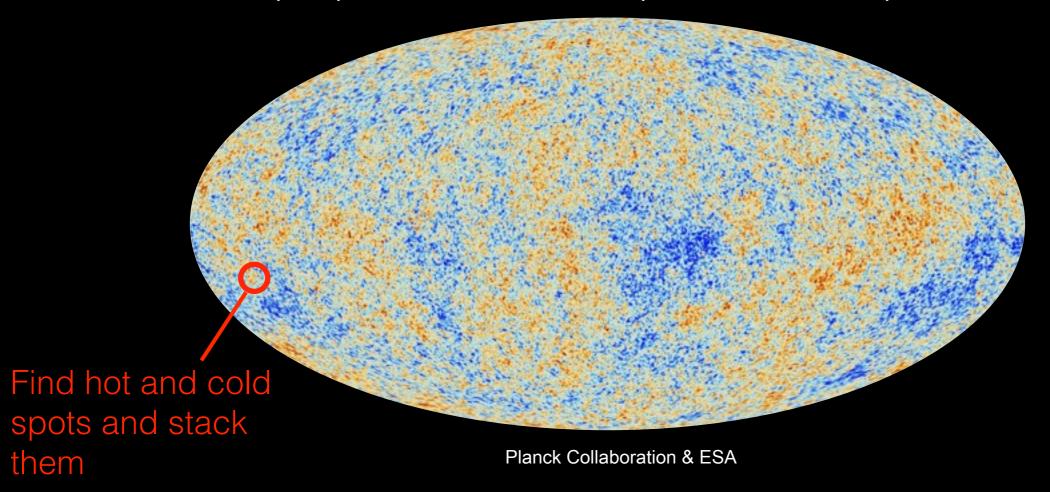


E-modes and B-modes are an orthogonal basis.

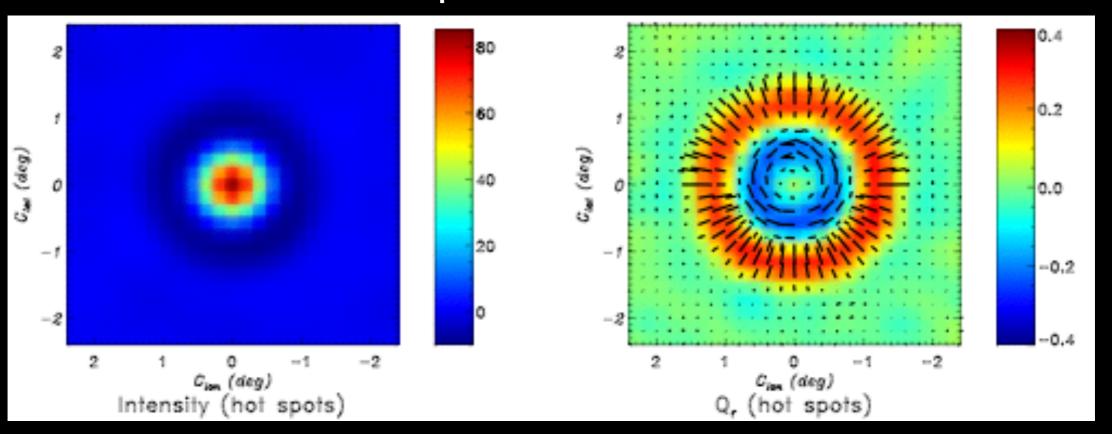
In the standard cosmology, there are *no* B-modes (i.e. patterns with *only* curl and no divergence)



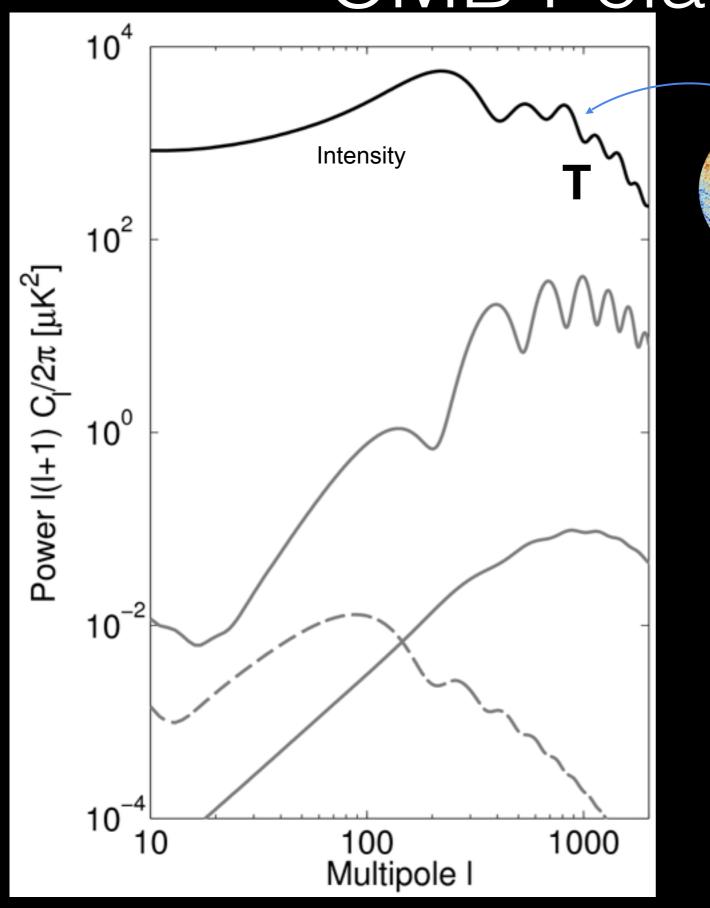
The polarization pattern on the sky is a superposition of these pure E-mode patterns.

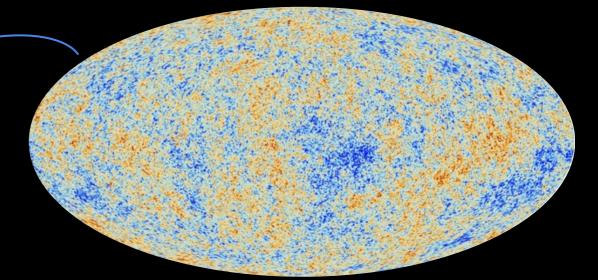


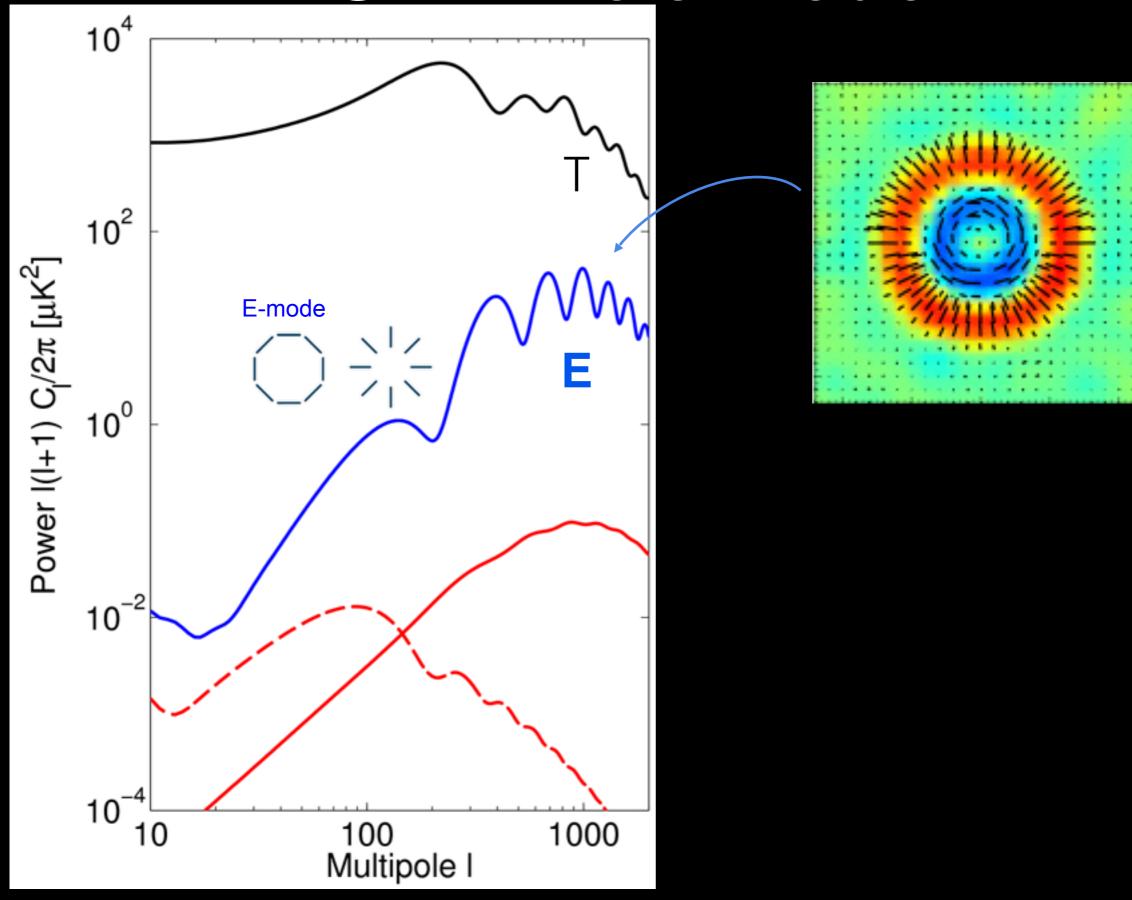
Planck polarization maps stacked over CMB hot spots — pure E-mode

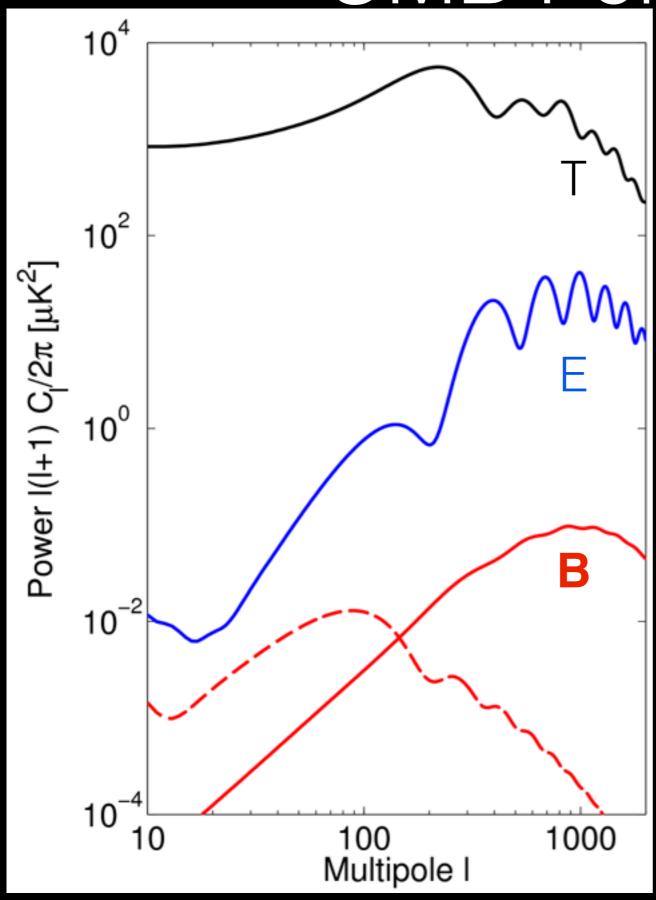


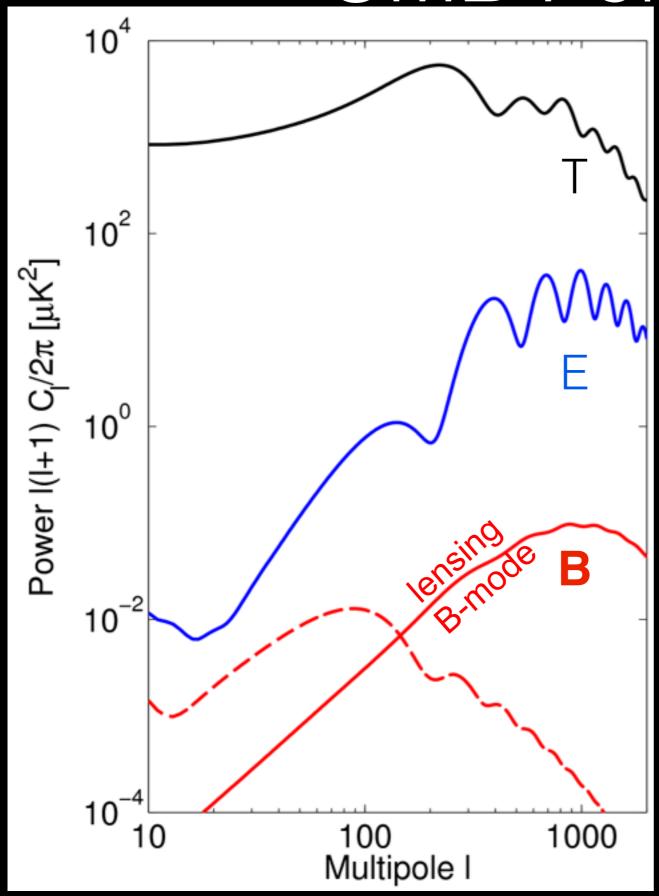
Planck collaboration (2013)





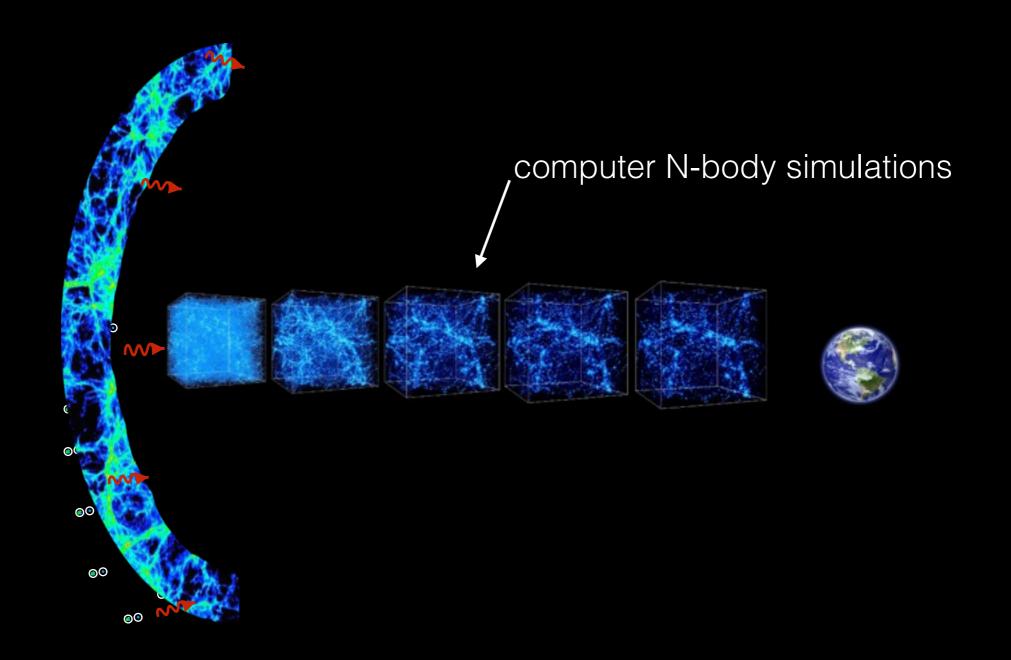






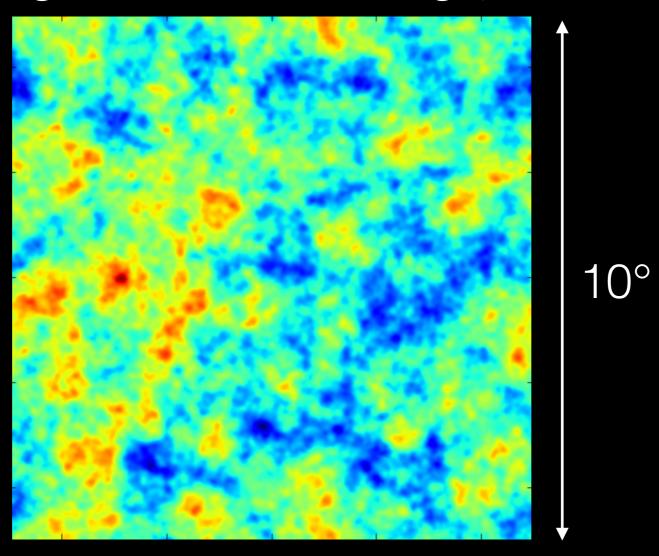
Gravitational lensing of CMB

CMB photons moving through the evolving large scale structure of the universe are gravitationally lensed a little bit



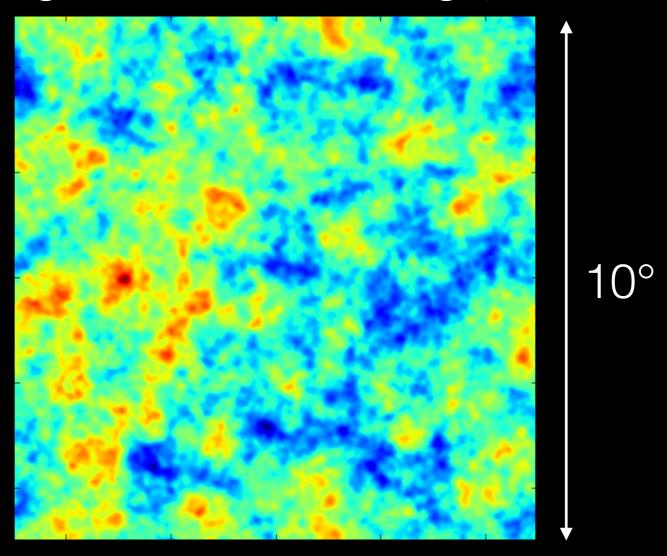
Gravitational lensing of CMB

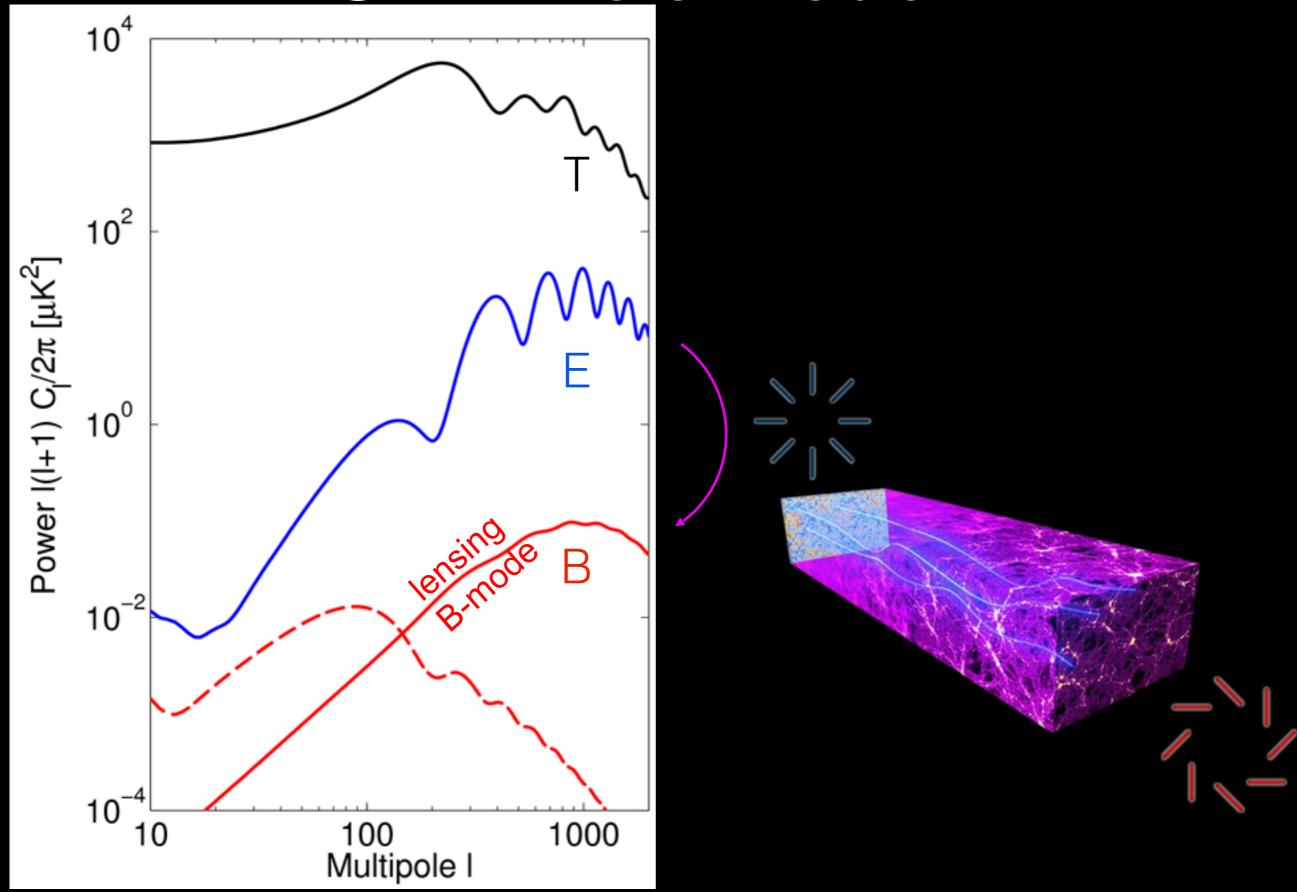
before gravitational lensing (simulated)

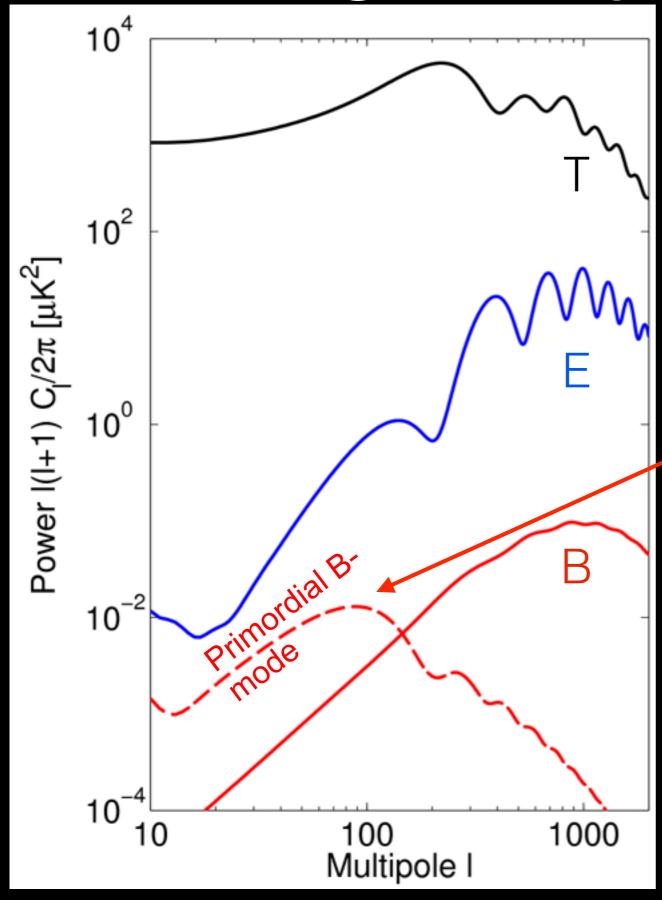


Gravitational lensing of CMB

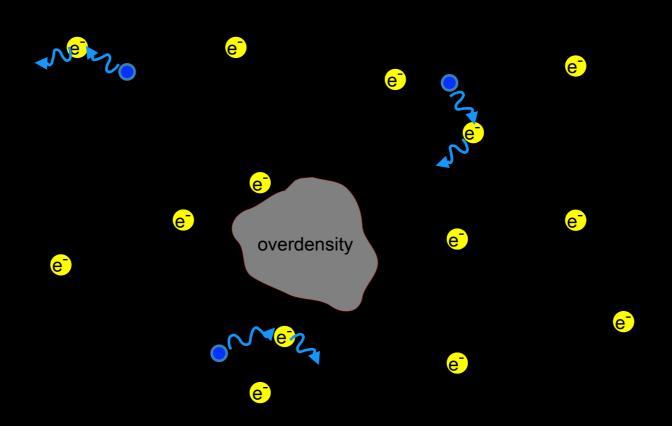
after gravitational lensing (simulated)

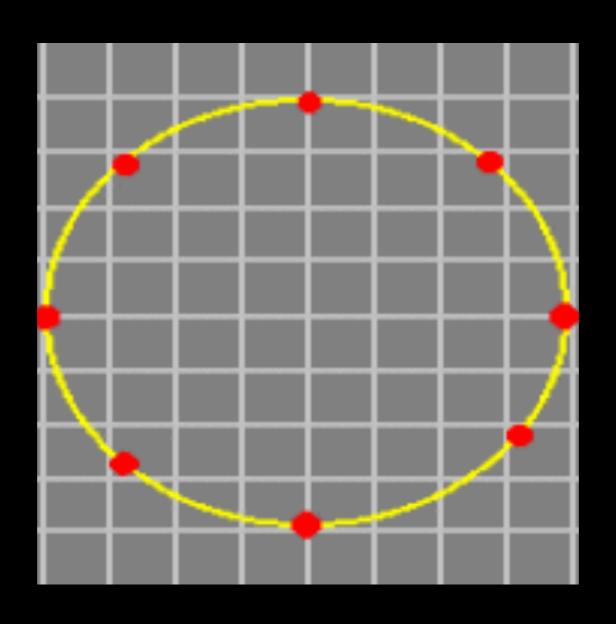


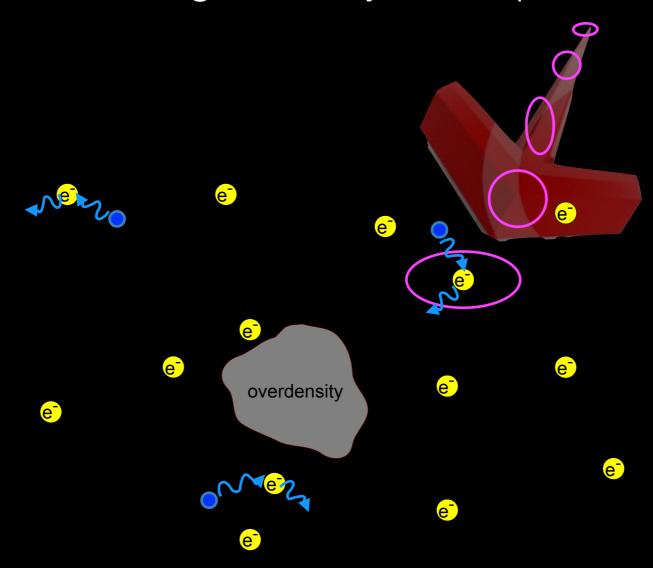


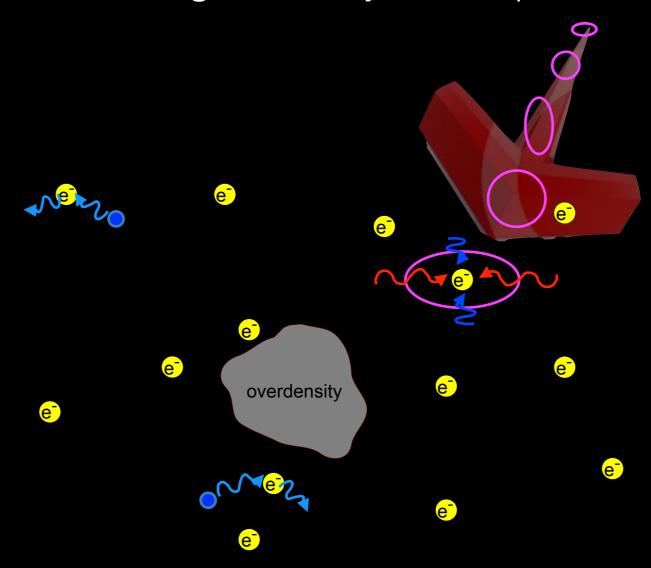


B-modes from primordial gravitational waves

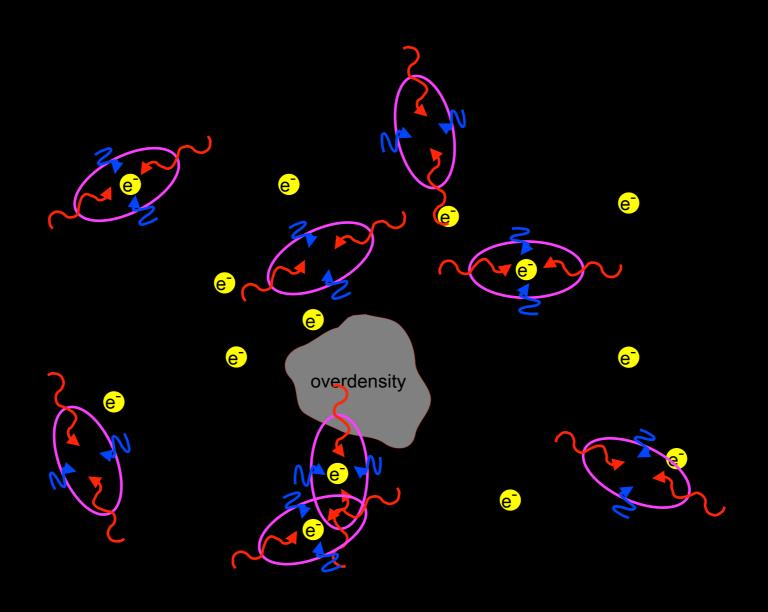




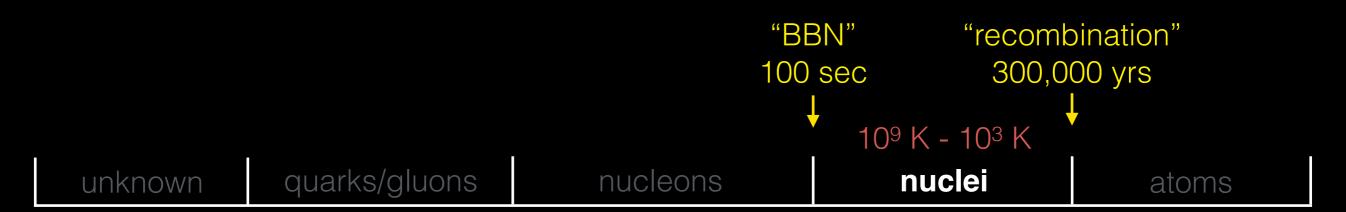




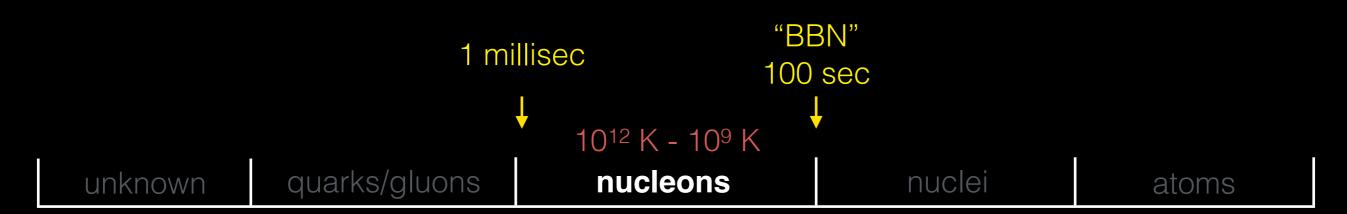
Their random orientations produce E-modes and B-modes nearly *indiscriminately*.



Whence the gravitational waves?



Evidence: light element abundances (H, He, Li) match predictions of Big Bang Nucleosynthesis



No direct evidence from observational cosmology, but physics is testable at collider energies









Inflation?

Exponential expansion turns quantum fluctuations into macroscopic density inhomogeneities.

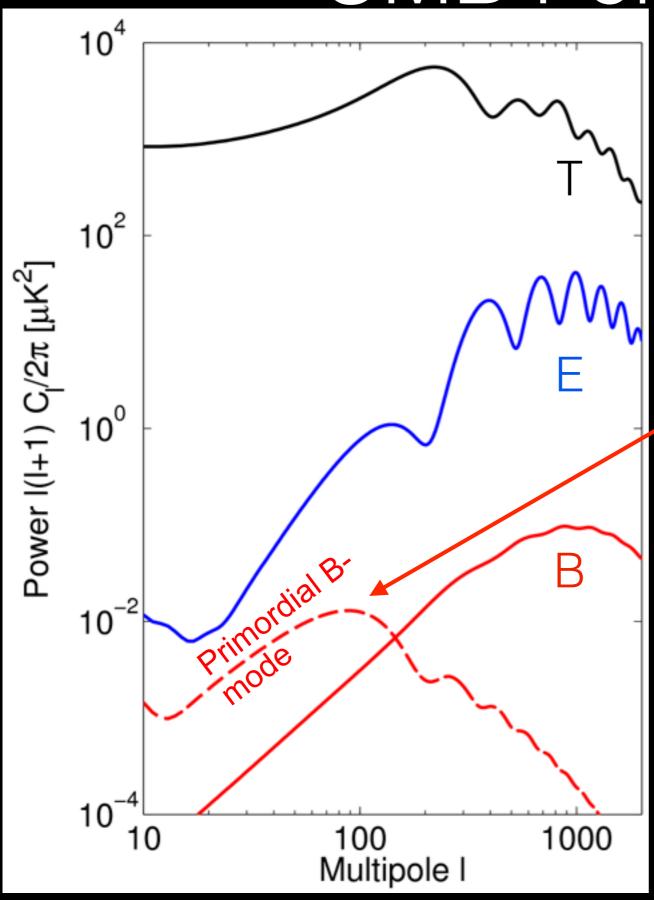


Inflation?

density inhomogeneities ↔ scalar metric perturbations gravitational waves ↔ tensor metric perturbations

Inflation produces both!

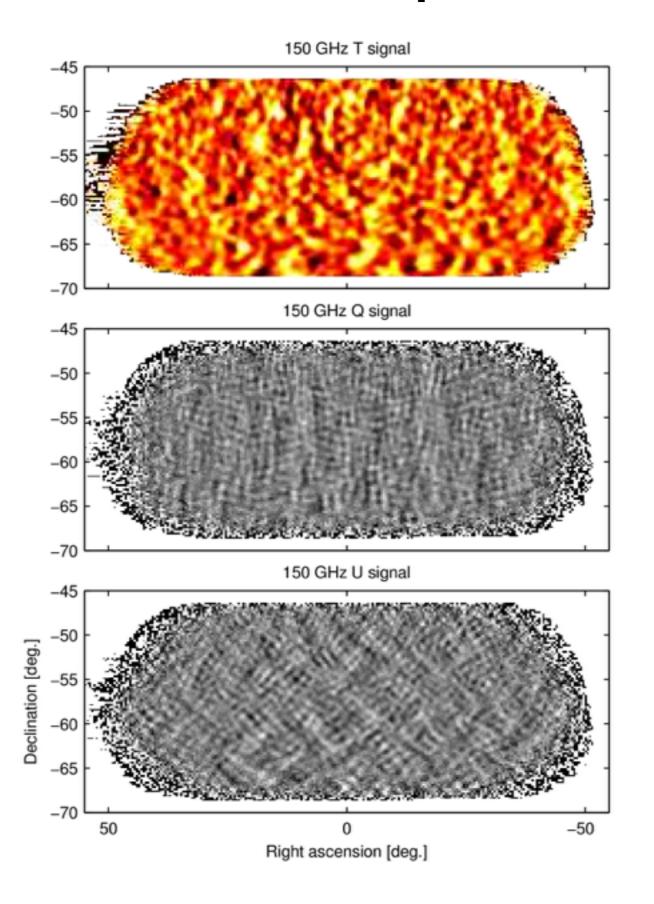
The ratio of the amplitude of tensor perturbations to scalar perturbations is parametrized by r=T/S



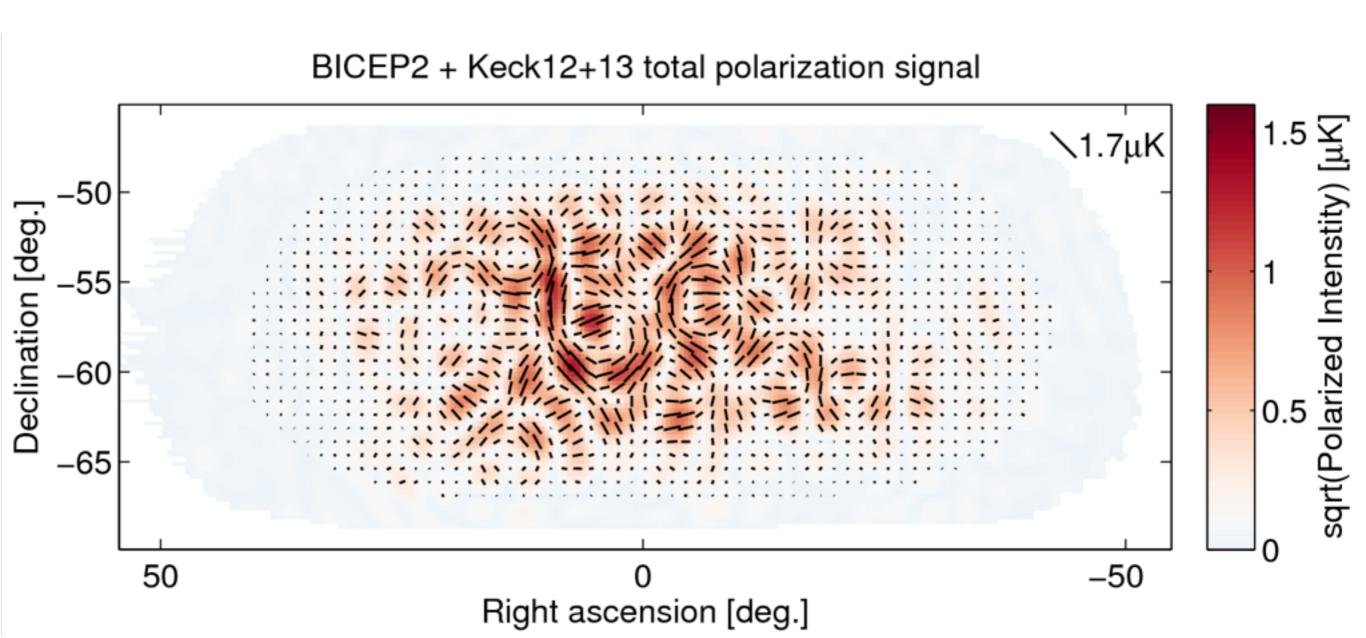
Inflationary gravitational waves are unique source of B-modes

- → peaking at l≈100: degree scales
- → amplitude directly proportional to r

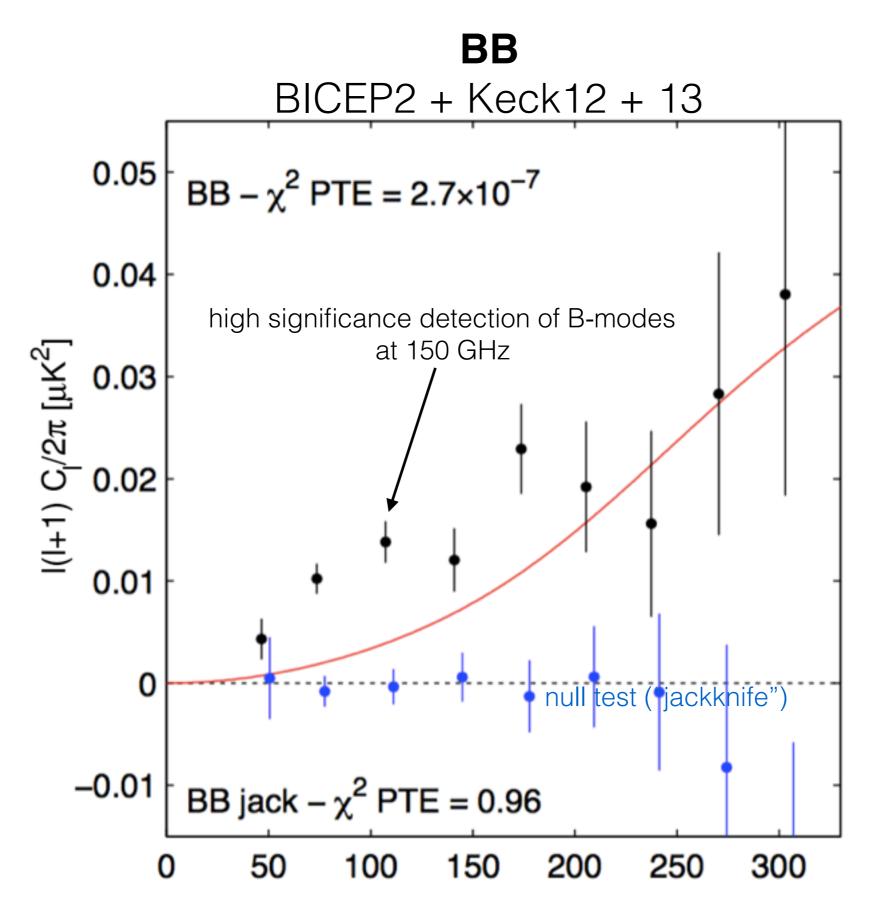
BICEP2 maps



Total Polarization



Using all data collected through 2013



Polarized galactic

synchrotron dominates

at low frequencies

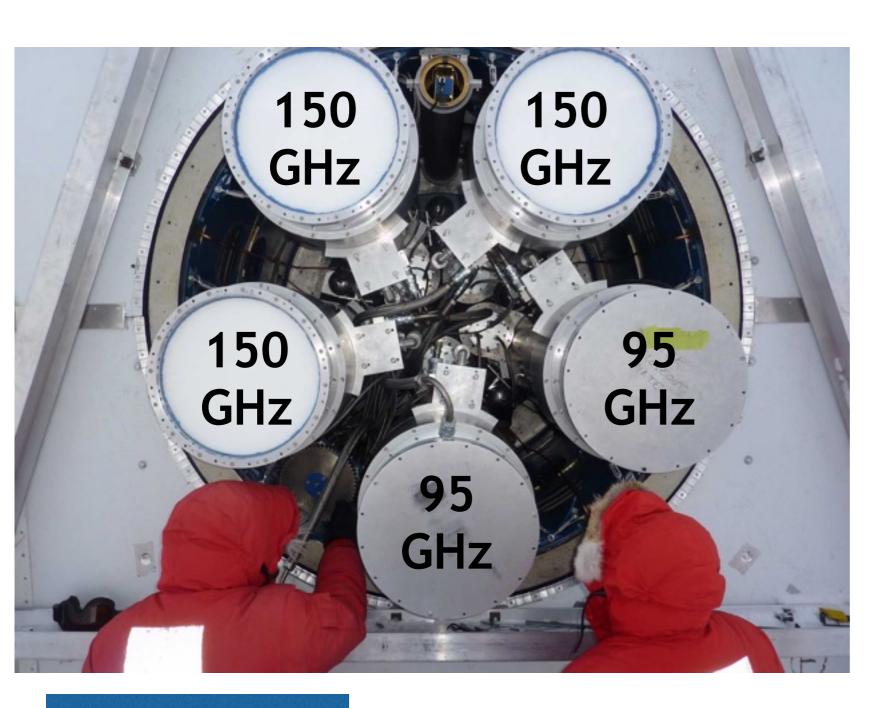
Polarized Galactic Foregrounds as seen by the Planck satellite.

Polarized thermal emission (~20K) from galactic **dust** aligned in magnetic fields dominates at high frequencies

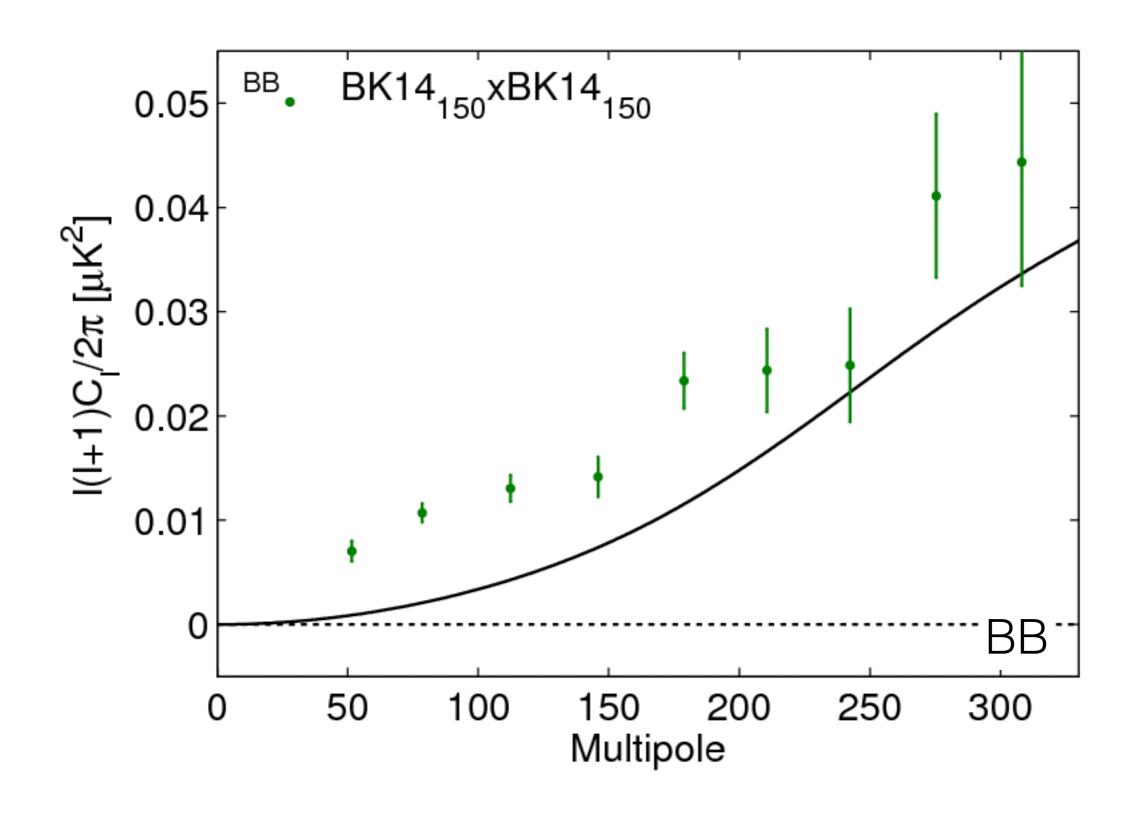
30 GHz 44 GHz **70 GHz** 100 GHz 143 GHz 217 GHz 353 GHz

The BICEP/Keck Collaboration

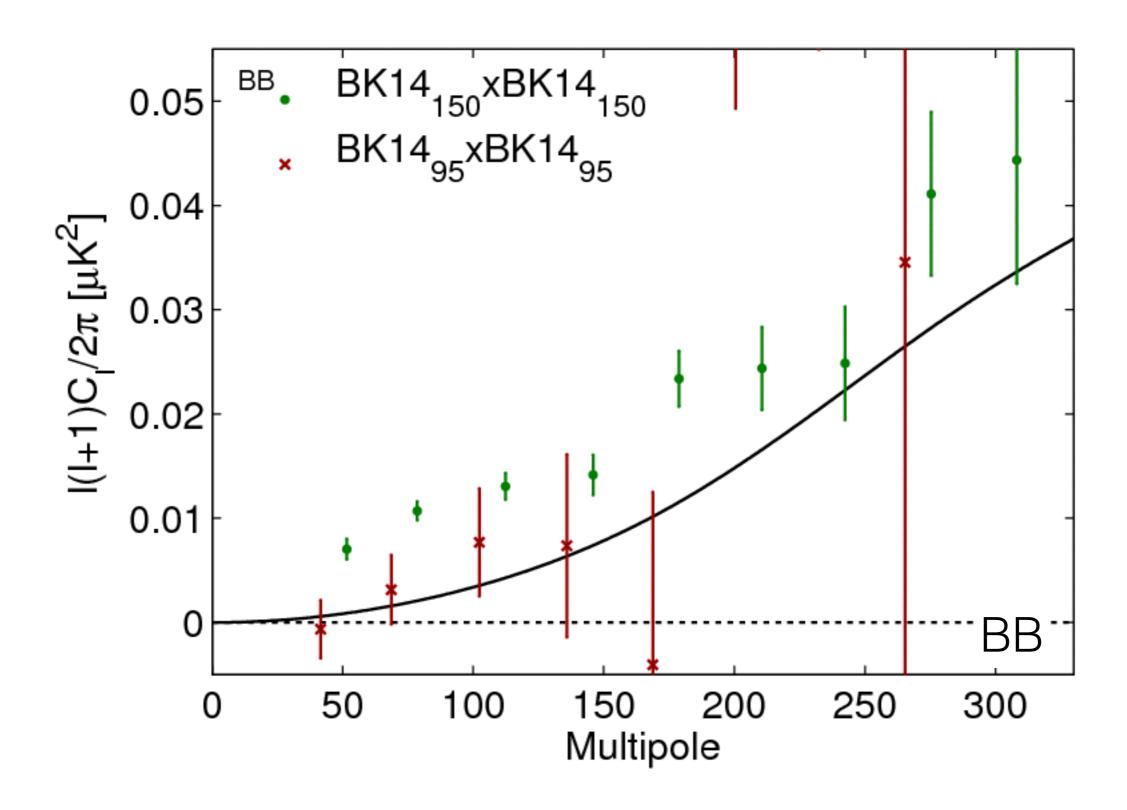
Keck Array Frequency Coverage



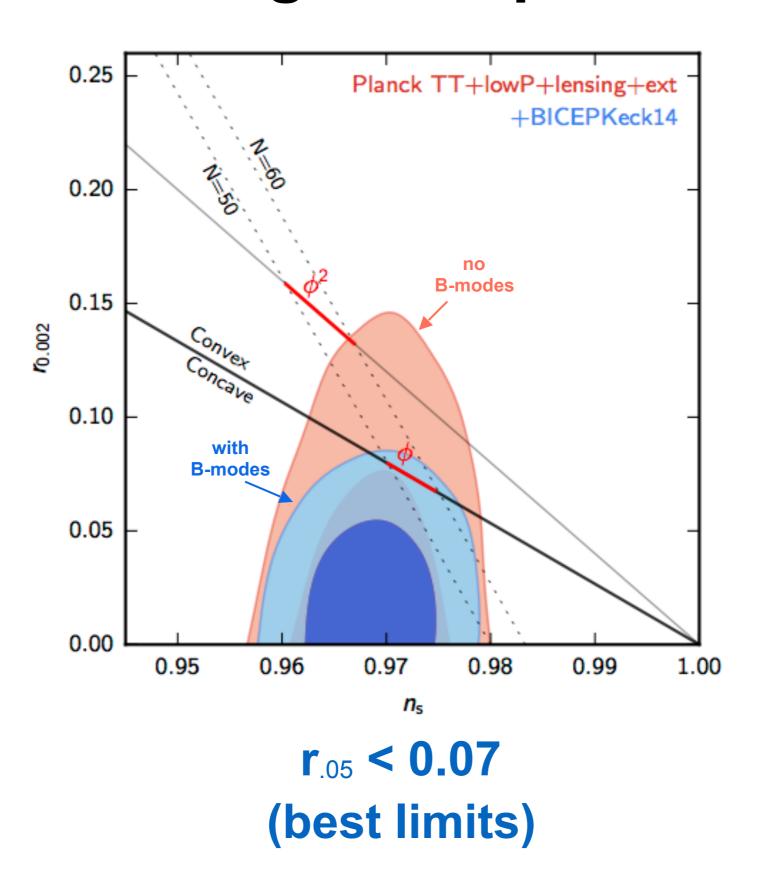
BICEP2 + Keck BB auto and cross-spectra



BICEP2 + Keck BB auto and cross-spectra



Adding in temperature



The current push is to continue making very deep maps at many frequencies to disentangle galactic foregrounds from the CMB.

Thanks!